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1) Find the Time complexity of the recurrence relation
$$T(n) = T(n-1) + n.$$

$$T(n-1) + n, if n > 0,$$

$$T(n) = \begin{cases} 1, & n = 0. \end{cases}$$

Solution:

$$T(n) = T(n-1) + n$$
 (i)

$$T(n) = T(n-2) + (n-1) + n - (ii)$$

$$T(n) = \left[T(n-3) + (n-2)\right] + (n-1) + n - For (ii) Substritute value
 $T(n) = T(n-3) + (n-2) + (n-1) + n - (iii)$$$

$$T(n) = T(n-k) + T(n-(k-1)) + (n-(k-2)) + ---- + (n-1) + n$$

$$T(n) = T(n-n) + (n-n+1) + (n-n+2) + - - - + (n-1) + n$$

$$T(n) = T(0) + 1 + 2 + --- + (n-1) + h$$

Sum g n natural numbers.

$$T(n) = 1 + n(n+1) = n^2 + n$$

Time Complexity is O(n2).

2) Recursive tree for the computation of Power (2,5) and give o(n) Answers input size: n Function call: n-1 Time taken: O(n) Represent the Recurrence Tree for the Previous Function 1 if n=0 (power(2,5), if n>0 xeturn 8 * 4 = 32 Power (2,4) return 4*2 = 8 veturn 2 # 2 = 4 veturn 1*1*2 = 2 power (2, 2) return 1 DOWER (2,0) 32 Power (2,5) Power (2,2) Power (2,3) 2 4 Power(2,1) Power(2,1) Power(2,2) Power(2,1)

3) Recursive algorithm for finding the maximum element in a sequence, s, of an n element. Give Pseudocode. What is the running time and space usage of this Algorithm & Answerd Algorithm Max (A, M) inputo Array A, & integers. element in Such that O < n < 1A). outputs max value of the n element in A. Pseydo Corele: if n=0 then return 0 else it (max (A, n-1) < A[n-1]) else return (max (A, M-1) > The ounning time is O(n).

4) Amounte the sequences according to the order of complexity:

A. n3, 10 lugn, 57 vn, 49 lugn, 2h.

Answer: 49 log logn < 10 logn < 57 vn < n3 < 2n.

B. 6897 niogn, 5n5, 2nh, 8510gn, 10000n.

<u>Answer:</u> 85 logn < 10000n < 6897 n logn < 5 n < 2nn.

c. $2 n \sqrt{n}$, 36485, 73 [n/2], 2^{18} , $5n^2$.

Answer: $36485 < 2^{18} < 73[^{n}/_{2}] < 2n\sqrt{n} < 5n^{2}$.