

```
def pseudoCode(inp,counter=0):  
    if inp[0]>inp[1]:  
        return 0  
    if inp[len(inp)-1]>inp[len(inp)-2]:  
        return len(inp)-1  
    if inp[len(inp)//2-1]<inp[len(inp)//2] and inp[len(inp)//2]>inp[len(inp)//2+1]:  
        return len(inp)//2+counter  
    elif inp[len(inp)//2-1]<inp[len(inp)//2] and inp[len(inp)//2]<inp[len(inp)//2+1]:  
        first_length=len(inp)  
        inp=inp[first_length//2:first_length]  
        counter+=first_length-len(inp)  
        return pseudoCode(inp,counter)  
    elif inp[len(inp)//2-1]>inp[len(inp)//2] and inp[len(inp)//2]>inp[len(inp)//2+1]:  
        first_length = len(inp)  
        inp=inp[0:first_length//2]  
        return pseudoCode(inp,0)
```

This code is here to be  
able to copy it and  
to run in interpreter.

Onur Yaman  
2007961

```
def pseudoCode(inp, counter=0):
```

```
    if inp[0] > inp[1]:
```

```
        return 0
```

$$C_1 = O(1)$$

```
    if inp[len(inp)-1] > inp[len(inp)-2]:
```

```
        return len(inp)-1
```

$$C_2 = O(1)$$

```
    if inp[len(inp)//2-1] < inp[len(inp)//2] and inp[len(inp)//2] > inp[len(inp)//2+1]:
```

$$C_3 = O(1)$$

```
        return len(inp)//2 + counter
```

```
    elif inp[len(inp)//2-1] < inp[len(inp)//2] and inp[len(inp)//2] < inp[len(inp)//2+1]:
```

$$C_4 = O(1)$$

```
        first_length = len(inp)
```

$$+ O(1)$$

```
        inp = inp[first_length//2 : first_length]
```

$$+ O(n)$$

```
        counter += first_length - len(inp)
```

$$+ O(1)$$

```
        return pseudoCode(inp, counter)
```

```
    elif inp[len(inp)//2-1] > inp[len(inp)//2] and inp[len(inp)//2] > inp[len(inp)//2+1]:
```

$$C_5 = O(1)$$

```
        first_length = len(inp)
```

$$+ O(1)$$

```
        inp = inp[0 : first_length//2]
```

$$+ O(n)$$

```
        return pseudoCode(inp, 0)
```

$$+ O(1)$$

Note that time complexity for slicing is  $O(n)$

Slicing is `inp = inp[start, end]`. In order to remove all entries that are increasing or decreasing, this syntax was used.

## Time Complexity

### Best Case Analysis

$C_1$  and  $C_2$  are time complexity for corner cases. In both cases, (increasing or decreasing order) time complexity is  $O(1)$ .  $C_3$  is best case since the peak is at the mid of input array. Time complexity is  $O(1)$ .

## Worst Case Analysis

Assume that `pseudoCode(array)` has size of  $n$ . When the array is strictly increasing or decreasing, the recursive function `pseudoCode(array)` would be implemented  $\log_2 n$  times. To calculate time complexity for the problem size of  $n$ :

$$O(\log_2 n) \cdot O(n) = O(n \log_2 n) \text{ since } O \text{ is multiplicative.}$$

To show  $O(n \log_2 n)$ :

$$\begin{aligned} T(n) &= c_4 + T(n/2) \\ &= 2c_4 + T(n/4) \\ &= 3c_4 + T(n/8) \\ &\vdots \\ &= i \cdot c_4 + T(n/2^i) \\ &= (\log_2 n)n + T(1) \\ &= (\log_2 n)n \end{aligned}$$

assuming the peak is picked at  $i^{\text{th}}$  recursive step, we have  $i = \log_2 n$  and  $c_4 = O(n)$

$$\Rightarrow T(n) = (\log_2 n) \cdot n$$

$$\Rightarrow \text{Time complexity is } \boxed{O(n \log n)}$$