

ASSIGNMENT-9

R.YAMINI

1 QUESTION No-2.2(VECTORS)

Let $\mathbf{A} = \begin{pmatrix} 4 \\ 2 \end{pmatrix}$, $\mathbf{B} = \begin{pmatrix} 6 \\ 5 \end{pmatrix}$ and $\mathbf{C} = \begin{pmatrix} 1 \\ 4 \end{pmatrix}$ be the vertices of $\triangle ABC$.

- The median from \mathbf{A} meets BC at \mathbf{D} . Find the coordinates of the point \mathbf{D} .
- Find the coordinates of the point \mathbf{P} on AD such that $AP : PD = 2 : 1$.
- Find the coordinates of the points \mathbf{Q} and \mathbf{R} on medians BE and CF respectively such that $BQ : QE = 2 : 1$ and $CR : RF = 2 : 1$.

2 SOLUTION

- Given $\triangle ABC$ with vertices

$$\mathbf{A} = \begin{pmatrix} 4 \\ 2 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 6 \\ 5 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 1 \\ 4 \end{pmatrix} \quad (2.0.1)$$

Given that the median from \mathbf{A} meets BC at \mathbf{D} , now the coordinate of \mathbf{D} is given as,

$$\mathbf{D} = \frac{\mathbf{B} + \mathbf{C}}{2} = \frac{\begin{pmatrix} 6 \\ 5 \end{pmatrix} + \begin{pmatrix} 1 \\ 4 \end{pmatrix}}{2} \quad (2.0.2)$$

$$\Rightarrow \mathbf{D} = \begin{pmatrix} \frac{7}{2} \\ \frac{9}{2} \end{pmatrix} \quad (2.0.3)$$

- Result :The coordinates of point \mathbf{C} dividing the line AB in the ratio $m : n$ is given by

$$\frac{n\mathbf{A} + m\mathbf{B}}{m + n} \quad (2.0.4)$$

Given that the point \mathbf{P} divides AD in the ratio $2 : 1$, now to find \mathbf{P} we use (2.0.4),

$$\mathbf{P} = \frac{1 \begin{pmatrix} 4 \\ 2 \end{pmatrix} + 2 \begin{pmatrix} \frac{7}{2} \\ \frac{9}{2} \end{pmatrix}}{3} = \begin{pmatrix} \frac{11}{3} \\ \frac{11}{3} \end{pmatrix} \quad (2.0.5)$$

- Given that the point \mathbf{Q} on the median BE divides

it in the ratio $2 : 1$, first we find \mathbf{E} ,

$$\mathbf{E} = \frac{\mathbf{A} + \mathbf{C}}{2} = \frac{\begin{pmatrix} 4 \\ 2 \end{pmatrix} + \begin{pmatrix} 1 \\ 4 \end{pmatrix}}{2} \quad (2.0.6)$$

$$\Rightarrow \mathbf{E} = \begin{pmatrix} \frac{5}{2} \\ \frac{3}{2} \end{pmatrix}. \quad (2.0.7)$$

Now we find \mathbf{Q} using (2.0.4)

$$\mathbf{Q} = \frac{1 \begin{pmatrix} 6 \\ 5 \end{pmatrix} + 2 \begin{pmatrix} \frac{5}{2} \\ \frac{3}{2} \end{pmatrix}}{3} = \begin{pmatrix} \frac{11}{3} \\ \frac{11}{3} \end{pmatrix} \quad (2.0.8)$$

Similarly, Given that the point \mathbf{R} on the median CF divides it in the ratio $2 : 1$, first we find \mathbf{F} ,

$$\mathbf{F} = \frac{\mathbf{A} + \mathbf{B}}{2} = \frac{\begin{pmatrix} 4 \\ 2 \end{pmatrix} + \begin{pmatrix} 6 \\ 5 \end{pmatrix}}{2} \quad (2.0.9)$$

$$\Rightarrow \mathbf{F} = \begin{pmatrix} \frac{5}{2} \\ \frac{7}{2} \end{pmatrix}. \quad (2.0.10)$$

Now we find \mathbf{R} using (2.0.4)

$$\mathbf{R} = \frac{1 \begin{pmatrix} 1 \\ 4 \end{pmatrix} + 2 \begin{pmatrix} \frac{5}{2} \\ \frac{7}{2} \end{pmatrix}}{3} = \begin{pmatrix} \frac{11}{3} \\ \frac{11}{3} \end{pmatrix} \quad (2.0.11)$$

The plot of the $\triangle ABC$ is given below

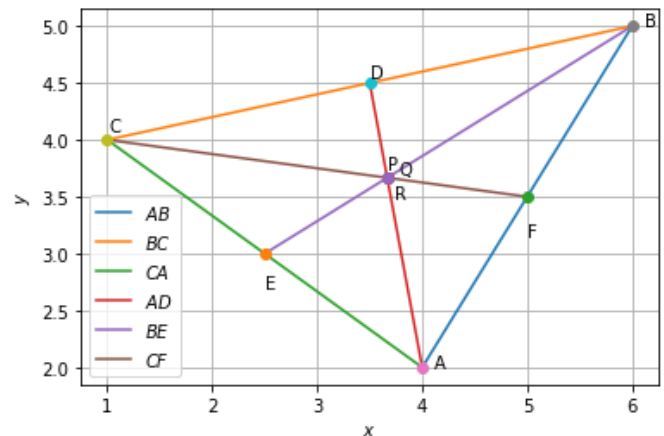


Fig. 2.1: Plot of $\triangle ABC$