

Project 3 - Report (Phase 2)

Due Monday by 11pm **Points** 180 **Submitting** on paper **Available** after May 18 at 12am

CS 165 - Project 3

Algorithmic Experiments of Real-World Phenomena

(Phase 2)

180 points

For Phase 2 of Project 3, you will need to submit your report on the performance electronically to Gradescope.

Project 3 involves testing various graph algorithms experimentally to determine properties of models of real-world networks. The specific graph algorithms you should implement are the following three algorithms (please see the course notes for details on these algorithms):

1. **Diameter algorithm**, that is, as best is reasonably possible, determine the length of a longest path in the graph.
2. **Clustering-coefficient algorithm**, that is, determine the ratio of three times the number of triangles over the number of paths of length 2.
3. **Degree-distribution algorithm**, that is, determine for each possible degree, the number of vertices in the graph with that degree.

You need to test each algorithm on graphs of the following type (depending on your student ID):

- If your student ID is an odd number, you should test the above algorithms on Erdos-Renyi random graphs, $G(n,p)$, with $p = 2(\ln n)/n$, where " $\ln n$ " denotes the natural logarithm of n .
- If your student ID is an even number, you should test the above algorithms on Barabasi-Albert random graphs, generated with the parameter $d = 5$ as the number of neighbors each new vertex chooses.

You should determine the **diameter** and **clustering coefficients** of multiple random graphs of length n , and have n grow, and then plot the **average diameters and clustering coefficients**, respectively, as a function of n , on a **lin-log scale**. You should then **make a determination** as

to **whether** these values **grow, decrease, or remain constant** as a function of n . Also, **if they grow, determine if they grow proportional** to the function, $\log n$, **or** according to a function that grows **faster or slower** than the function, $\log n$.

For each number of vertices, $n=1,000$, $n=10,000$, and $n=100,000$, plot the **degree distribution** of an instance of your chosen type of random graph having that number of vertices. You should plot the degree-distribution results on **a regular (lin-lin) scale** and **a log-log scale**, and then **make a determination whether** that degree distribution **has a power law**. If you decide that the degree distribution **has** a power law, **find the slope** of a line fitting the data in the **log-log scale** and **report** on the **exponent of that power law**.

Write a report that shows your plots, includes your conclusions, explains how you implemented your algorithms (including pseudo-code for your versions), and any other observations that you would like to make.

There will be 10 points of extra credit available to students who implement and test both types of graph models, Erdos-Renyi and Barabasi-Albert, including **plots and **analysis** in their report for both types.**

Your report will be graded based on the following rubric:

- 90 points. Correct English grammar and spelling
- 30 points. Plotting the degree distributions and determining if they follow a power law.
- 30 points. Plotting the clustering coefficients and determining if they are changing as a function of n .
- 30 points. Plotting the diameters and determining if they are changing as a function of n .
- 10 points extra credit. Report on **performance** for both Erdos-Renyi and Barabasi-Albert graph models.

Turn in your written report as a PDF file via **GradeScope**.