

Routing Protocols

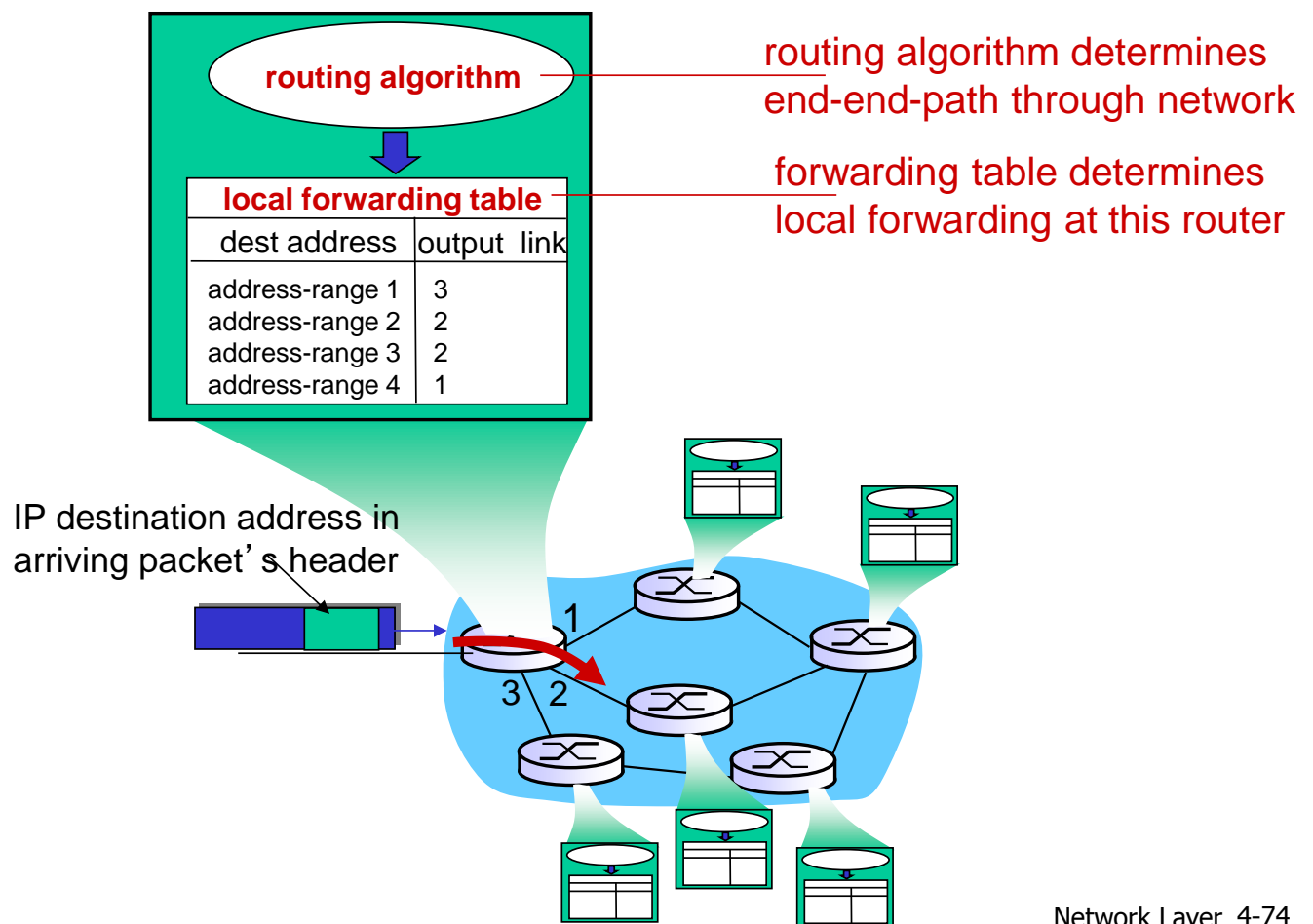
- How is routing/forwarding table established?
- Unfortunately, your textbook has nothing on this.
- Therefore, I resort to 4.5-4.7 of:

Computer networking : a top-down approach, 6th ed., Kurose and Ross

- On 3-hour reserve at DC Library
- You may find the slides to be detailed enough.

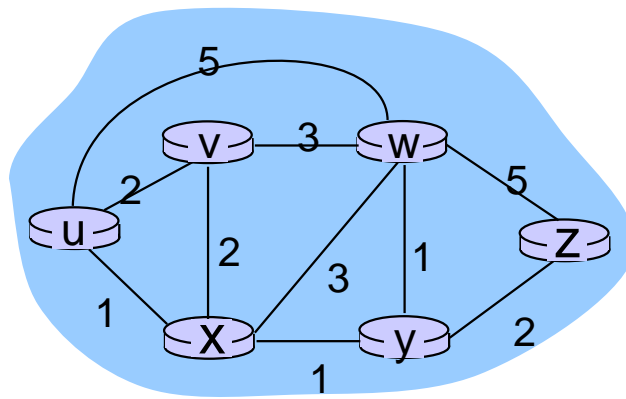
Often manual configuration of routes is not practical (they can be super complicated and dynamic). Thus we get routing protocols. There is nothing in the current textbook for this so you need to look at the older textbook.

Interplay between routing, forwarding



The whole point of a routing protocol is to figure out what the forwarding table should look like. Basically where the packets should go next.

Graph abstraction



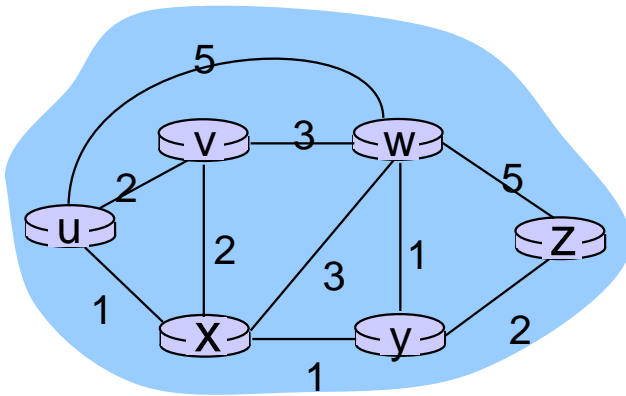
graph: $G = (N, E)$

N = set of routers = $\{ u, v, w, x, y, z \}$

E = set of links = $\{ (u,v), (u,x), (v,x), (v,w), (x,w), (x,y), (w,y), (w,z), (y,z) \}$

aside: graph abstraction is useful in other network contexts, e.g., P2P, where N is set of peers and E is set of TCP connections

Graph abstraction: costs



$c(x, x') = \text{cost of link } (x, x')$

e.g., $c(w, z) = 5$

cost could always be 1, or
inversely related to bandwidth,
or inversely related to
congestion

cost of path $(x_1, x_2, x_3, \dots, x_p) = c(x_1, x_2) + c(x_2, x_3) + \dots + c(x_{p-1}, x_p)$

key question: what is the least-cost path between u and z ?

routing algorithm: algorithm that finds that least cost path

We abstract this out to a graph. We have nodes and weighted edges (often the nodes are routers or devices). Often the cost is multidimensional which can make things complicated. We want to try to find the cheapest path through this graph.

Routing algorithm classification

Q: global or decentralized information?

global:

- ❖ all routers have complete topology, link cost info
- ❖ “link state” algorithms

decentralized:

- ❖ router knows physically-connected neighbors, link costs to neighbors
- ❖ iterative process of computation, exchange of info with neighbors
- ❖ “distance vector” algorithms

Q: static or dynamic?

static:

- ❖ routes change slowly over time

dynamic:

- ❖ routes change more quickly
 - periodic update
 - in response to link cost changes

A Link-State Routing Algorithm

Dijkstra's algorithm

- ❖ net topology, link costs known to all nodes
 - accomplished via “link state broadcast”
 - all nodes have same info
- ❖ computes least cost paths from one node (‘source’) to all other nodes
 - gives *forwarding table* for that node
- ❖ iterative: after k iterations, know least cost path to k dest.’s

notation:

- ❖ $c(x,y)$: link cost from node x to y; $= \infty$ if not direct neighbors
- ❖ $D(v)$: current value of cost of path from source to dest. v
- ❖ $p(v)$: predecessor node along path from source to v
- ❖ N' : set of nodes whose least cost path definitively known

Dijkstra's Algorithm

1 **Initialization:**

2 $N' = \{u\}$

3 for all nodes v

4 if v adjacent to u

5 then $D(v) = c(u,v)$

6 else $D(v) = \infty$

7

8 **Loop**

9 find w not in N' such that $D(w)$ is a minimum

10 add w to N'

11 update $D(v)$ for all v adjacent to w and not in N' :

12 **$D(v) = \min(D(v), D(w) + c(w,v))$**

13 /* new cost to v is either old cost to v or known

14 shortest path cost to w plus cost from w to v */

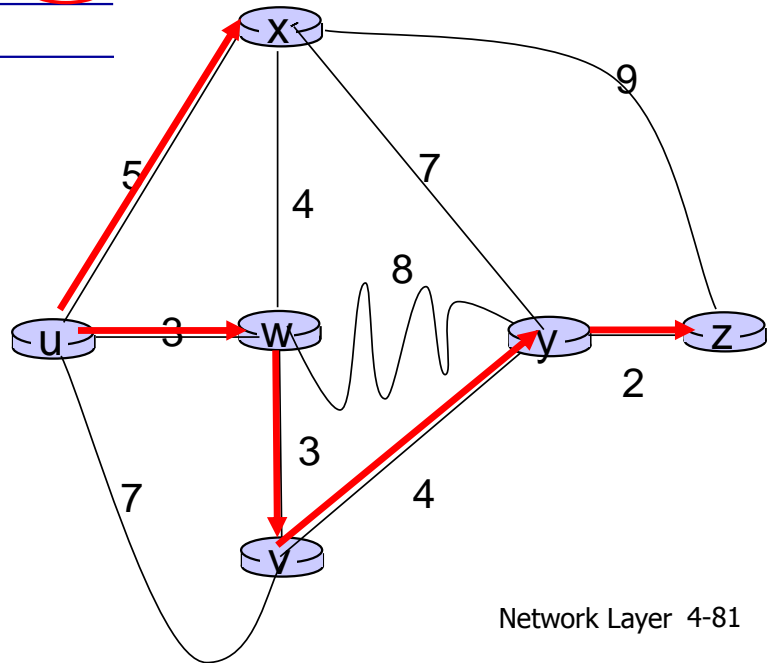
15 **until all nodes in N'**

Dijkstra's algorithm: example

Step	N'	D(v) p(v)	D(w) p(w)	D(x) p(x)	D(y) p(y)	D(z) p(z)
0	u	7,u	3,u	5,u	∞	∞
1	uw	6,w		5,u	11,w	∞
2	uwx	6,w			11,w	14,x
3	uwxv				10,v	14,x
4	uwxvy					12,y
5	uwxvyz					

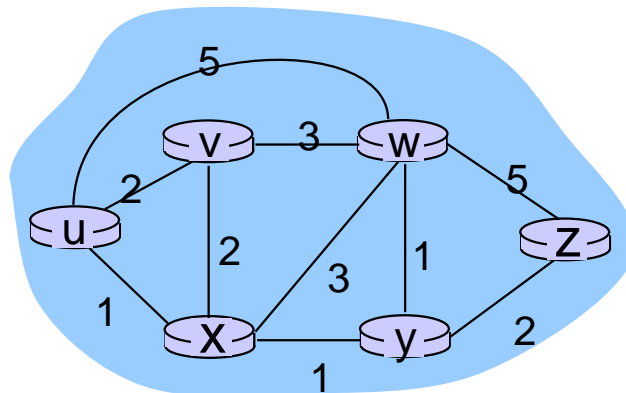
notes:

- ❖ construct shortest path tree by tracing predecessor nodes
- ❖ ties can exist (can be broken arbitrarily)



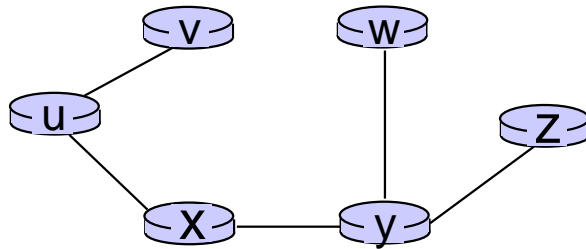
Dijkstra's algorithm: another example

Step	N'	D(v),p(v)	D(w),p(w)	D(x),p(x)	D(y),p(y)	D(z),p(z)
0	u	2,u	5,u	1,u	∞	∞
1	ux	2,u	4,x		2,x	∞
2	uxy	2,u	3,y			4,y
3	uxyv		3,y			4,y
4	uxyvw					4,y
5	uxyvwz					



Dijkstra's algorithm: example (2)

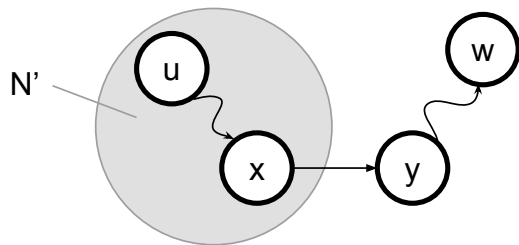
resulting shortest-path tree from u:



resulting forwarding table in u:

destination	link
v	(u,v)
x	(u,x)
y	(u,x)
w	(u,x)
z	(u,x)

Dijkstra's - correctness (Cormen et al.)



- Let $\delta(a)$ denote shortest distance from u to a
- Let w be first vertex added in loop such that:
 $D(w) > \delta(w)$
- A shortest path from u to w can be decomposed into $u \rightsquigarrow x \rightarrow y \rightsquigarrow w$, where $u, x \in N'$ and $y, w \notin N'$

- Because $u \rightsquigarrow w$ is a shortest path, so is $u \rightsquigarrow y$. Therefore, just before we choose w in the loop, $D(y) = \delta(y)$. And $\delta(y) = D(y) \leq \delta(w) < D(w)$.
- But we chose w over y in the loop. So, $\delta(w) < D(w) \leq D(y) = \delta(y)$.
- Contradiction. Therefore, $\delta(w) = D(w) = D(y) = \delta(y)$.

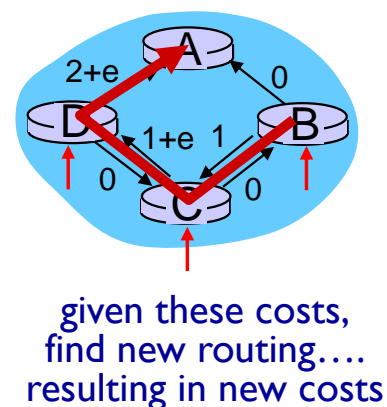
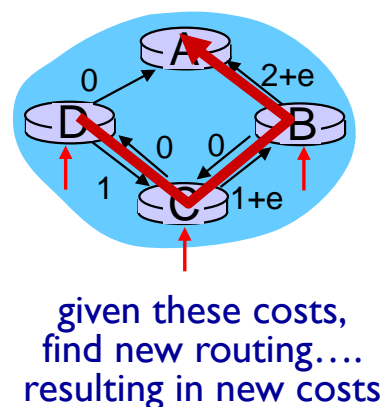
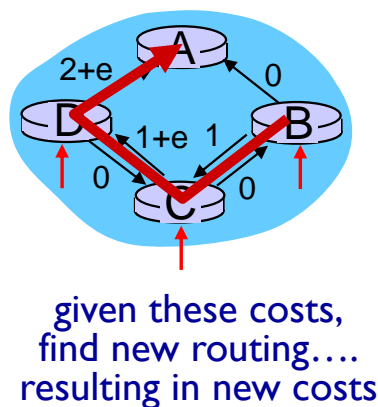
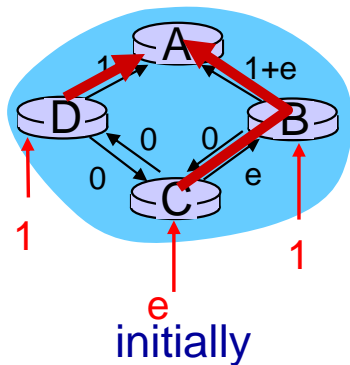
Dijkstra's algorithm, discussion

algorithm complexity: n nodes

- ❖ each iteration: need to check all nodes, w , not in N
- ❖ $n(n+1)/2$ comparisons: $O(n^2)$
- ❖ more efficient implementations possible: $O(n \log n)$

oscillations possible:

- ❖ e.g., support link cost equals amount of carried traffic:



Chapter 4: outline

4.1 introduction

4.2 virtual circuit and datagram networks

4.3 what's inside a router

4.4 IP: Internet Protocol

- datagram format
- IPv4 addressing
- ICMP
- IPv6

4.5 routing algorithms

- link state
- distance vector
- hierarchical routing

4.6 routing in the Internet

- RIP
- OSPF
- BGP

4.7 broadcast and multicast routing

Distance vector algorithm

Bellman-Ford equation (dynamic programming)

let

$d_x(y) :=$ cost of least-cost path from x to y

then

$$d_x(y) = \min_v \{ c(x,v) + d_v(y) \}$$

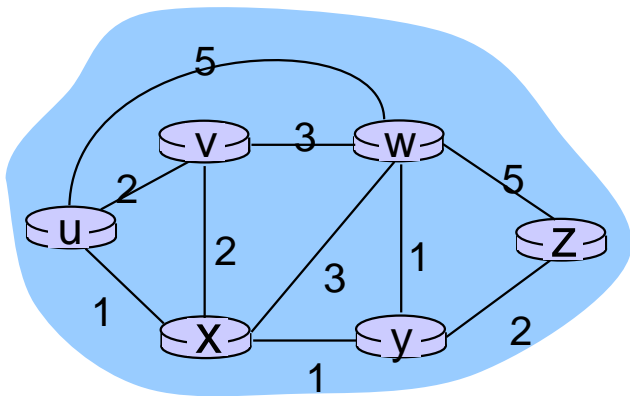
cost from neighbor v to destination y

cost to neighbor v

\min taken over all neighbors v of x

Dijkstra's algorithm shit.

Bellman-Ford example



clearly, $d_v(z) = 5$, $d_x(z) = 3$, $d_w(z) = 3$

B-F equation says:

$$\begin{aligned} d_u(z) &= \min \{ c(u,v) + d_v(z), \\ &\quad c(u,x) + d_x(z), \\ &\quad c(u,w) + d_w(z) \} \\ &= \min \{ 2 + 5, \\ &\quad 1 + 3, \\ &\quad 5 + 3 \} = 4 \end{aligned}$$

node achieving minimum is next
hop in shortest path, used in forwarding table

Distance vector algorithm

- ❖ $D_x(y)$ = estimate of least cost from x to y
 - x maintains distance vector $\mathbf{D}_x = [D_x(y): y \in N]$
- ❖ node x :
 - knows cost to each neighbor v : $c(x,v)$
 - maintains its neighbors' distance vectors. For each neighbor v , x maintains $\mathbf{D}_v = [D_v(y): y \in N]$

Distance vector algorithm

key idea:

- ❖ from time-to-time, each node sends its own distance vector estimate to neighbors
- ❖ when x receives new DV estimate from neighbor, it updates its own DV using B-F equation:

$$D_x(y) \leftarrow \min_v \{c(x,v) + D_v(y)\} \text{ for each node } y \in N$$

- ❖ under minor, natural conditions, the estimate $D_x(y)$ converge to the actual least cost $d_x(y)$

Distance vector algorithm

iterative, asynchronous:

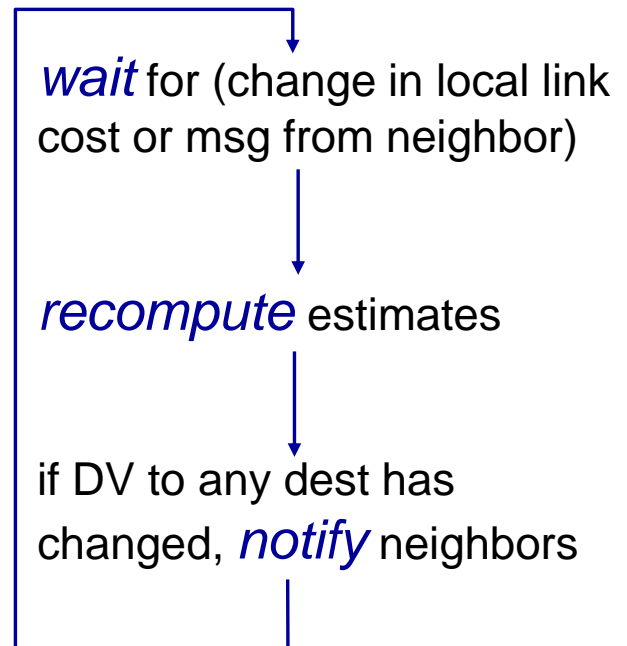
each local iteration
caused by:

- ❖ local link cost change
- ❖ DV update message from neighbor

distributed:

- ❖ each node notifies neighbors *only* when its DV changes
 - neighbors then notify their neighbors if necessary

each node:



$$D_x(y) = \min\{c(x,y) + D_y(y), c(x,z) + D_z(y)\} \\ = \min\{2+0, 7+1\} = 2$$

$$D_x(z) = \min\{c(x,y) + D_y(z), c(x,z) + D_z(z)\} \\ = \min\{2+1, 7+0\} = 3$$

**node x
table**

		cost to		
		x	y	z
from	x	0	2	7
	y	∞	∞	∞
	z	∞	∞	∞

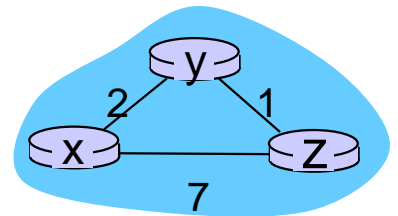
		cost to		
		x	y	z
from	x	0	2	3
	y	2	0	1
	z	7	1	0

**node y
table**

		cost to		
		x	y	z
from	x	∞	∞	∞
	y	2	0	1
	z	∞	∞	∞

**node z
table**

		cost to		
		x	y	z
from	x	∞	∞	∞
	y	∞	∞	∞
	z	7	1	0



time

$$D_x(y) = \min\{c(x,y) + D_y(y), c(x,z) + D_z(y)\} \\ = \min\{2+0, 7+1\} = 2$$

$$D_x(z) = \min\{c(x,y) + D_y(z), c(x,z) + D_z(z)\} \\ = \min\{2+1, 7+0\} = 3$$

node x
table

		cost to		
		x	y	z
from	x	0	2	7
	y	∞	∞	∞
	z	∞	∞	∞

node y
table

		cost to		
		x	y	z
from	x	∞	∞	∞
	y	2	0	1
	z	∞	∞	∞

node z
table

		cost to		
		x	y	z
from	x	∞	∞	∞
	y	∞	∞	∞
	z	7	1	0

		cost to		
		x	y	z
from	x	0	2	3
	y	2	0	1
	z	7	1	0

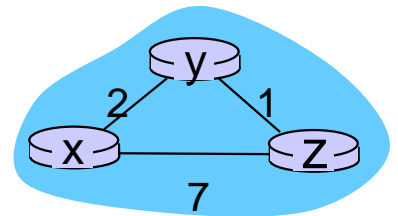
		cost to		
		x	y	z
from	x	0	2	7
	y	2	0	1
	z	7	1	0

		cost to		
		x	y	z
from	x	0	2	7
	y	2	0	1
	z	3	1	0

		cost to		
		x	y	z
from	x	0	2	3
	y	2	0	1
	z	3	1	0

		cost to		
		x	y	z
from	x	0	2	3
	y	2	0	1
	z	3	1	0

		cost to		
		x	y	z
from	x	0	2	3
	y	2	0	1
	z	3	1	0

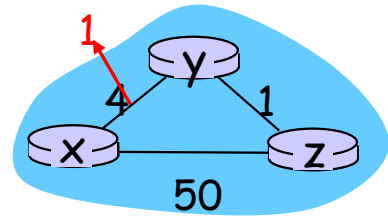


time

Distance vector: link cost changes

link cost changes:

- ❖ node detects local link cost change
- ❖ updates routing info, recalculates distance vector
- ❖ if DV changes, notify neighbors



“good
news
travels
fast”

t_0 : y detects link-cost change, updates its DV, informs its neighbors.

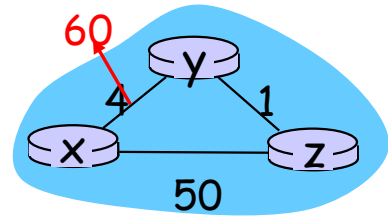
t_1 : z receives update from y , updates its table, computes new least cost to x , sends its neighbors its DV.

t_2 : y receives z 's update, updates its distance table. y 's least costs do *not* change, so y does *not* send a message to z .

Distance vector: link cost changes

link cost changes:

- ❖ node detects local link cost change
- ❖ *bad news travels slow* - “count to infinity” problem!
- ❖ 44 iterations before algorithm stabilizes: see text



poisoned reverse:

- ❖ If Z routes through Y to get to X :
 - Z tells Y its (Z's) distance to X is infinite (so Y won't route to X via Z)
- ❖ will this completely solve count to infinity problem?

We can keep track of distance vector tables that say the total cost of the path to another node and the next hop in the path. These values are calculated using djikstra's algorithm. You keep updating it by adding and taking mins as you go. Basically nodes keep each other in sync by sending their distance tables to each other and if a better path occurs updating to match it.

When the distance between two nodes updates shit gets a bit crazy. Basically the nodes that notices the change will update its table to reflect it. If the path is now shorter it moves very quickly sending it around. If the path increases it moves incredibly slowly. We can get loops because the tables don't all update at the same time so one table can think that one way is the optimal path while a table with fresher data knows that another path is optimal. This results in data moving around a ton.

Counting to infinity Say Y notices the update first. It sees that to get to X costs 60 so it looks for a faster route. Z says that it can get to X with a cost of 5 so Y wants to use Z. Once this is done Y broadcasts its change and Z decides to update. Then Z updates its self. It does the same logic where it sees that Y can reach X with a cost of six so it wants to go through there. Then Z broadcasts its change. This goes back and forth for a while until it gets its shit together.

poisoned reverse: with this Z advertises to Y that it has a cost of infinity to get anywhere. This makes Y go directly to X and broadcasts the update to Z. This puts an infinity to get to Z. Now Z has to update itself. It updates its routing table to now use the direct connects to X and Y (because these are the cheapest known paths). This is how we get around the counting to infinity problem. Poisoned reverse is not always sufficient. He gives a good example for this, see supplementary notes on it. There is going to be a question about this on the exam

Comparison of LS and DV algorithms

message complexity

- ❖ **LS:** with n nodes, E links, $O(nE)$ msgs sent
- ❖ **DV:** exchange between neighbors only
 - convergence time varies

speed of convergence

- ❖ **LS:** $O(n^2)$ algorithm requires $O(nE)$ msgs
 - may have oscillations
- ❖ **DV:** convergence time varies
 - may be routing loops
 - count-to-infinity problem

robustness: what happens if router malfunctions?

LS:

- node can advertise incorrect *link* cost
- each node computes only its own table

DV:

- DV node can advertise incorrect *path* cost
- each node's table used by others
 - error propagate thru network

LOOK THIS UP IN THE TEXTBOOK

Hierarchical routing

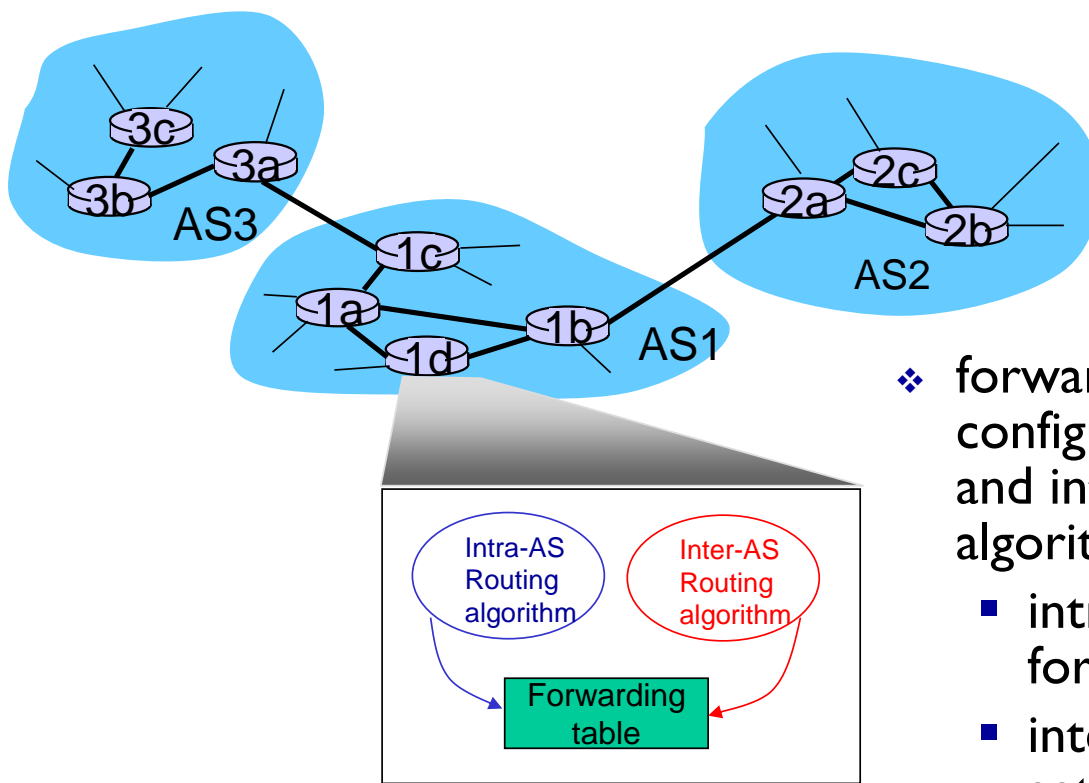
- ❖ aggregate routers into regions, “**autonomous systems**” (AS)
- ❖ routers in same AS run same routing protocol
 - “**intra-AS**” routing protocol
 - routers in different AS can run different intra-AS routing protocol

gateway router:

- ❖ at “edge” of its own AS
- ❖ has link to router in another AS

Every system figures out which routing protocol works for them so a gateway router is needed to talk between them. This allows us to categorize routers by the routing protocol that they follow.

Interconnected ASes



- ❖ forwarding table configured by both intra- and inter-AS routing algorithm
 - intra-AS sets entries for internal dests
 - inter-AS & intra-AS sets entries for external dests

There's an intra routing algorithm and inter and these could be different and are categorized by AS.

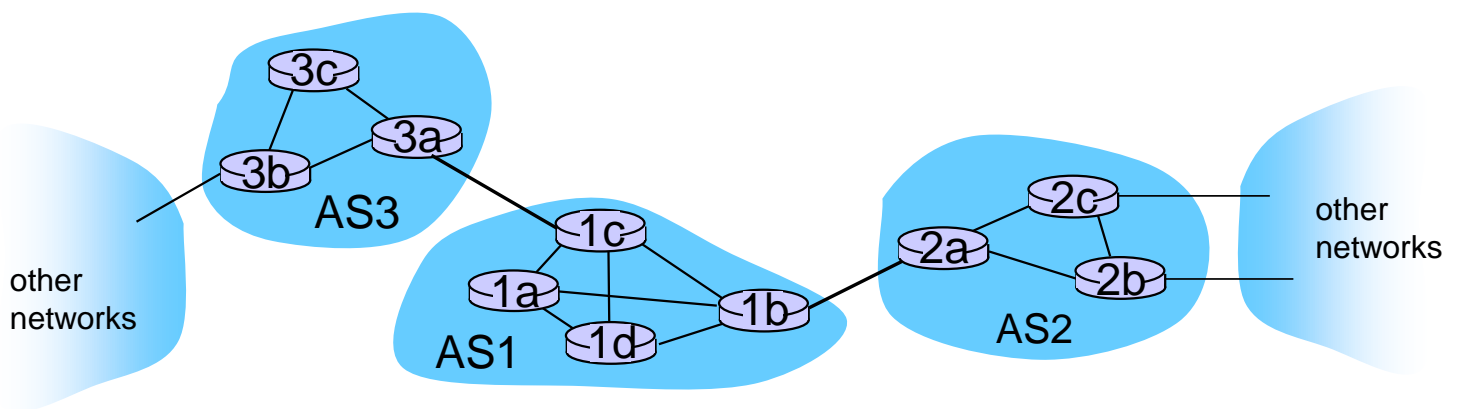
Inter-AS tasks

- ❖ suppose router in AS1 receives datagram destined outside of AS1:
 - router should forward packet to gateway router, but which one?

AS1 must:

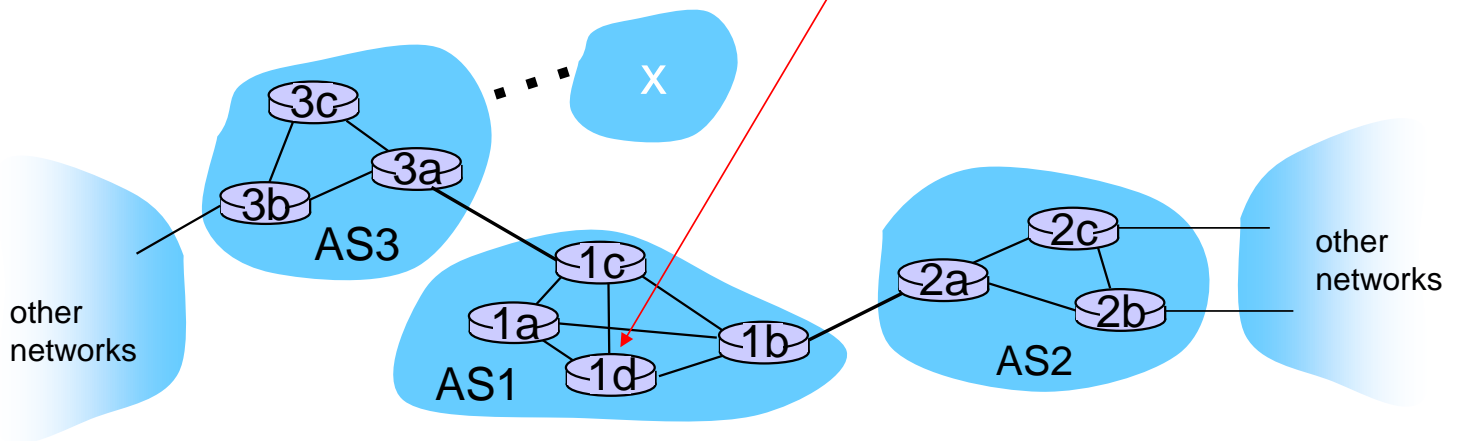
1. learn which destds are reachable through AS2, which through AS3
2. propagate this reachability info to all routers in AS1

job of inter-AS routing!



Example: setting forwarding table in router 1d

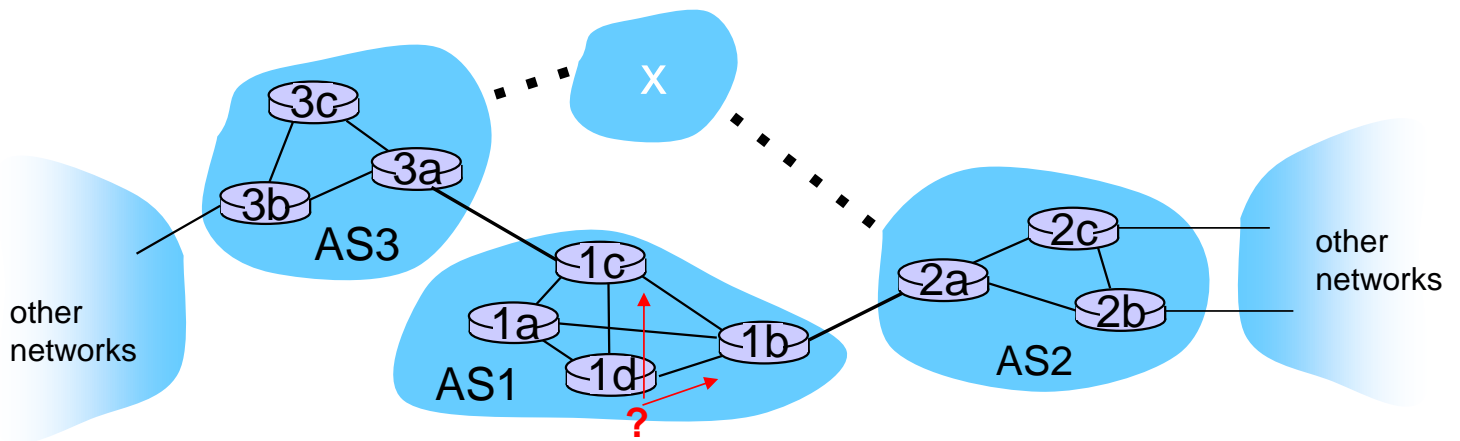
- ❖ suppose AS1 learns (via inter-AS protocol) that subnet **x** reachable via AS3 (gateway 1c), but not via AS2
 - inter-AS protocol propagates reachability info to all internal routers
- ❖ router 1d determines from intra-AS routing info that its interface **1** is on the least cost path to 1c
 - installs forwarding table entry **(x,1)**



Subnet X is reachable by AS3 and not AS2, then the interAS protocol propagates that information to all internal routers. We use intraAS to see that 1B's least cost to 1C is through some interface so it makes an entry for that.

Example: choosing among multiple ASes

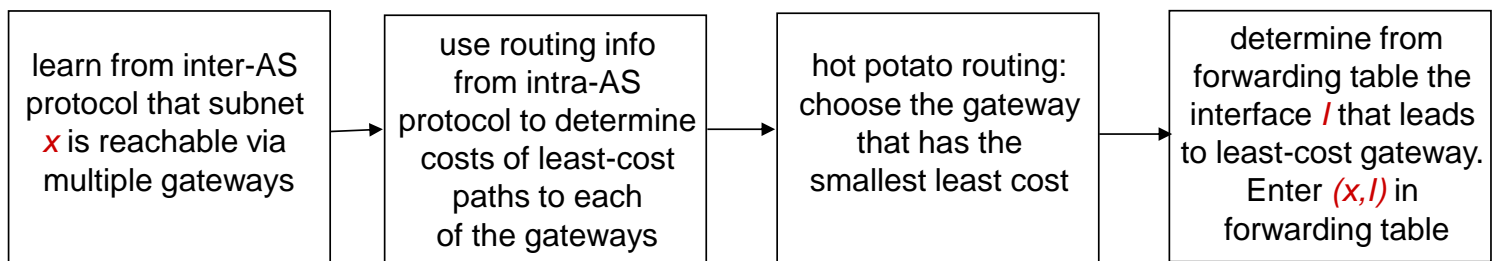
- ❖ now suppose AS1 learns from inter-AS protocol that subnet **x** is reachable from AS3 *and* from AS2.
- ❖ to configure forwarding table, router 1d must determine which gateway it should forward packets towards for dest **x**
 - this is also job of inter-AS routing protocol!



If we now know that X is reachable by AS1, we now have a choice for 1d to figure out the least cost path to get a packet through to X. This is much harder to figure out and done through interAS.

Example: choosing among multiple ASes

- ❖ now suppose AS1 learns from inter-AS protocol that subnet **x** is reachable from AS3 *and* from AS2.
- ❖ to configure forwarding table, router 1d must determine towards which gateway it should forward packets for dest **x**
 - this is also job of inter-AS routing protocol!
- ❖ *hot potato routing: send* packet towards closest of two routers.

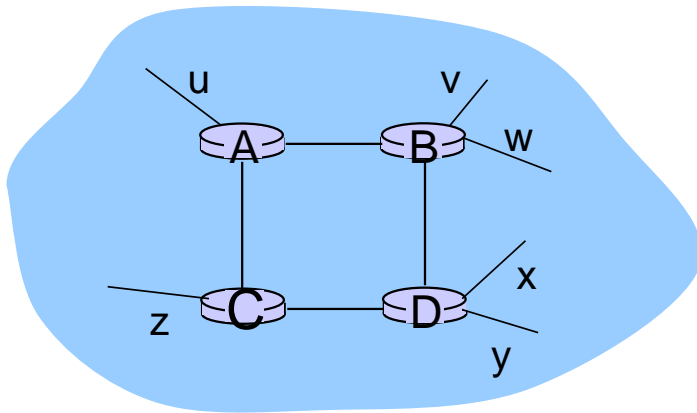


Intra-AS Routing

- ❖ also known as *interior gateway protocols (IGP)*
- ❖ most common intra-AS routing protocols:
 - RIP: Routing Information Protocol
 - OSPF: Open Shortest Path First
 - IGRP: Interior Gateway Routing Protocol (Cisco proprietary)

RIP (Routing Information Protocol)

- ❖ included in BSD-UNIX distribution in 1982
- ❖ distance vector algorithm
 - distance metric: # hops (max = 15 hops), each link has cost 1
 - DVs exchanged with neighbors every 30 sec in response message (aka **advertisement**)
 - each advertisement: list of up to 25 destination **subnets** (in IP addressing sense)

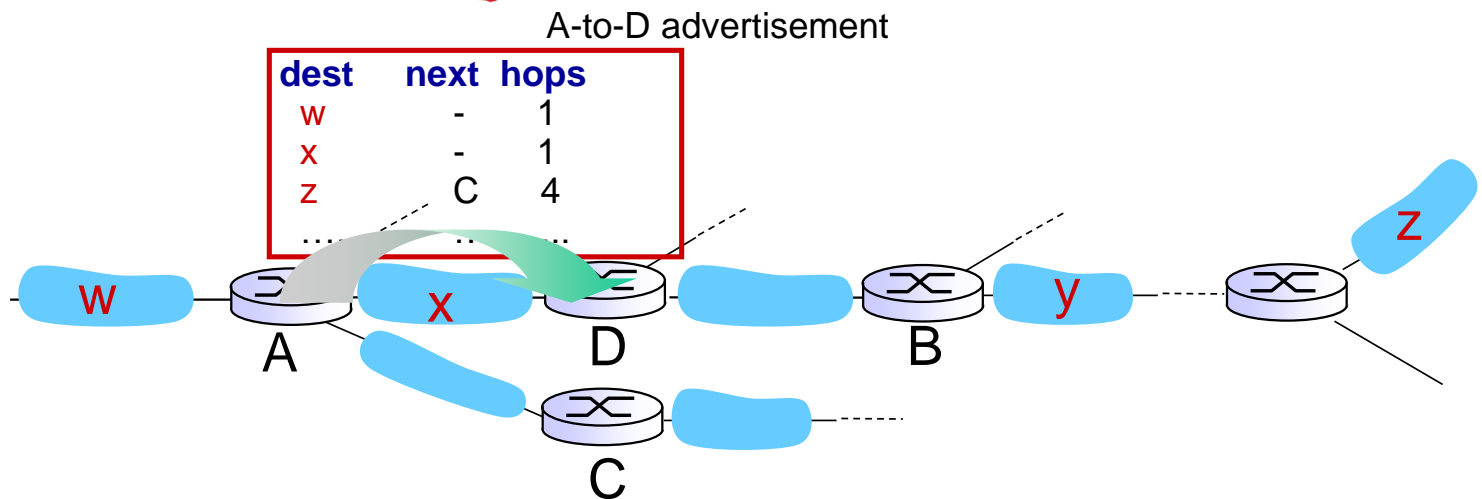


from router A to destination **subnets**:

<u>subnet</u>	<u>hops</u>
u	1
v	2
w	2
x	3
y	3
z	2

Interesting to note that we count a hop from an internal port to external (so the hop to u is one).

RIP: example



routing table in router D

destination subnet	next router	# hops to dest
W	A	2
y	B	2
Z	B A	7 5
X	--	1
....

In this example if we wanted to have the route from internal to external to be 0 we would have the distance from D to W to be equal to 0 which is clearly not true. This is why we make that cost equal to 1.

RIP: link failure, recovery

if no advertisement heard after 180 sec -->
neighbor/link declared dead

- routes via neighbor invalidated
- new advertisements sent to neighbors
- neighbors in turn send out new advertisements (if tables changed)
- link failure info quickly (?) propagates to entire net
- *poison reverse* used to prevent ping-pong loops (infinite distance = 16 hops)

If we haven't heard an advertisement in a while we will deem the node dead. Usually the time span is about 3 minutes.

RIP table processing

- ❖ RIP routing tables managed by *application-level* process called route-d (daemon)
- ❖ advertisements sent in UDP packets, periodically repeated

