

## Carbon Dating

You probably have seen or read news stories about fascinating ancient artifacts. At an archaeological dig a piece of wooden tool is unearthed and the archaeologist finds it to be 5,000 years old. A child mummy is found high in the Andes and the archaeologist says the child lived more than 2,000 years ago. Ever wondered how they know?

Carbon dating is a way of determining the age of certain archaeological artifacts of biological origin. Your job is to write a program that figures out how old a sample is.



*This is a real velociraptor fossil. It's very old.*

When an organism is alive, its matter will have a constant amount of a special type of carbon called carbon-14 ( $c_{14}$ ). It turns out all living things have the same fraction: wood, mammoths, your body right now... small cats... all have the same amount.

An important property of  $c_{14}$  is that it disappears at a constant rate: every 5,700 years the amount of  $c_{14}$  is halved (its half life is 5,700 years). For example, if one starts with 100% of the natural occurrence of  $c_{14}$ :

In 5,700 years we expect there will only be 50% left.

In 11,400 years we would expect there will only have 25% left.

And so on...

When an organism is alive, it keeps replenishing its supply of  $c_{14}$  to the natural level. But when it dies (moment of silence), the amount of  $c_{14}$  starts to decrease. By testing how much  $c_{14}$  is left, scientists know how long a dead thing has been dead for. Good times.

## Lookup Table

To get started, let's make a lookup table that maps the percent of c14 remaining to the number of years the sample has been dead for. Print out the percent c14 remaining, and the number of years passed for the first 20 half lives. Your table should look like the following:

```
Carbon dating lookup table
percent C-14 remaining:  years passed
-----
100.0%:  0 years
50.0%:   5700 years
25.0%:  11400 years
12.5%:  17100 years
6.25%:   22800 years
3.125%:  28500 years
1.5625%: 34200 years
0.78125%: 39900 years
0.390625%: 45600 years
0.1953125%: 51300 years
0.09765625%: 57000 years
0.048828125%: 62700 years
0.0244140625%: 68400 years
0.01220703125%: 74100 years
0.006103515625%: 79800 years
0.0030517578125%: 85500 years
0.00152587890625%: 91200 years
7.62939453125E-4%: 96900 years
3.814697265625E-4%: 102600 years
1.9073486328125E-4%: 108300 years
```

Think about the variable type that you use to keep track of the amount of carbon left. What happens if you use an integer for percent?

## Extension

If you finish early, and have extra time, try this extension.

For scientists it will be much more useful for them to input the percent of natural c14 that they measured, and have the program tell them the age. Repeatedly ask the user to enter a percent of natural c14 remaining and then output the age of their sample.

```
What percent of natural carbon-14 does your sample have? 99
99.0% carbon-14...
It is: 82.64754726215602 years old

What percent of natural carbon-14 does your sample have? 10
10.0% carbon-14...
It is: 18934.990140857964 years old

What percent of natural carbon-14 does your sample have? 0.001
0.0010% carbon-14...
It is: 94674.95070428985 years old

What percent of natural carbon-14 does your sample have? |
```

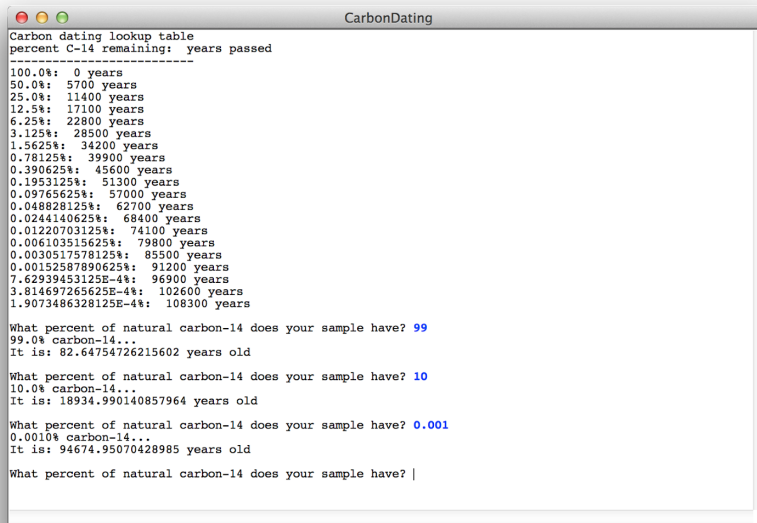
The formula for the age in years of a sample, given the percent of natural c14 remaining is:

$$\text{Age} = (\log(\text{percentage}/100) / -0.693) * 5700$$

To take the natural log of a number (the ln function) use the method:

`Math.log(value)`

Overall, your program should look like the following:



```

CarbonDating
Carbon dating lookup table
percent C-14 remaining: years passed
-----
100.0%: 0 years
50.0%: 5700 years
25.0%: 11400 years
12.5%: 17100 years
6.25%: 22800 years
3.125%: 28500 years
1.5625%: 34200 years
0.78125%: 39900 years
0.390625%: 45600 years
0.1953125%: 51300 years
0.09765625%: 57000 years
0.048828125%: 62700 years
0.0244140625%: 68400 years
0.01220703125%: 74100 years
0.006103515625%: 79800 years
0.0030517578125%: 85500 years
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