

XRAY Loss 4 Nov 2020

$$L_{\text{Cross-Entropy}}(f(\vec{x}), \vec{y}) = \beta_p \sum_{y_c=1} -\ln(f(x_c)) + \beta_n \sum_{y_c=0} -\ln(1 - f(x_c))$$

$$\beta_p = \frac{|P|+N}{|P|} \quad \beta_n = \frac{|P|+N}{|N|} \quad \text{dans un Batch}$$

Tensor Flow $x = f(x)$ $z = \text{label}$

$$\begin{aligned}
 ① & z * -\log(f(x)) + (1-z) * -\log(1-f(x)) \\
 ② & z * -\log(1/(1+e^{-x})) + (1-z) * -\log(e^{-x}/(1+e^{-x})) \\
 ③ & z * ④ \log(1+e^{-x}) + (1-z) * -\log(e^{-x}) + \log(1+e^{-x}) \\
 ④ & z * \log(1+e^{-x}) + (1-z) * (x + \log(1+e^{-x})) \\
 ⑤ & (1-z)*x + \log(1+e^{-x}) \\
 ⑥ & x - xz + \log(1+e^{-x})
 \end{aligned}$$

$$x > 0 \quad ⑦ -x * z + \log(1+e^{-x})$$

$$⑧ \max(x, 0) - x * z + \log(1+e^{-\text{abs}(x)})$$

$$④ \rightarrow ⑤ \rightarrow C_1 z * A + (1-z)(x + A) \cdot C_2 \quad C_1 2A - C_2 2A + (1-z)x C_2$$

$$\frac{1}{1+e^{-x}} = \frac{e^x}{e^x + 1}$$

$$\log\left(\frac{e^x+1}{e^x}\right) = \log(e^x+1) - \log(e^x)$$

$$= \log(e^x+1) - x$$

$$1+e^{-x} = \frac{e^x+1}{e^x}$$

Avec correction pour l'inégalité:

$$4 \quad \beta_p(z * \log(1 + e^{-x})) + \beta_N[(1-z) * (x + \log(1 + e^{-x}))] \quad x > 0$$

$$\beta_p\left(z * \log\left(\frac{e^x + 1}{e^x}\right)\right) + \beta_N\left[(1-z) * \left(x + \log\left(\frac{e^x + 1}{e^x}\right)\right)\right]$$

$$\beta_p\left(z * \left(\log(e^x + 1) - x\right)\right) + \beta_N\left[(1-z) * \left(\log(e^x + 1)\right)\right]$$

$$\boxed{\beta_p\left(z * \left(\log(1 + e^{-|x|}) + \min(0, x)\right)\right) + \beta_N\left[(1-z) * \left(\max(0, x) + \log(e^{-x} + 1)\right)\right]}$$

②

fell - f slurm ... out

→ tensorboard

