ASSIGNMENT-2

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1 QUESTION NO-2.14 (LINEAR FORMS)

Find the equation of the line satisfying the following conditions.

1) passing through the point $\begin{pmatrix} -4 \\ 3 \end{pmatrix}$ and with slope $\frac{1}{2}$.

2) passing through the point $\begin{pmatrix} 2 \\ 2\sqrt{3} \end{pmatrix}$ and inclined with the x-axis at an angle of $75°$.

2 SOLUTION

1) Given point $\mathbf{P} = \begin{pmatrix} -4 \\ 3 \end{pmatrix}$ and slope $m = \frac{1}{2}$. The direction vector is $\mathbf{m} = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$. Hence, the normal vector

$$\mathbf{n} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}\mathbf{m} \tag{2.0.1}$$

$$= \begin{pmatrix} -1 \\ 2 \end{pmatrix} \tag{2.0.2}$$

The equation of the line in terms of the normal vector is then obtained as

$$\mathbf{n}^T (\mathbf{x} - \mathbf{A}) = 0 \tag{2.0.3}$$

$$\implies \begin{pmatrix} -1 & 2 \end{pmatrix}\mathbf{x} = 10 \tag{2.0.4}$$
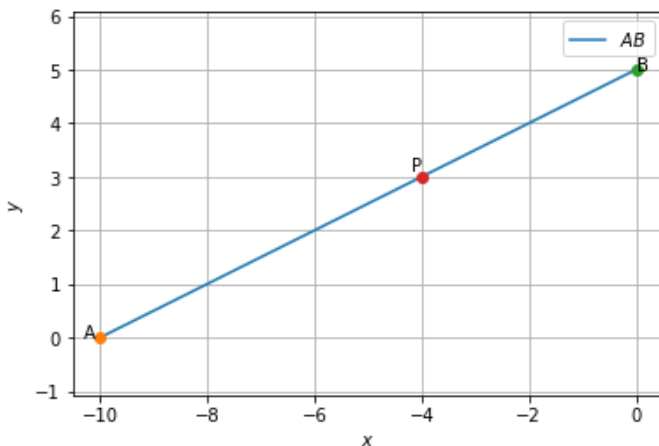
Plot of the line AB

Fig. 2.1: Plot of Line AB (Part-1)

2) Given point $\mathbf{P} = \begin{pmatrix} 2 \\ 2\sqrt{3} \end{pmatrix}$. From the given information, $\tan 75° = m = \frac{\sqrt{3}+1}{\sqrt{3}-1}$. The direction vector is $\mathbf{m} = \begin{pmatrix} 1 \\ \tan 75° \end{pmatrix}$. Hence, the normal vector

$$\mathbf{n} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}\mathbf{m} \tag{2.0.5}$$

$$= \begin{pmatrix} -\tan 75° \\ 1 \end{pmatrix} \tag{2.0.6}$$

The equation of the line in terms of the normal vector is then obtained as

$$\mathbf{n}^T (\mathbf{x} - \mathbf{A}) = 0 \tag{2.0.7}$$

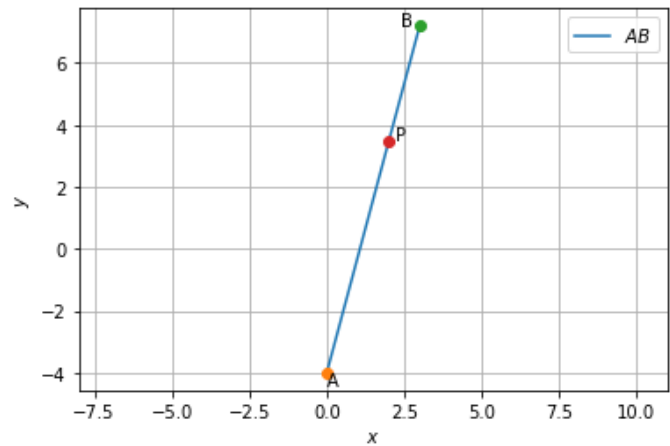$$\implies \begin{pmatrix} -\sqrt{3}+1 & \sqrt{3}-1 \end{pmatrix}\mathbf{x} = -4\left(\sqrt{3}-1\right) \tag{2.0.8}$$

Plot of the line AB

Fig. 2.2: Plot of Line AB (Part-2)