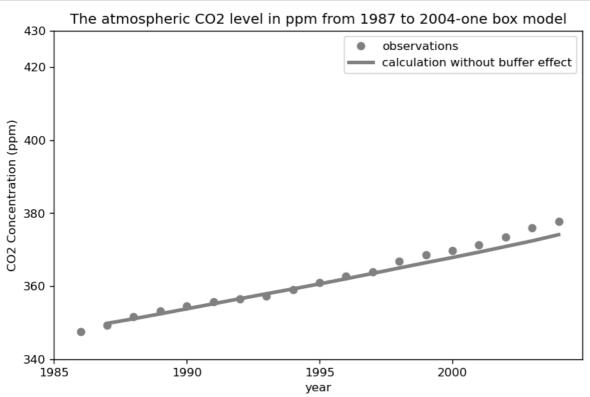
In [1]:

```
#import module
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from scipy import integrate
from scipy.integrate import solve_ivp
from scipy.optimize import curve_fit
from numpy import exp
import glob
%matplotlib inline
import warnings
warnings.filterwarnings('ignore')
```

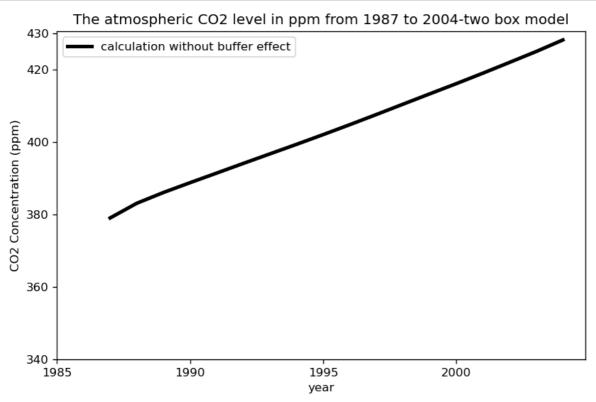
```
In [2]:
```

```
# 1.1
# read the file
df = pd. read csv("co2 annmean mlo. csv", skiprows = 55)
CO2=df.loc[ (df['year'] >1985)&(df['year'] <2005)][['year', 'mean']]
#define \gamma (This step is taught by Yin Yuling)
def \gamma (t):
    #get the fossil fuel data
    data = pd. read_csv("global. 1751_2008. csv")
    γ=float(data.loc[ (data['Year"'] ==int(t))]['Total carbon emissions from fossil-fuels (million metric tons of C)']/1000/2.13)
# Define the function
def model(f, t, k12, k21):
    N1, N2=f
    \mbox{dfdt} \ = \ \left[ -k12*N1+k21*N2+\gamma \ (\mbox{t}) \, , \, k12*N1-k21*N2 \right]
    return dfdt
# initial condition
k12, k21 = 105/740, 102/900
N10=740/2.13
N20=900/2.13
y0 = [N10, N20]
# Time points
t = np. linspace (1985, 2004, 20)
# Solve ODE
from scipy.integrate import odeint
sol = odeint(model, y0, t, args=(k12, k21))
plt.figure(figsize=(8,5),dpi=120)
plt.plot(CO2['year'], CO2['mean'],'o',c='grey',label='observations', markersize=6)
plt.plot(t[2:], sol[2:,0], c='grey',label='calculation without buffer effect', linewidth=3)
plt.xlabel('year')
plt.ylabel('CO2 Concentration (ppm)')
plt. xticks([1985, 1990, 1995, 2000])
plt.yticks([340, 360, 380, 400, 420, 430])
plt.legend(loc='best')
plt.title('The atmospheric CO2 level in ppm from 1987 to 2004-one box model')
plt.show()
```

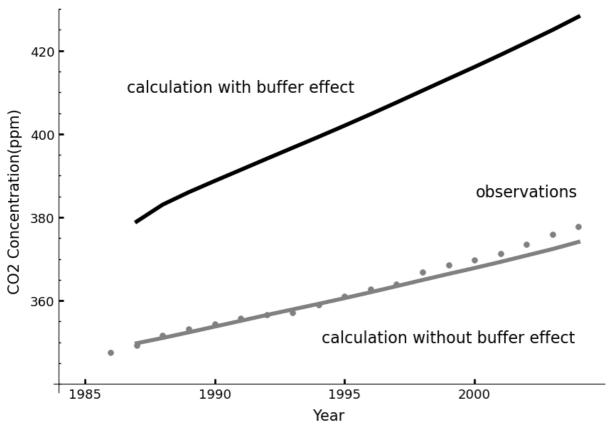


```
In [3]:
```

```
# 1.2
# read the file
data = pd. read csv("co2 annmean mlo. csv", skiprows = 55)
CO2=data.loc[ (data['year'] >1985)&(data['year'] <2005)][['year', 'mean']]
#define \gamma (the same as 1.1)
def \gamma (t):
    #get the fossil fuel data
    data2 = pd. read_csv("global. 1751_2008. csv")
    \gamma = \text{float}(\text{data2.loc}[(\text{data2}['\text{Year}^{\text{w}'}] = \text{int}(t))]['\text{Total carbon emissions from fossil-fuels (million metric tons of C)']/1000/2.13)}
#define a
def a(N1):
    a=3.69+1.86*(1e-2)*N1-1.8*(1e-6)*N1*N1
    return a
#define the function
def model2(f, t, k12, k21, N20):
    dfdt = [-k12*N1+k21*(N20+a(N1)*(N2-N20))+\gamma(t), k12*N1-k21*(N20+a(N1)*(N2-N20))]
    return dfdt
k12 = 105/740
k21 = 102/900
N20 = 821/2.13
f0 = [740/2.13, 900/2.13]
# Time points
t = np. linspace (1985, 2004, 20)
sol2 = integrate.odeint(model2, f0, t, args=(k12, k21, N20))
plt.figure(figsize=(8,5),dpi=120)
#plt.plot(CO2['year'], CO2['mean'],'o',c='grey', label='observations', markersize=6)
plt.plot(t[2:], sol2[2:,0],c='k', label='calculation without buffer effect', linewidth=3)
plt.xlabel('year')
plt.ylabel('CO2 Concentration (ppm)')
plt. xticks([1985, 1990, 1995, 2000])
plt. yticks([340, 360, 380, 400, 420, 430])
plt.legend(loc='best')
plt.title('The atmospheric CO2 level in ppm from 1987 to 2004-two box model')
plt.show()
```



```
#1.3
# combine the two figures
# set the figure size
fig = plt.figure(figsize=(10, 7))
ax = fig. add\_subplot(1, 1, 1)
#Set the scale and ticks of the coordinate axis
plt.xlim(1983.8,2005)
ax.tick_params(axis='x', which='major', direction='in', width=2, length=5, pad=4, labelsize=13)
ax.set_xticks(np.arange(1985, 2000 + 5, 5))
ax.set_xticks(np.arange(180, 180 + 2.5, 2.5), minor=True)
ax. set_xlabel('Year', labelpad=8, fontsize=15)
plt.ylim(338,430)
ax. tick_params(axis='y', which='major', direction='in', width=2, length=5, pad=4, labelsize=13)
ax. tick_params(axis='y', which='minor', direction='in', width=1, length=2)
ax.set_yticks(np.arange(360, 420 + 20, 20))
ax.set_yticks(np.arange(340, 430 + 5, 5), minor=True)
ax.set_ylabel('CO2 Concentration(ppm)', labelpad=8, fontsize=15)
#Set the origin of axes and plot it(ask for Yin Yuling)
ax.spines['bottom'].set_position(('data',340))
ax.spines['left'].set_position(('data', 1984))
ax.plot(t[2:], sol[2:,0], linewidth=4, color='grey', label='calculation without buffer effect') ax.plot(t[2:], sol2[2:,0], linewidth=4, color='k', label='calculation with buffer effect') ax.scatter(CO2['year'], CO2['mean'], s=32, c='grey', marker='o', lw=0.5, label='observations')
#Remove the right border and top border
ax.spines['right'].set_visible(False)
ax. spines['top']. set_visible(False)
#add the text
ax. text (1999, 350,
           "calculation without buffer effect",
          horizontalalignment = center',
          fontsize = 16, zorder=2)
ax. text (1991, 410,
           "calculation with buffer effect",
          horizontalalignment = center,
         fontsize = 16, zorder=2)
ax. text (2002, 385,
           "observations",
          horizontalalignment ='center',
          fontsize = 16, zorder=2)
plt.show()
```



```
In [ ]:
```

In [5]:

```
# Bonus
# this is taught by Shao Shi, I think the functions are correct, but somehow it seems that there are some problems.
# read γ file
gama = np. loadtxt("global.1751_2008.csv", delimiter=",", skiprows = 2, usecols = 1)/10**3
# create year vector
t = np.linspace(1751, 2008, 258, dtype='int')
# read CO2 observation data 1
co2_1010 = np.loadtxt("co2_1010.csv", delimiter=",", skiprows = 148)
# read CO2 observation data 2
annual_CO2_Obs = np.loadtxt("co2_annmean_mlo.csv", delimiter=",", skiprows = 56)[:,1]
annual_CO2_Obs_t = np.loadtxt("co2_annmean_mlo.csv", delimiter=",", skiprows = 56)[:,0]
# read the data of delta
delta = np.empty_like(gama)
delta[0:100] = np.linspace(0.2,0.5,100)
#delta[99:-3] = np.loadtxt("Global_land-use_flux-1850_2005.CSV", delimiter=",", skiprows = 1, usecols = 1)/10**3
delta[-3:] = delta[-4]
```

In [6]:

```
# define f
import math
def compute_f(P, β):
    f0=62/2.13
    P0=290.21
    f=f0*(1+β*math.log(P/P0))
    return f
```

In [7]:

```
def compute_a(CO2_ppm):
    a = 3.69 + 1.86 * 10**-2 * CO2_ppm - 1.80 * 10**-6 * CO2_ppm**2
    return a
```

In [8]:

```
# delta: emission rate to the atmosphere by changes in land use
def delta(t):
   data_delta = pd.read_csv("Global_land-use_flux-1850_2005.csv")
   delta=float(data_delta.loc[ (data_delta['Year'] ==int(t))]['Global']/1000/2.13)
   return delta
```

In [9]:

```
# define function
def model3(N, t, a, \gamma, f, delta):
    N1, N2, N3, N4, N5, N6, N7=N
    dfdt = [-k12*N1+k21*(N20+a(N1)*(N2-N20)) + \gamma(t) - f(P, \beta) + delta(t) + k51*N5+k71*N7,
            k12*N1-k21*(N20+a(N1)*(N2-N20))-k23*N2+k32*N3-k24*N2
            k23*N2-k32*N3-k34*N3+k43*N4,
           k34*N3-k43*N4+k24*N2-k45*N4,
           k45*N4-k51*N5,
           f(P, \beta)-k67*N6-2*delta(t),
           k67*N6-k71*N7+delta(t)
    return dNdt
k12 = 60/615
k21 = 60/842
k23 = 9/842
k24 = 43/842
k32 = 52/9744
k34 = 162/9744
k43 = 205/26280
k45 = 0.2/26280
k51 = 0.2/90000000
k67 = 62/731
k71 = 62/1328
N20 = 821/2.13
NO = [615/2.13, 842/2.13, 9744/2.13, 26280/2.13, 90000000/2.13, 731/2.13, 1238/2.13]
```

In [10]:

```
N1_eq_6_12_beta1 = np.empty_like(t)
N1_eq_6_12_beta2 = np.empty_like(t)
```

```
In [11]:
\# \beta = 0.38
\beta = 0.38
NO = [615, 842, 9744, 26280, 90000000, 731, 1238]
N1_eq_6_12_beta1[0] = NO[0]
C02_{ppm} = N1_{eq_6_{12_{beta1}[0]/2.13}
a = compute_a(CO2_ppm)
f = compute_f(CO2_ppm, β)
# slove the ODE year by year
for i in range (1, 258):
    #set the setp size
    dt = [0, 1]
    # numericly solve the eq.s
    N = odeint(model3, NO, dt, args=(\gamma(i-1), a, f, delta(i-1)))
    # store the result
    N1_{eq_6_{12}beta1[i]} = N[1][0]
    # initiation of the next step
    C02_{ppm} = N1_{eq_6_{12_{beta1}[i]/2.13}
    NO = N[1]
    a = a (CO2_ppm)
    f = compute f(CO2 ppm, \beta)
plt.plot(t[1:],N1_eq_6_12_beta1[1:]/2.13,label=' \beta = 0.38')
plt.plot(t[1:],N1_eq_6_12_beta2[1:]/2.13,label=' \beta = 0.50')
plt.plot(co2_1010[:,0], co2_1010[:,1],'k.')
plt.plot(annual_CO2_Obs_t, annual_CO2_Obs, 'k.', label='observation')
plt.ylabel('CO2 Concentration (ppm)')
plt.xlabel('Year')
plt.legend(loc='best')
my_x_ticks = np. arange(1985, 2004, 3)
plt. show()
TypeError
                                             Traceback (most recent call last)
 \AppData\Local\Temp\ipykernel_20432\1464446600.py in <module>
     11
            dt = [0, 1]
     12
            # numericly solve the eq.s
 --> 13
             N = \text{odeint} (\text{model3}, N0, dt, args=(\gamma(i-1), a, f, delta(i-1)))
            # store the result
     14
     15
            N1_{eq_6_{12}} = N[1][0]
 ^{\sim}\AppData\Local\Temp\ipykernel_20432\1454946238.py in \gamma (t)
           #get the fossil fuel data
      8
      9
            data2 = pd. read_csv("global. 1751_2008. csv")
             \gamma = \text{float}(\text{data2.loc}[(\text{data2['Year'']}] == \text{int(t))}]['Total carbon emissions from fossil-fuels (million metropy)]
---> 10
ic tons of C)']/1000/2.13)
     11
            return γ
     12
D:\LI_YANCHEN\APP_INSTALL\Anaconda\envs\cper\lib\site-packages\pandas\core\series.py in wrapper(self)
    183
                if len(self) == 1:
    184
                    return converter (self. iloc[0])
                   raise TypeError(f"cannot convert the series to {converter}")
--> 185
    186
            wrapper. __name__ = f"__{converter.__name__}
TypeError: cannot convert the series to <class 'float'>
In [ ]:
In [ ]:
In [ ]:
```