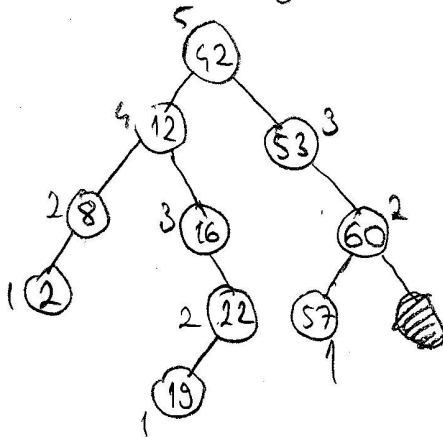


1. Binary Search Trees

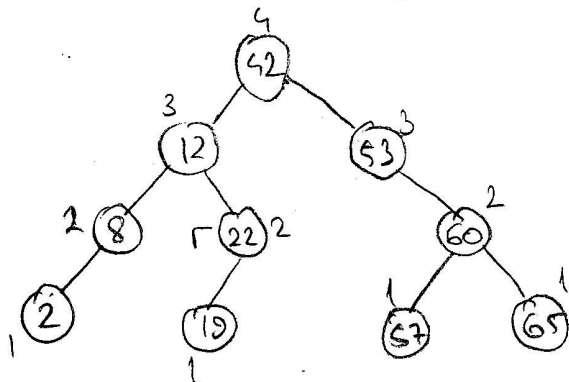
Task-1

- After removing 65 from the tree



Since 65 is leaf node, do nothing.

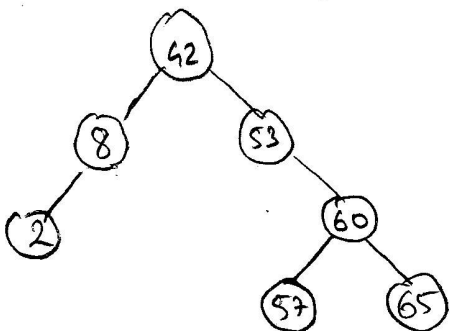
- After removing node 16 from the original tree



Since 16 has one child $r=22$, this is simple case, 22 would be right child of 12.

The tree is balanced, so rotation is not needed.

- After removing node 12 from the original tree

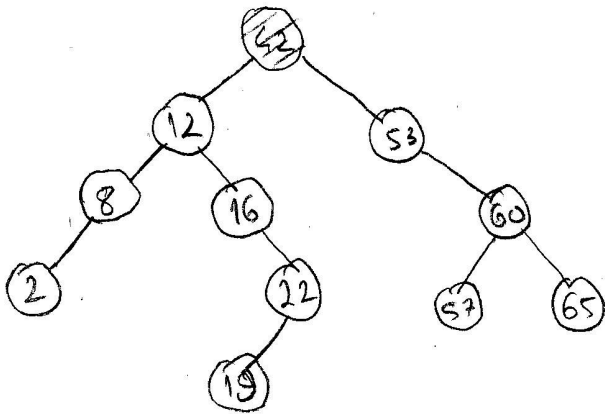


$r = \text{before}(p)$, where $p = 12$

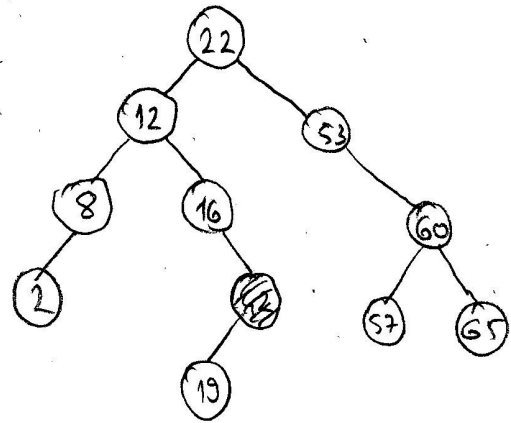
Since 12 has two child, it should be replaced by $r=8$. Then the state would be simple case.

The tree is balanced now.

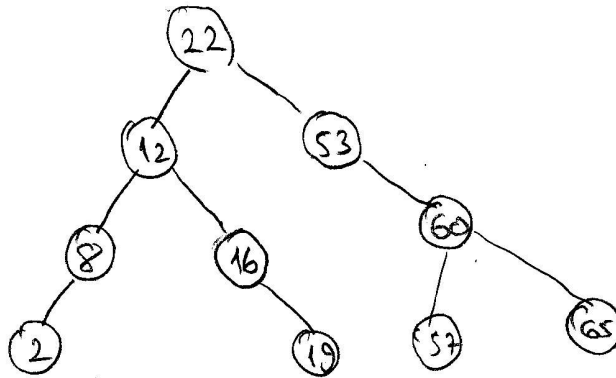
- After removing node 42 from the original tree



before(42) = 22
 →
 replace 22
 with 22



delete 42
 →
 simple case



Task-2

Pseudo code for the before()

before(p):

if left+(p) is not None then

walk = left+(p)

while righth(walk) is not None do

walk = righth(walk)

return walk

else

walk = p

child = child(walk)

while child is not None and walk == left+(child) do

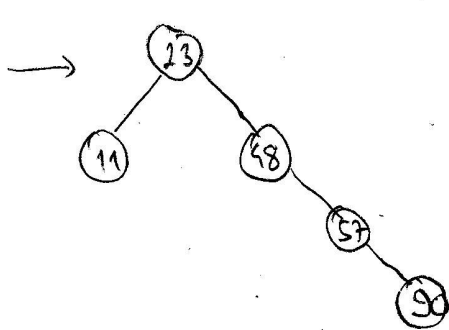
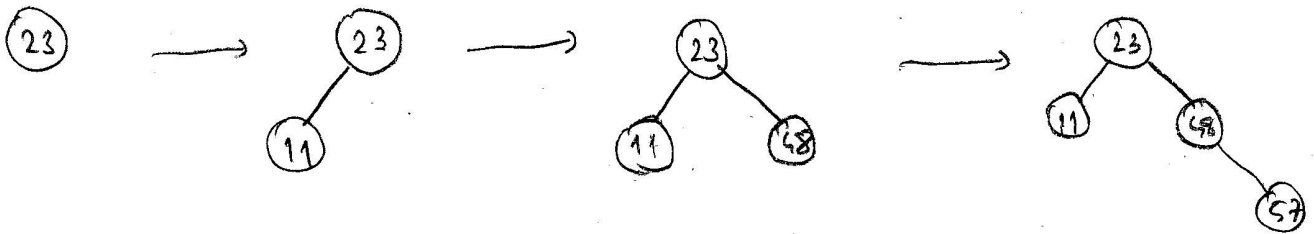
walk = child

child = child(walk)

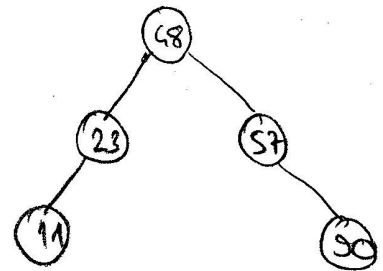
return child

2. AVL Trees

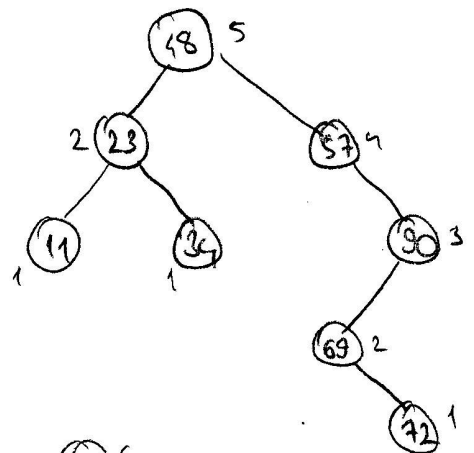
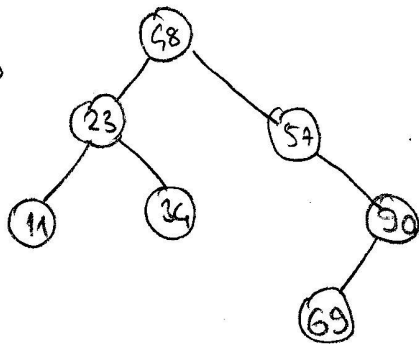
Task-3:



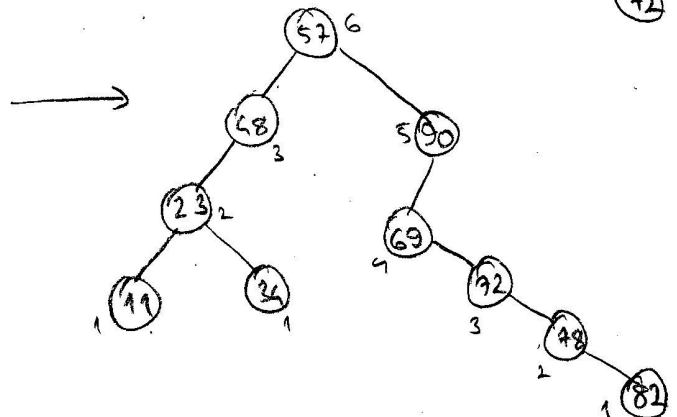
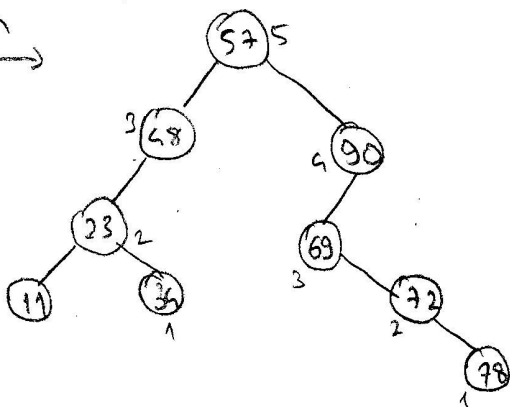
Unbalanced,
rotation is needed
Case 4,
single rotation
between 23 and 48



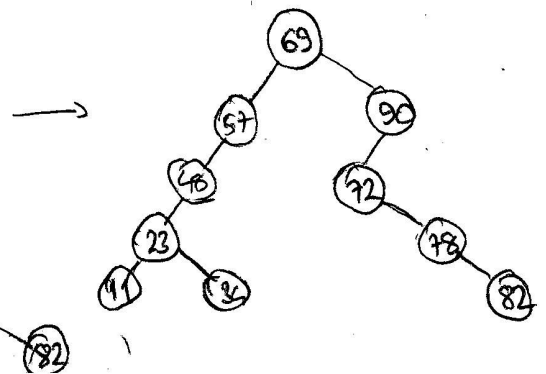
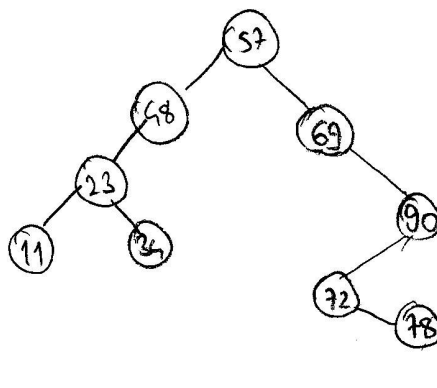
after 34 and 69



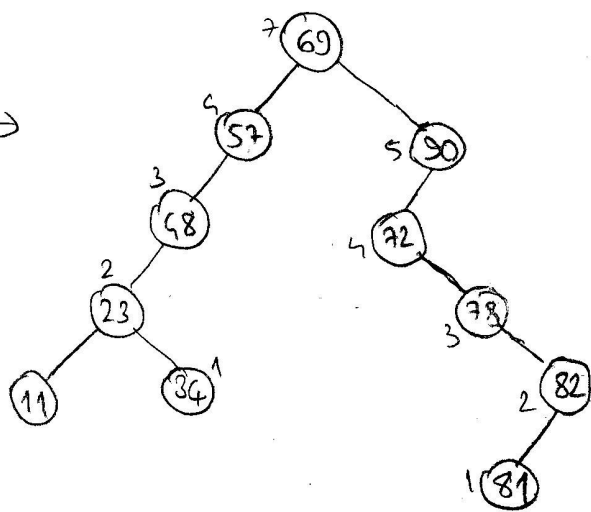
rotation
case 4
and
insert
78



rotation
case 3,
double rotation
between 90 and 69
firstly, then between
57 and 69



insert
81



Task-4

Delete 69 from the tree above: note: before(69) = 57
after replacing 69 with 57, delete operation is applied.

