Congratulations! You passed!

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1 / 1 point

1. Given the vectors:

 \vec{v} = (1, 0, 7)

 \vec{w} = (0, -1, 2)

find the distance between them, $d(\vec{v}, \vec{w})$.

- \bigcirc 5
- O -2
- \bigcirc $\sqrt{(23)}$

✓ Correct

Correct! $d(\vec{v}, \vec{w}) = \sqrt{(0-1)^2 + (-1-0)^2 + (2-7)^2}$

2. You are given the points P: (1, 0, -3) and Q: (-1,0,-3). The magnitude of the vector from P to Q is:

- 2
- O 3
- O -2

Corre

Correct! The magnitude of the vector is the distance between points P and Q, which you find by using the following: $\sqrt{((-1)-1)^2+0^2+((-3)-(-3))}=\sqrt{4}=2$

3. Select the correct statements pertaining to the dot product.

0.5 / 1 point

1/1 point

- The dot product of orthogonal vectors is always 0.
- Correct

Correct! Since both vectors are perpendicular to each other, the dot product is always 0.

- ☐ The dot product of orthogonal vectors is always 1.
- lacktriangle The dot product vector is the diagonal in a parallelogram formed by the two vectors $ec{u}$ and $ec{v}$.

(X) This should not be selected

Not quite. This is the sum of two vectors.

☐ The dot product of two vectors is always a scalar.

4. Calculate the norm ||v|| of the vector $\vec{v} = (1, -5, 2, 0, -3)$ and select the correct answer.

- $\bigcirc \ \|v\| = 5$
- $\bigcirc \ \|v\| = \sqrt{35}$
- ||v|| = 39
- $||v|| = \sqrt{39}$

Correct!
$$||v|| = \sqrt{((1^2) + (-5)^2 + 2^2 + 0^2 + (-3)^2)} = \sqrt{39}$$

5. Which of the vectors has the greatest norm?

1/1 point

$$\begin{bmatrix}
1 \\
0 \\
-2 \\
0 \\
-1
\end{bmatrix}$$

$$leftondown\left[2 \atop 5 \end{matrix} \right]$$

()	1
	2
	-3

- \circ $\begin{bmatrix} 2\\2\\2\\2\\2\end{bmatrix}$
- 0 0 0 0 \circ

⊘ Correct

Correct! The norm of the vector is $\sqrt{(2^2)+(5^2)}=\sqrt{29}$ which is larger than the other vectors in the options given.

6. Calculate the dot product $\vec{a} \cdot \vec{b}$ and select the correct answer.

1/1 point

$$\vec{a} = \begin{bmatrix} -1 \\ 5 \\ 2 \end{bmatrix}, \vec{b} = \begin{bmatrix} -3 \\ 6 \\ -4 \end{bmatrix}$$

- O 30
- $\bigcirc \begin{bmatrix}
 -3 \\
 30 \\
 -8
 \end{bmatrix}$
- 25

✓ Correct

Correct! By applying the formula you saw in the video <u>The dot product</u> ∠ as follows: $\vec{a} \cdot \vec{b} = ax \cdot bx + ay \cdot by + az \cdot bz$, you have:

$$\vec{a} \cdot \vec{b} = (-1) \cdot (-3) + 5 \cdot 6 + 2 \cdot (-4) = 3 + 30 - 8 = 25.$$

7. Which of the following is the result of performing the multiplication $M_1 \cdot M_2$? Where M_1 and M_2 are given by:

1 / 1 point

1/1 point

$$M_1 = \begin{bmatrix} 2 & -1 \\ 3 & -3 \end{bmatrix}, M_2 = \begin{bmatrix} 5 & -2 \\ 0 & 1 \end{bmatrix}.$$

- $\bigcirc
 \begin{bmatrix}
 10 & 3 \\
 15 & 4
 \end{bmatrix}$
- $\begin{bmatrix}
 10 & 15 \\
 -3 & -4
 \end{bmatrix}$

Correct! Remember from the video ${\rm \underline{Matrix}}$ ${\rm \underline{Multiplication}}$ ${\rm \underline{L}}^3$, to multiply matrices, you have: $\begin{bmatrix} c_1 & c_2 \\ c_3 & c_4 \end{bmatrix}$ where in the matrices given:

$$c_1 = 2 \cdot 5 + (-1) \cdot 0 = 10,$$

$$c_2 = 2 \cdot (-2) + (-1) \cdot 1 = -5,$$

$$c_3 = 3 \cdot 5 + (-3) \cdot 0 = 15,$$

$$c_4 = 3 \cdot (-2) + (-3) \cdot 1 = -9.$$

When you replace these values back onto the matrix, you obtain: $\begin{bmatrix} 10 & -5 \\ 15 & -9 \end{bmatrix}$

8. Calculate the dot product $ec{w} \cdot ec{z}$ and select the correct answer.

$$\vec{w} = \begin{bmatrix} -9 \\ -1 \end{bmatrix}, \vec{z} = \begin{bmatrix} -3 \\ -5 \end{bmatrix}$$

$$\left[\begin{array}{c}
-27 \\
-5
\end{array}\right]$$

$$\bigcirc \text{ Correct}$$

$$\text{Correct! } \vec{w} \cdot \vec{z} = \begin{bmatrix} -9 \\ -1 \end{bmatrix} \cdot \begin{bmatrix} -3 \\ -5 \end{bmatrix} = (-9) \left(-3 \right) + (-1) \left(-5 \right) = 32$$