

Exercise 3

Advanced Methods in Medical Image Analysis, Julia Wolleb

Deadline: 18.03.2024

Exercise 3: Gradient-based Optimization in 2D

Implement the **vanilla gradient-descent algorithm** to optimize the *Peaks* function

$$f(x, y) = 3 * (1 - x)^2 e^{-x^2 - (y+1)^2} - 10 * \left(\frac{x}{5} - x^3 - y^5\right) e^{-x^2 - y^2} - \frac{1}{3} e^{-(x+1)^2 - y^2} \quad (1)$$

- Calculate analytic gradients $\frac{\partial f}{\partial x}$, $\frac{\partial f}{\partial y}$ in your update procedure. You may use *Wolfram Alpha* or similar.
- Run your implemented optimizer several times **with different step-sizes** $\gamma_0 = 0.1$, $\gamma_1 = 0.01$, $\gamma_2 = 0.001$ and $\gamma_3 = 0.0001$ at the **initial position**: $x = 1, y = 0.5$.
- Report the **performance** of your optimizer in form of **convergence plots** (e.g. using `matplotlib.pyplot.plot`). The x-axis shows the number of steps, the y-axis shows the value of the *Peaks* function $f(x, y)$ at the current step.
- Hand in your code, which does not throw exceptions.

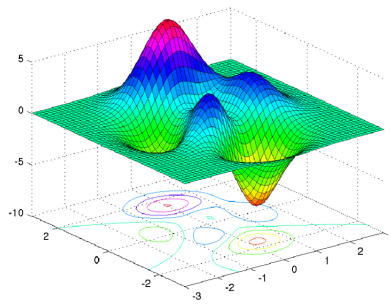


Figure 1: The Matlab *Peaks* function