

LATTIC homework hw11 yan liang 112889478

4/19/2018.

1.

$M=(3,7,19,43,89,195),$

Let me just run it once and the later one is similar as the first one, $S=260,$

$195 < 260$ so it is in, $260 - 195 = 65$ $89 > 65$ not in, $43 < 65$ in, so remaining will be 22,

Keep going, $19 < 22$, in, 3 remaining, 7 pass and 3 in ,

So the sequence will be (1,0,1,1,0,1)

Which means $3+19+43+195=260$ so it works for this one

$M=(5,11,25,61,125,261)$

The algorithms does not work, since there is no sequence that satisfy sum problem in this sequence.

$M=(2,5,12,28,60,131,257)$

$S=334$ similarly to preblem1 we will get

(0,1,1,0,1,0,1)

$5+12+60+257=334.$

$M=(4,12,15,36,75,162)$ $S=214$

The algorithms does not work since $4+12 > 15$ so it is not a super increasing sequence.

2.

public key is $M=(5186,2779,5955,2307,6599,6771,6296,7306,4115,637)$

$S=25916, A=4392 B=8387$

Find inverse(A) in sage

sage: $R=\text{Integers}(8387)$

sage: $\text{gcd}(8387,4392)$

1

sage: $R(4392)^{-1}$

2683

sage:

Then we can calculate r_i

The by multiply inverse(A) and then mod B

(5,14,30,75,160,351,750,1579,3253,6510)

Encrypted message $S=25916$ $S\text{-PRIME}=R(2683)*R(25916)=4398$

The we use the super increasing sequence $r(l)$ to solve the problem

(0,1,1,0,0,1,1,0,1,0)

So the message being send is the above sequence.

3.

(a) We need to find a matrix that solve this problem $A*B'=B$ since B and B' is $3*3$ so the A should be $3*3$

Since B is a basis, so all B should be invertible

So we just need $A=B*(B'^{-1})$

Putting in sage we get this:

[13/3 3 -11/3]

[-1 -1 4]

[1/3 0 4/3]

(b)

$|v|=3.74$

$|w|=4.58$

$v*w=-2+12+(-2)=8$

So $\cos(\theta)=8/(3.74*4.58)$. $\theta=62.16$ degrees.

6.7

sage: b=matrix([[1,3,-2],[2,1,0],[-1,2,5]])

sage: b.determinant

sage: b.determinant()

-35

So the volume should be 35, the volume can be calculated using the deterministic of the base.

