



# Attention Mechanism and Transformer

FA690 Machine Learning in Finance

Dr. Zonghao Yang

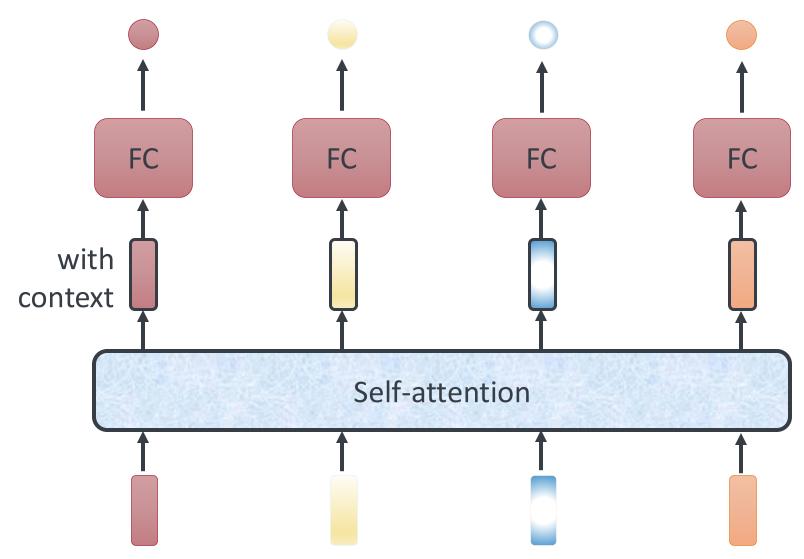
# **Learning Objective**

- Understand the self-attention mechanism and how it enables models to focus on relevant parts of input sequences
- Explore the architecture of Transformer models, including encoders, decoders, multi-head attention, cross attention
- Compare Transformer advantages over RNNs, particularly regarding parallel processing and longrange dependencies
- Examine transformer-based models like BERT and GPT, and understand how self-supervised pretraining enables these models to learn from massive datasets

# **Self Attention**

# **Motivating Example**

- Sentence completion: When she tried to print her tickets, she found that the printer was out of toner. She went to the stationery store to buy more toner. It was very overpriced. After installing the toner into the printer, she finally printed her \_\_\_\_.
- To learn from this training example, the RNN needs to model the dependency between "tickets" on the 7th step and the target word "tickets" at the end
- Vanilla RNN: Vanishing gradient problem
- LSTM: The design of three gates (input, forget, and output gates) to keep both long-term and shortterm memories
- Transformer: Input the entire sequence; the model learns where to pay attention to



# Multi-layer Self-attention

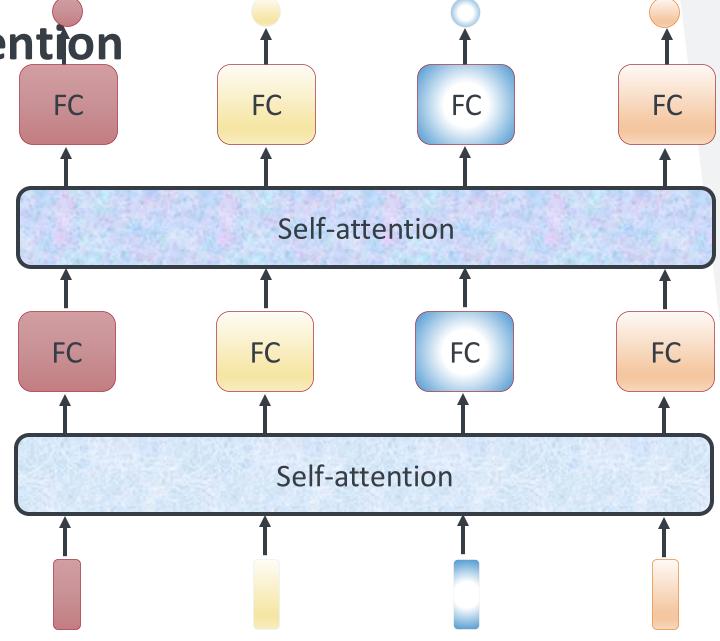


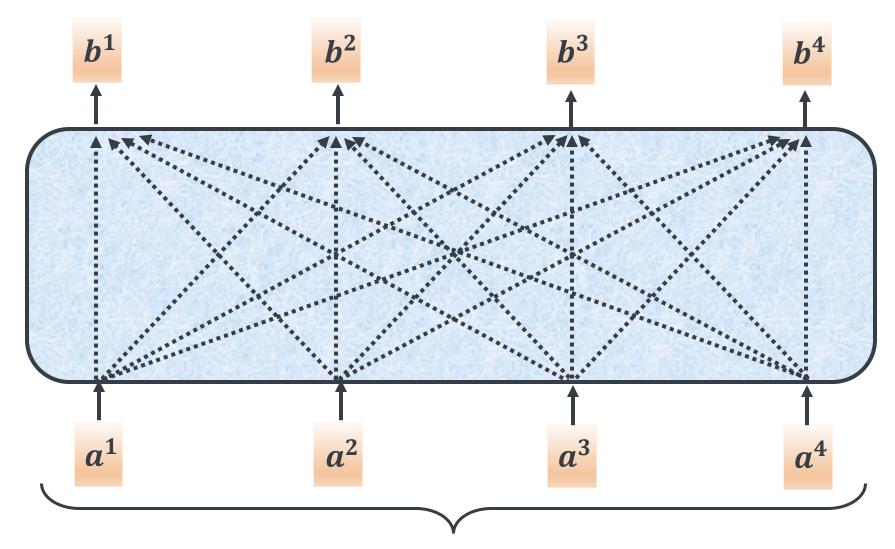
### Attention is all you need

A Vaswani, N Shazeer, N Parmar... - Advances in neural ..., 2017 - proceedings.neurips.cc

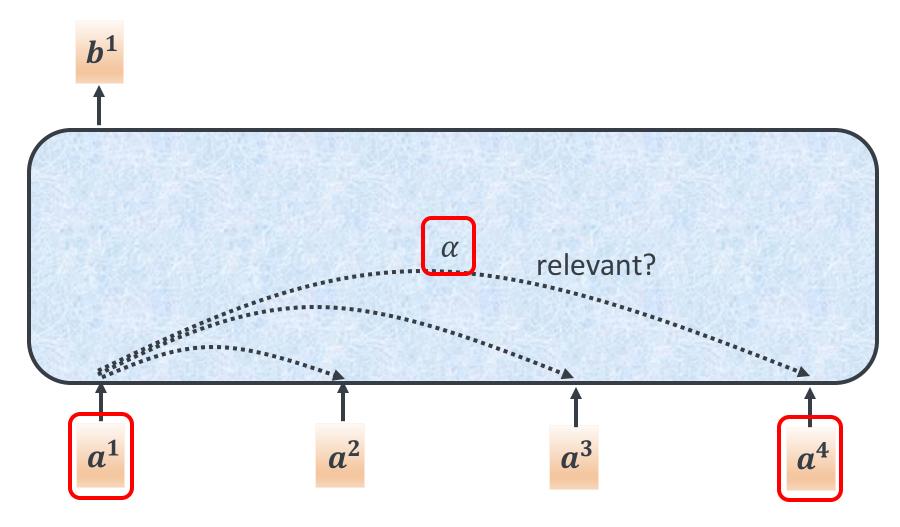
- $\dots$  to attend to **all** positions in the decoder up to and including that position. We **need** to prevent
- $\dots$  We implement this inside of scaled dot-product attention by masking out (setting to  $-\infty$ )  $\dots$

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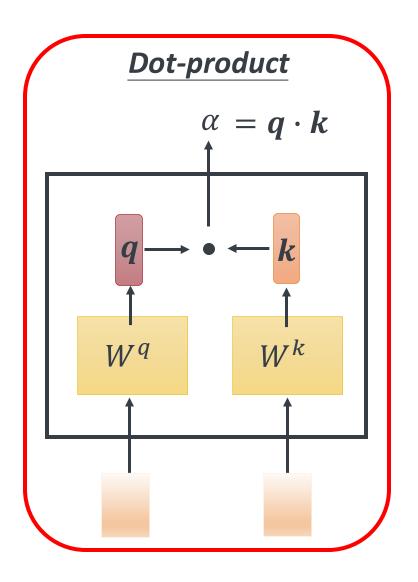


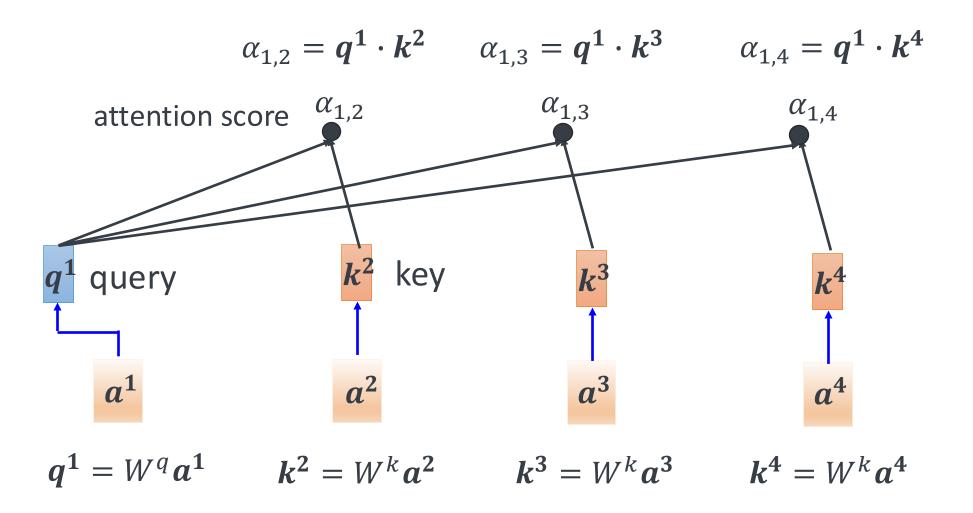
Can be either **input** or **a hidden layer** 



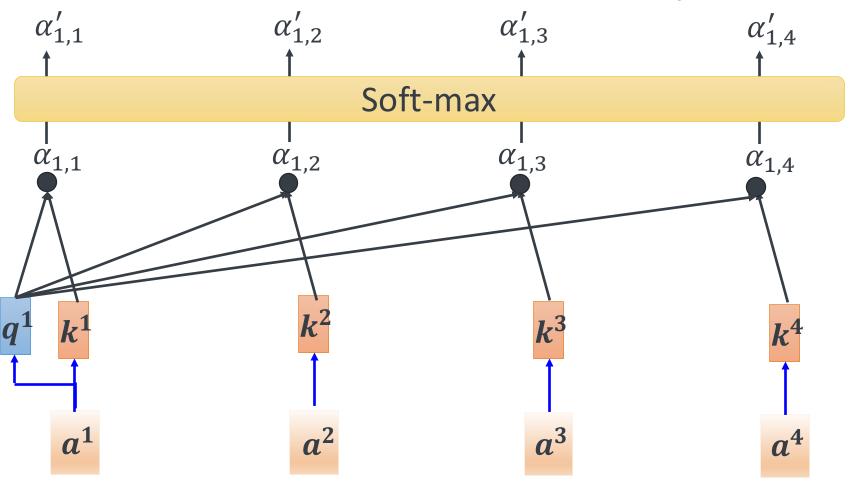
Find the relevant vectors in a sequence

# **Attention Measure**





$$\alpha'_{1,i} = \exp(\alpha_{1,i}) / \sum_{j} \exp(\alpha_{1,j})$$



$$q^1 = W^q a^1$$

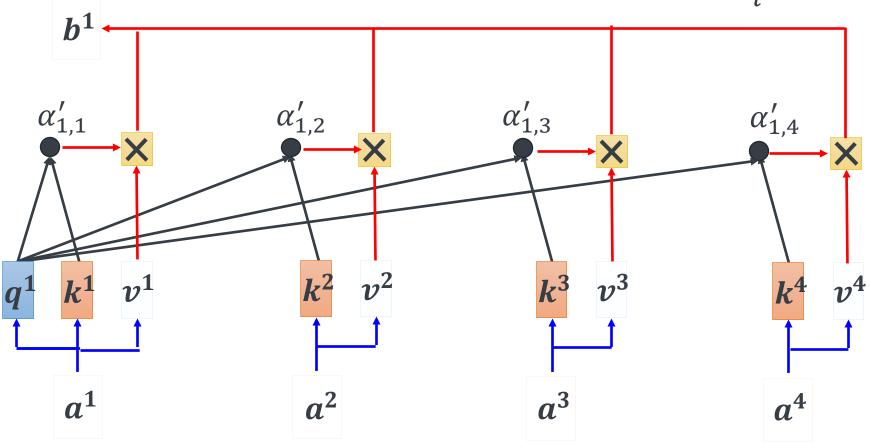
$$k^2 = W^k a^2$$

$$q^1 = W^q a^1$$
  $k^2 = W^k a^2$   $k^3 = W^k a^3$   $k^4 = W^k a^4$ 

$$k^4 = W^k a^4$$

Extract information based on attention scores

$$b^1 = \sum_i \alpha'_{1,i} v$$

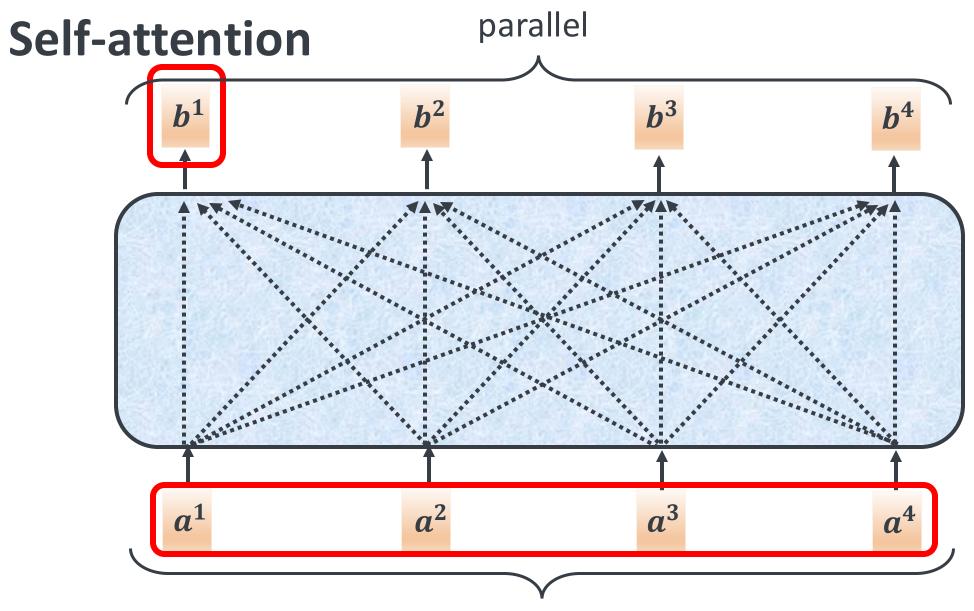


$$v^1 = W^v a^1$$

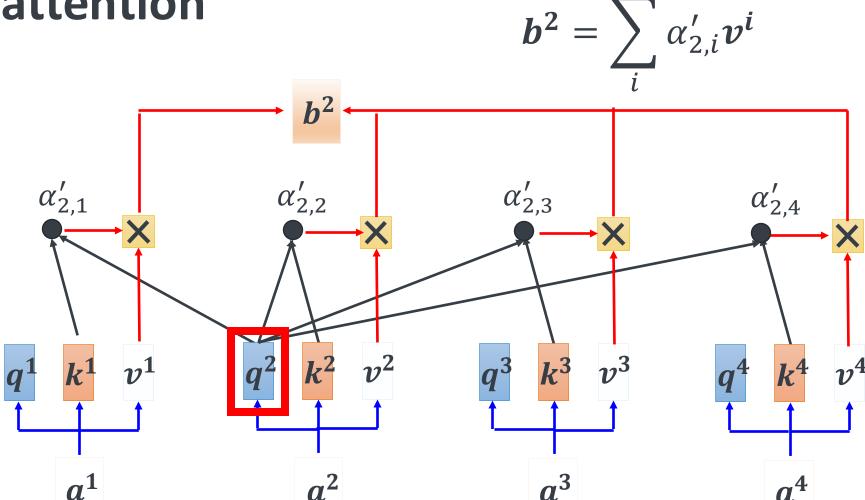
$$v^2 = W^v a^2$$

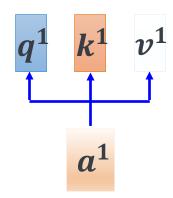
$$v^1 = W^v a^1$$
  $v^2 = W^v a^2$   $v^3 = W^v a^3$   $v^4 = W^v a^4$ 

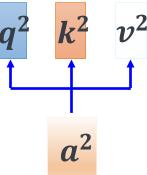
$$\boldsymbol{v^4} = W^{\boldsymbol{v}} \boldsymbol{a^4}$$

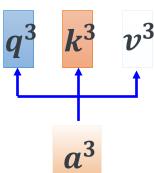


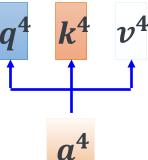
Can be either **input** or **a hidden layer** 

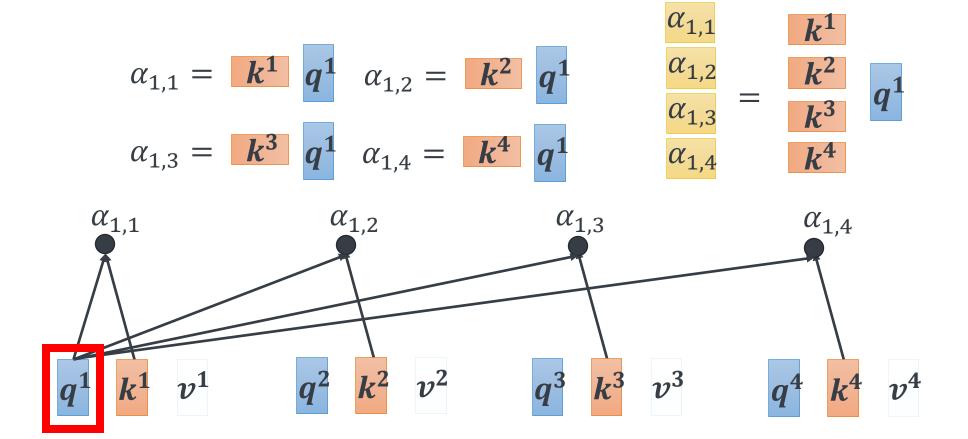




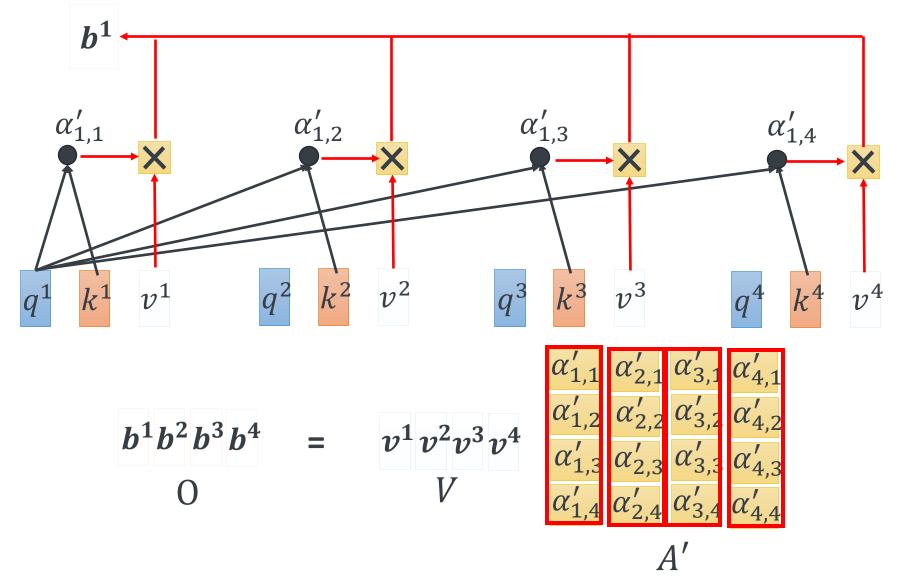








$$\alpha_{1,1} = k^{1} \quad q^{1} \quad \alpha_{1,2} = k^{2} \quad q^{1} \quad \alpha_{1,2} \\ \alpha_{1,3} = k^{3} \quad q^{1} \quad \alpha_{1,4} = k^{4} \quad q^{1} \quad \alpha_{1,4} \\ \alpha_{2,1} \quad \alpha_{2,1} \quad \alpha_{2,2} \quad \alpha_{2,3} \\ \alpha_{1,3} \quad \alpha_{2,4} \\ \alpha_{1,1} \quad \alpha_{2,1} \quad \alpha_{3,1} \quad \alpha_{4,1} \\ \alpha_{1,2} \quad \alpha_{2,2} \quad \alpha_{2,3} \\ \alpha_{2,4} \quad \alpha_{2,4} \\ \alpha_{1,1} \quad \alpha_{2,1} \quad \alpha_{3,1} \quad \alpha_{4,1} \\ \alpha_{1,2} \quad \alpha_{2,2} \quad \alpha_{3,2} \quad \alpha_{4,2} \\ \alpha_{1,3} \quad \alpha_{2,3} \quad \alpha_{3,3} \quad \alpha_{4,3} \\ \alpha_{1,4} \quad \alpha_{2,4} \quad \alpha_{3,4} \quad \alpha_{4,4} \\ \alpha_{1,4} \quad \alpha_{1,4} \quad \alpha_{1,4} \quad \alpha_{1,4} \quad \alpha_{1,4} \\ \alpha_{1,4} \quad \alpha_{1,4} \quad \alpha_{1,4} \quad \alpha_{1,4} \quad \alpha_{1,4} \quad \alpha_{1,4} \\ \alpha_{1,4} \quad \alpha_{1,4} \quad \alpha_{1,4} \quad \alpha_{1,4} \quad \alpha_{1,4} \quad \alpha_{1,4} \quad$$

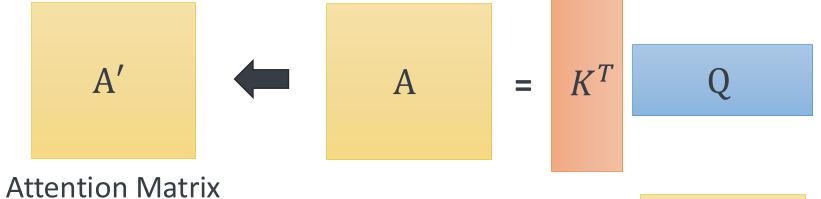


$$Q = W^{q} I$$

$$K = W^{k} I$$

$$V = W^{v} I$$

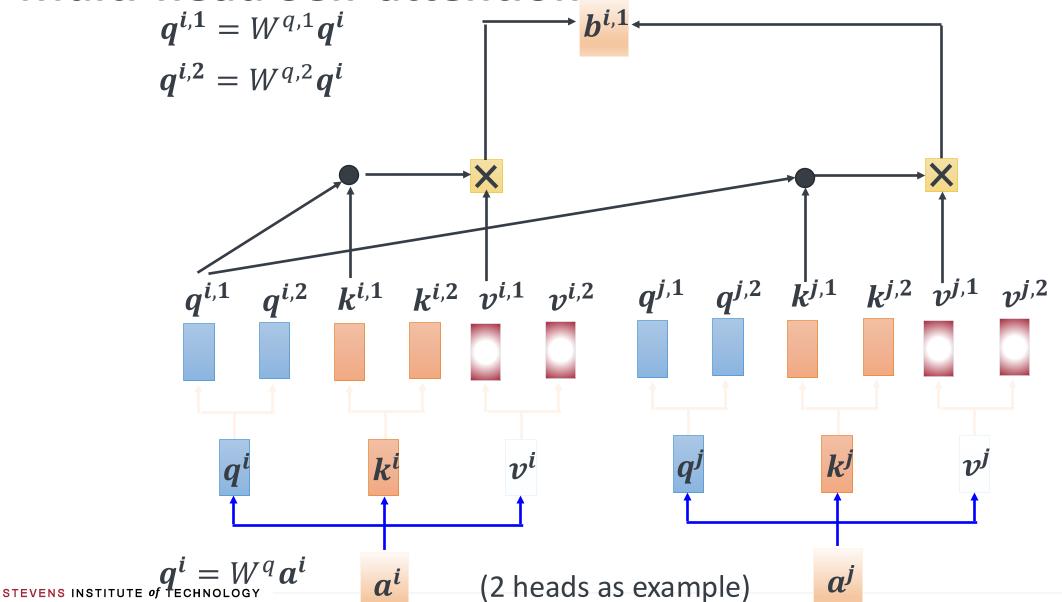
Parameters to be learned



O = V A'

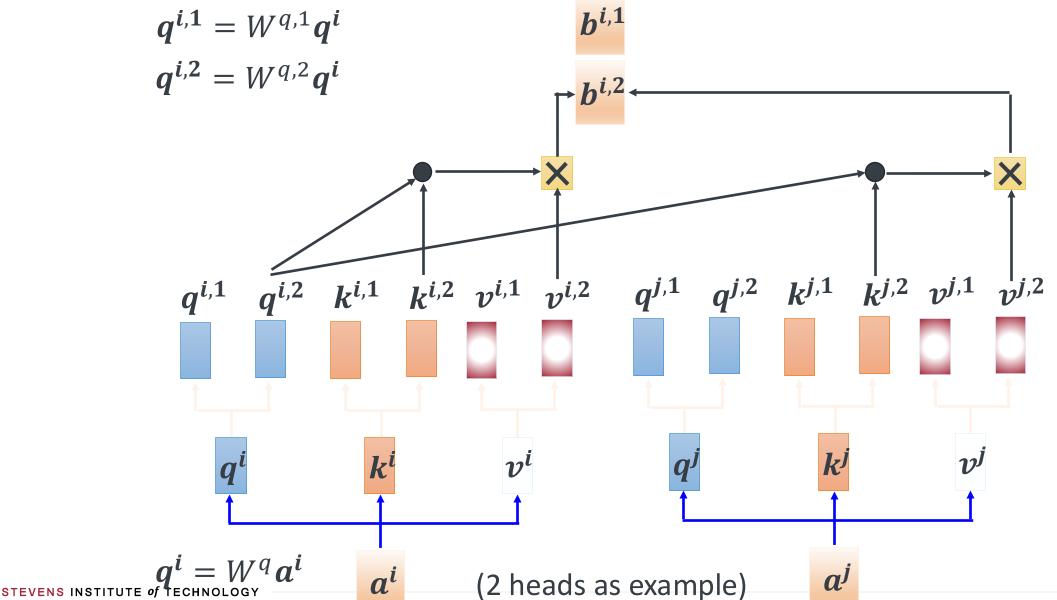
## Different types of relevance

# **Multi-head Self-attention**



### Different types of relevance

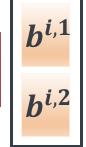
# **Multi-head Self-attention**

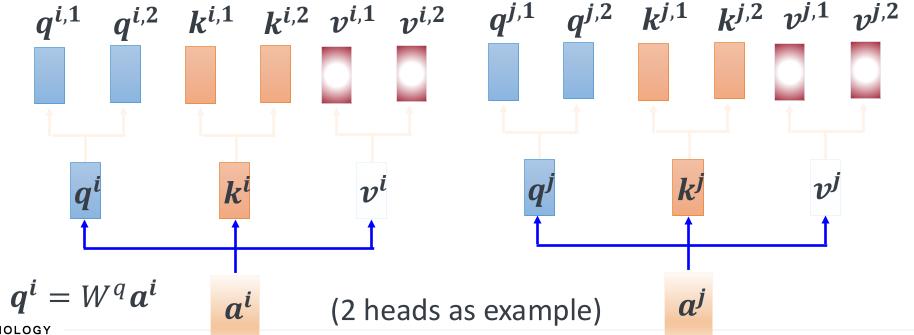


### Different types of relevance

# **Multi-head Self-attention**

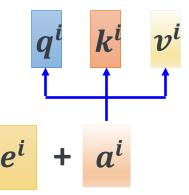
$$b^i = W^0$$



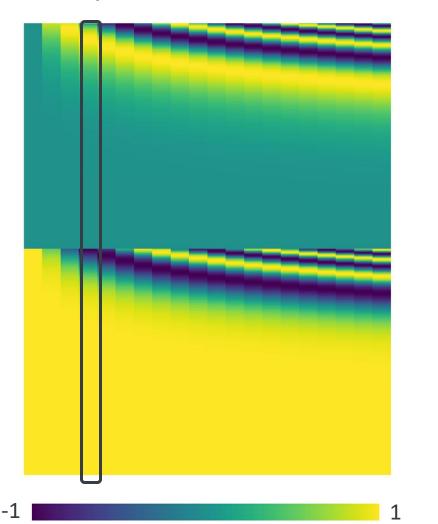


# **Positional Encoding**

- No position information in self-attention.
- Each position has a unique positional vector e<sup>i</sup>
- hand-crafted
- learned from data



Each column represents a positional vector  $e^i$ 



# **Applications of Self-attention**



**Transformer** 

https://arxiv.org/abs/1706.03762



BERT

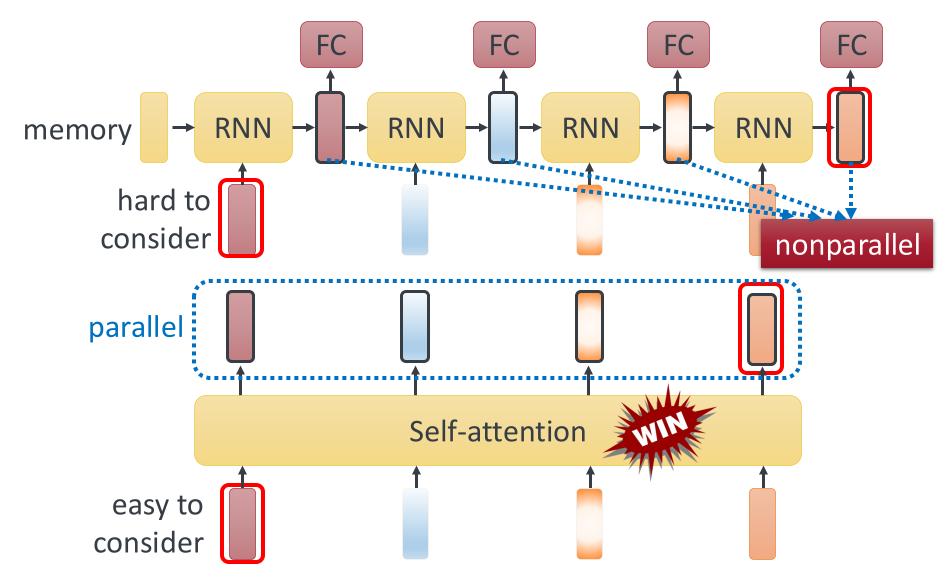
https://arxiv.org/abs/1810.04805

Widely used in Natural Langue Processing (NLP)!

# Self-attention vs. RNN

### Recurrent Neural Network (RNN)

25



# **Transformer**

# Sequence-to-sequence (Seq2seq)

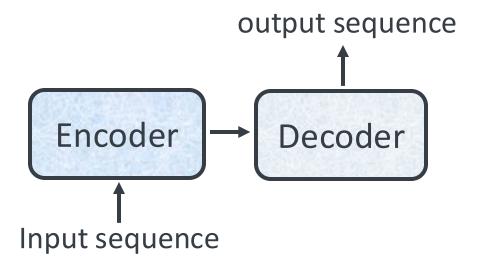
- Seq2seq: Input a sequence, output a sequence
  - The output length is determined by model, and can vary from the input
- Examples of seq2seq
  - Speech recognition: The input is audio signal, and the output is the transcript of the audio
  - Machine translation: The input and output are text in different languages
  - Large language models (Chatbot): Question answering
  - Sentiment analysis: The input is text and the output is a number indicating sentiment

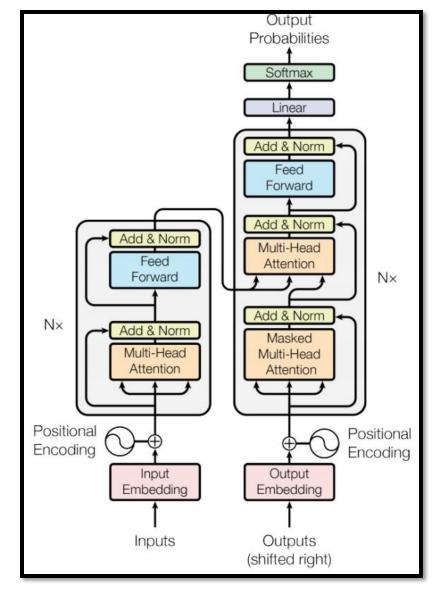


Transformer is a sequence-to-sequence model built on self attention

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# Seq2seq



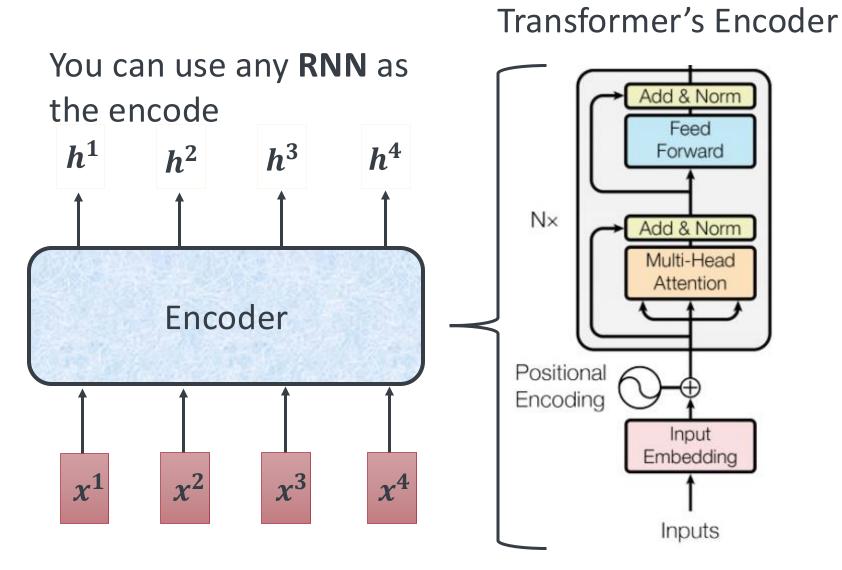


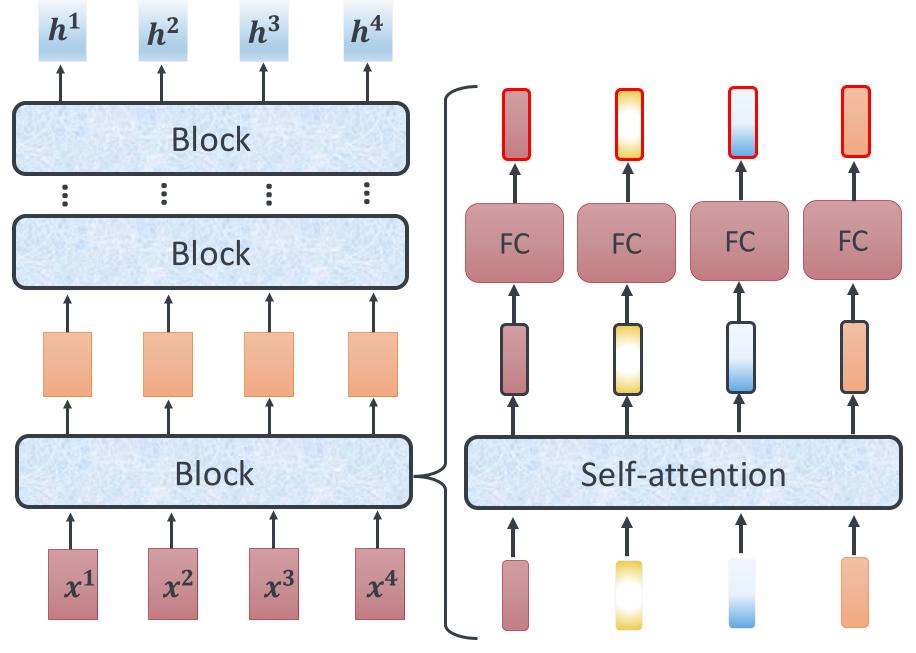
Transformer

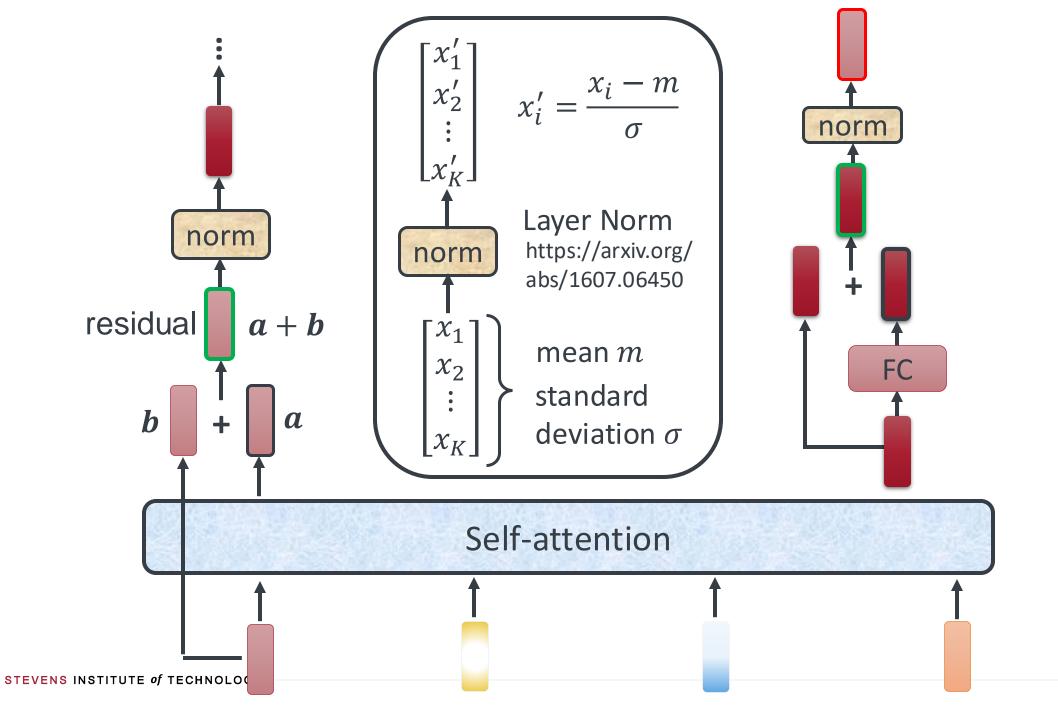
https://arxiv.org/abs/1706.03762

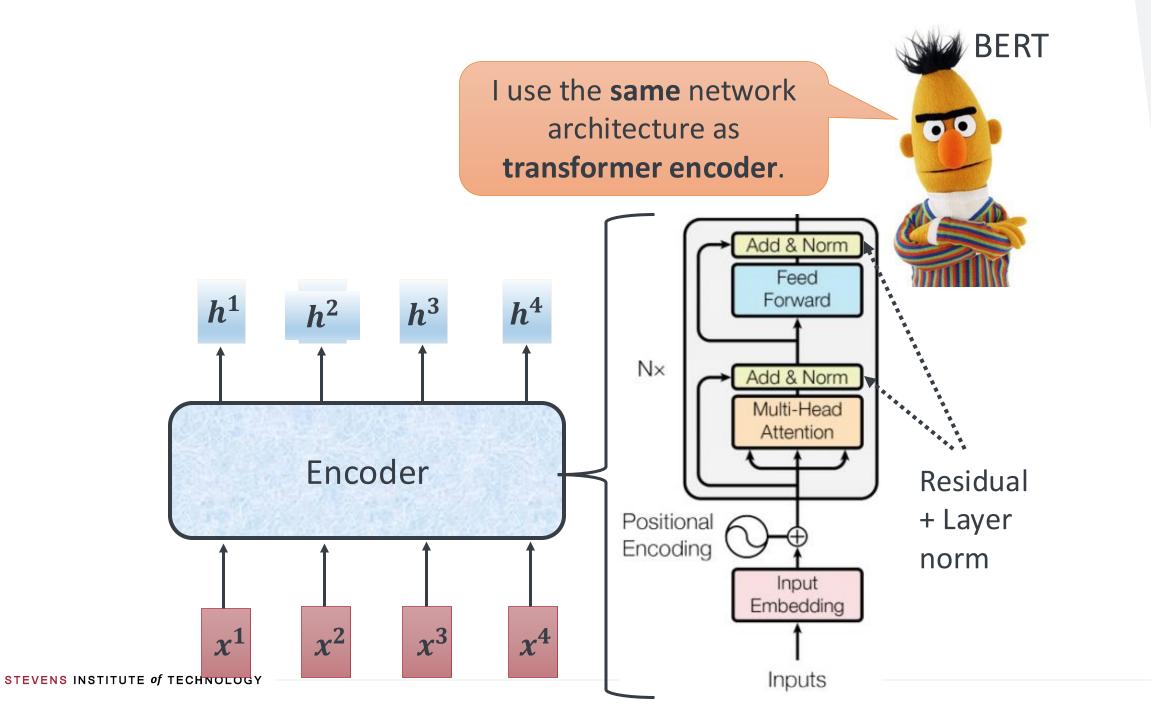
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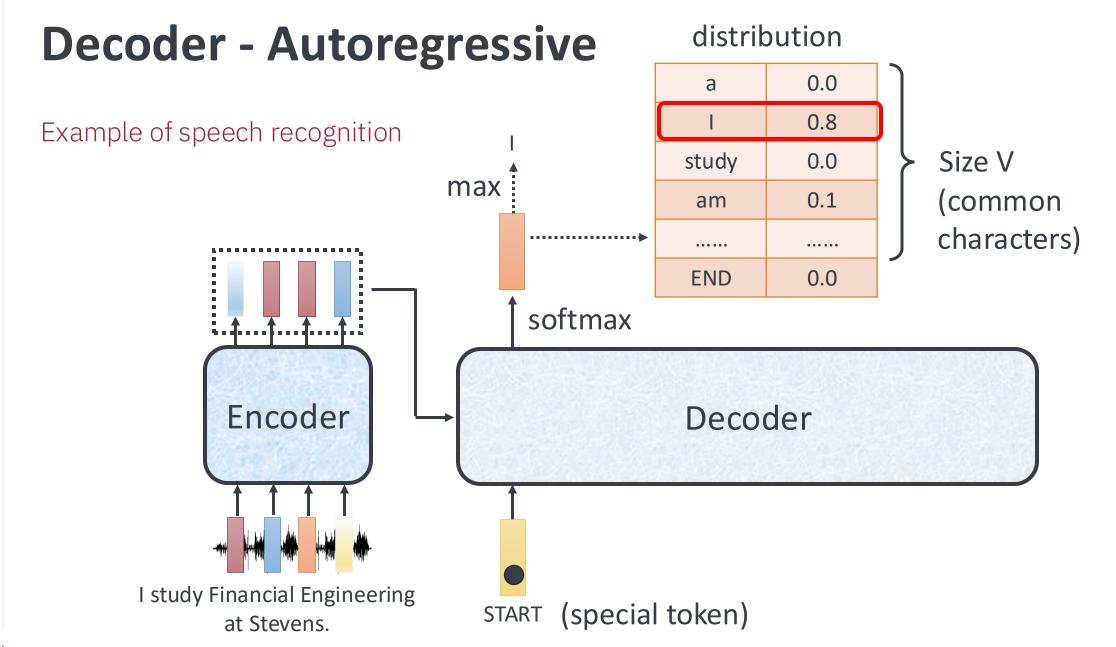
# **Encoder**



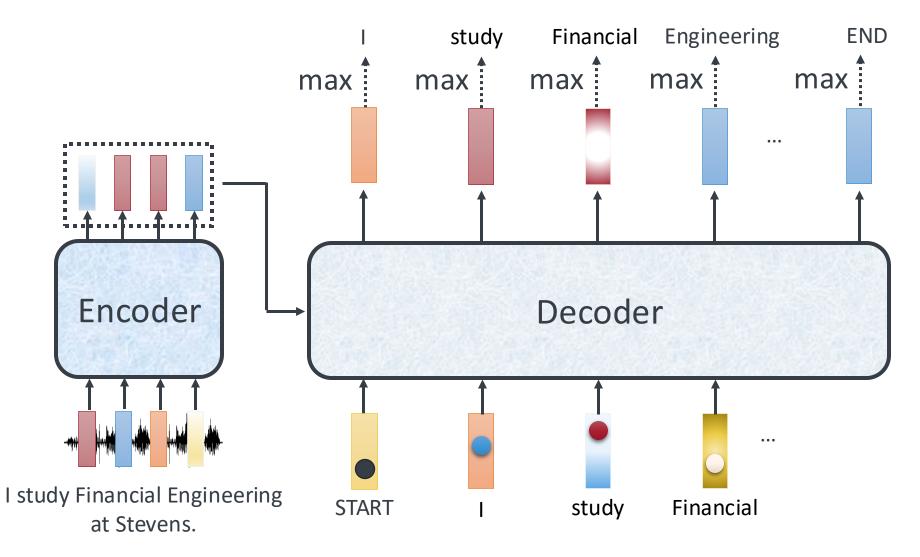


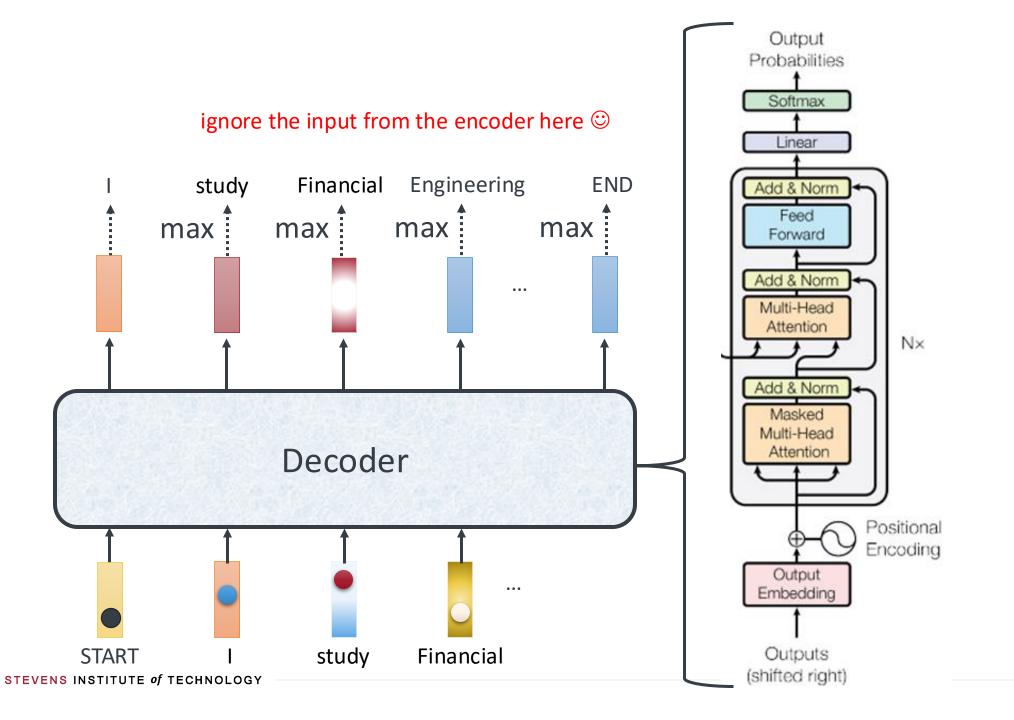


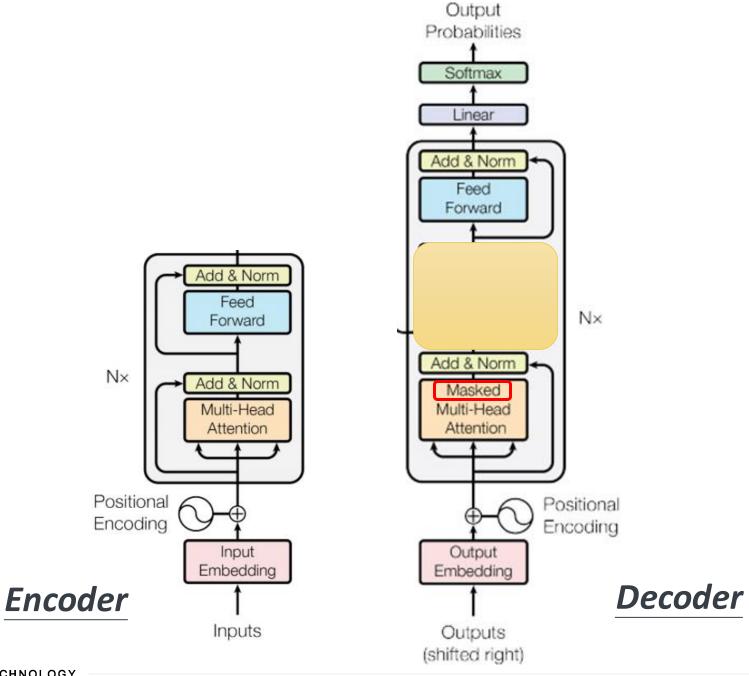




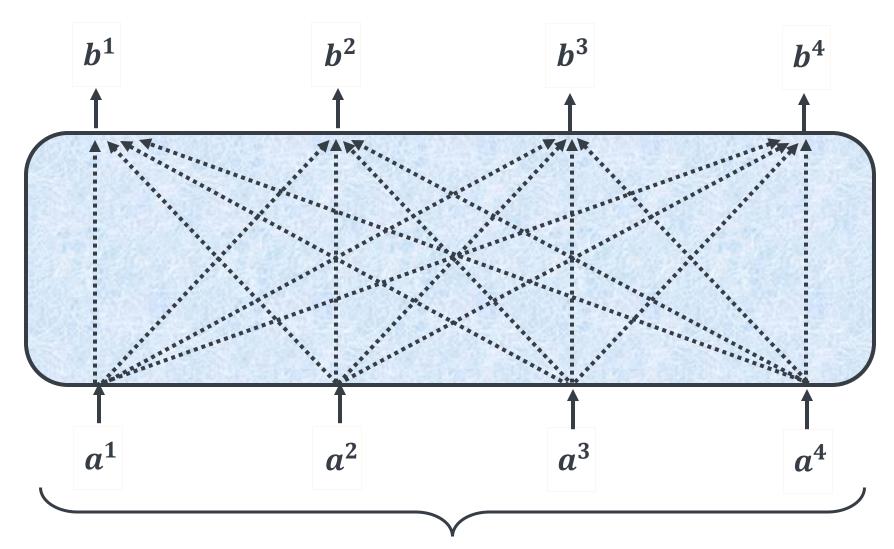
# **Decoder - Autoregressive**





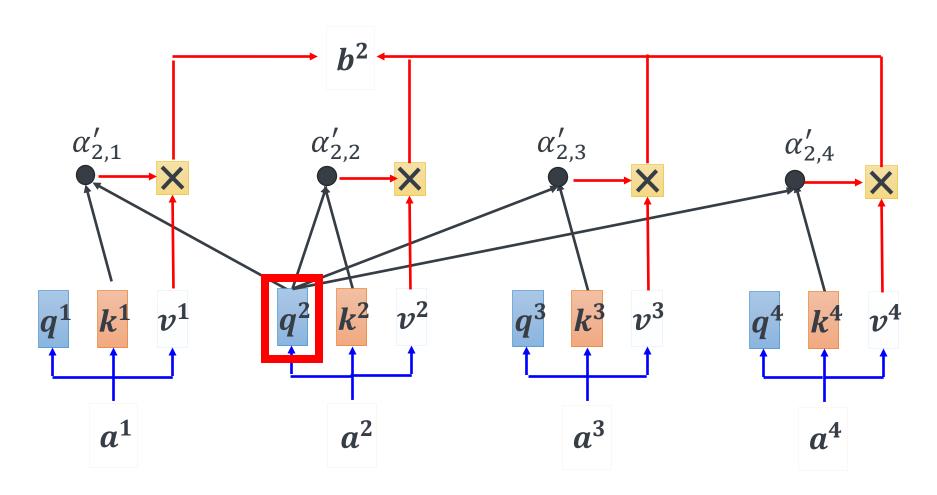


#### Self-attention → Masked Self-attention



Can be either input or a hidden layer

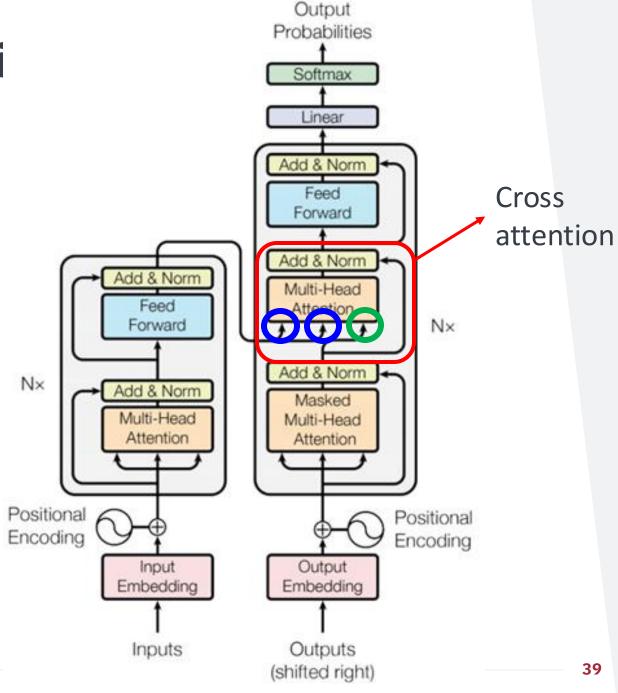
#### Self-attention → Masked Self-attention

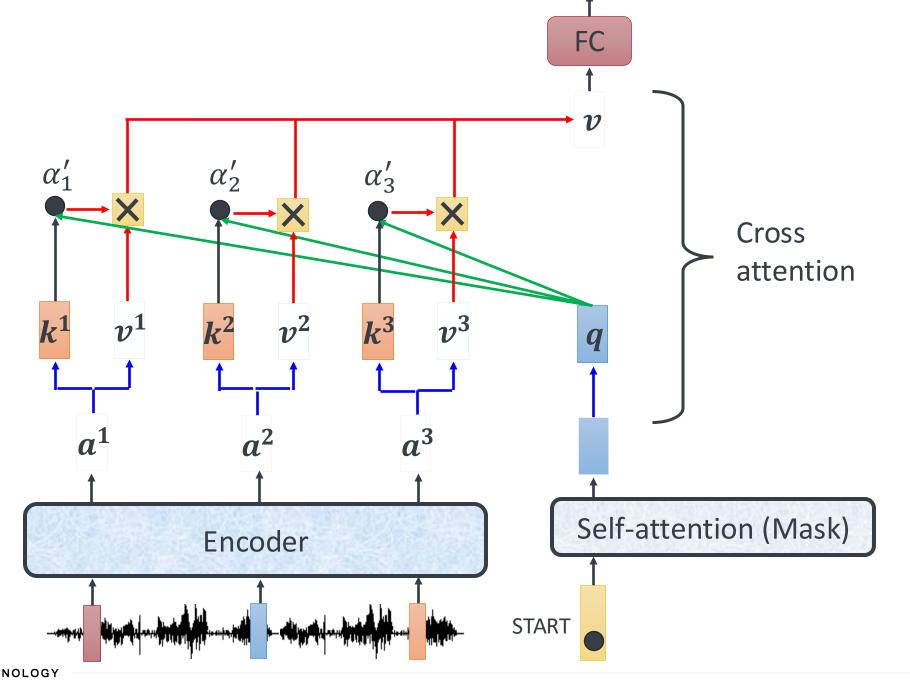


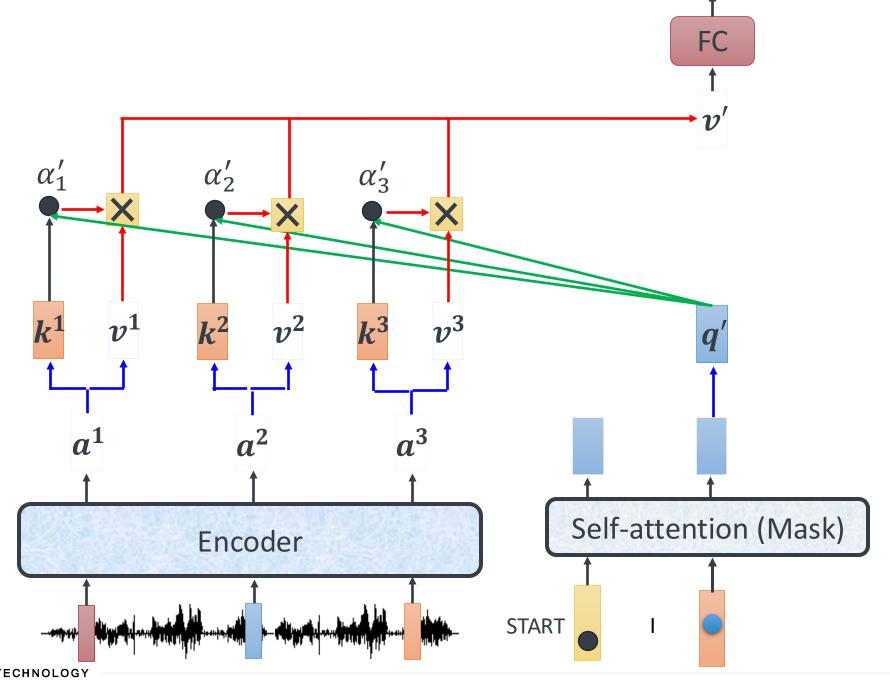
Why masked? Consider how does decoder work

#### **Transformer - Cross Attenti**

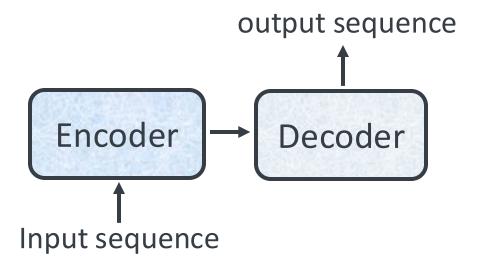
Information transformation from encoder to decoder

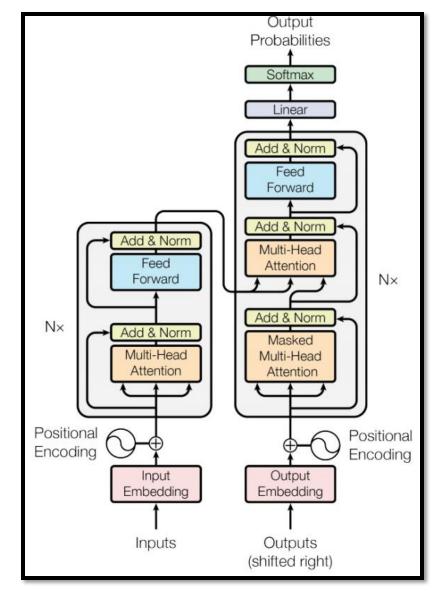






#### **Transformer**





Transformer

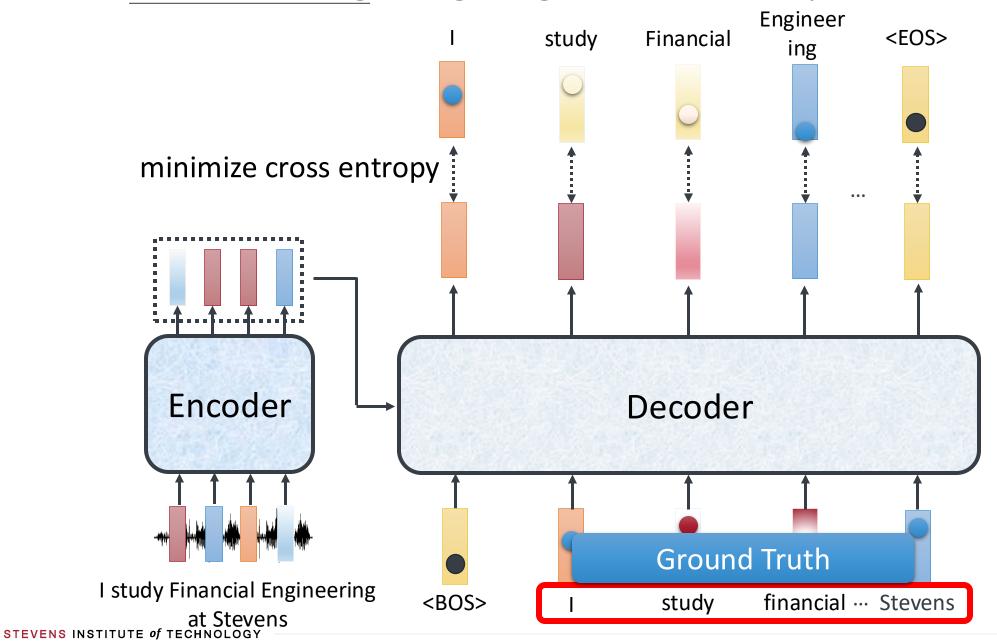
https://arxiv.org/abs/1706.03762

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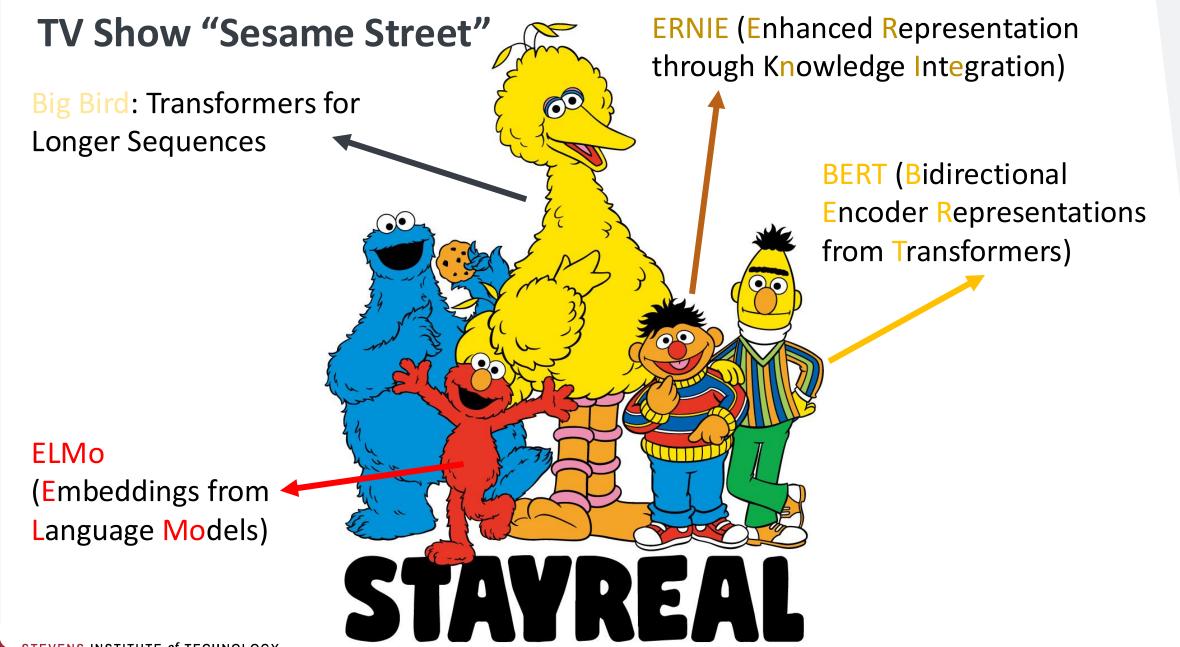
#### Ground a **Training** truth distribution study 0 0.1 a 0 am 0.7 . . . . . . . . . . . . Size V study 0.1 minimize cross entropy (common 0.1 am characters) ..... ..... softmax Encoder Decoder I study Financial Engineering STEVENS INSTITUTE of TECHNOLOGY at Stevens

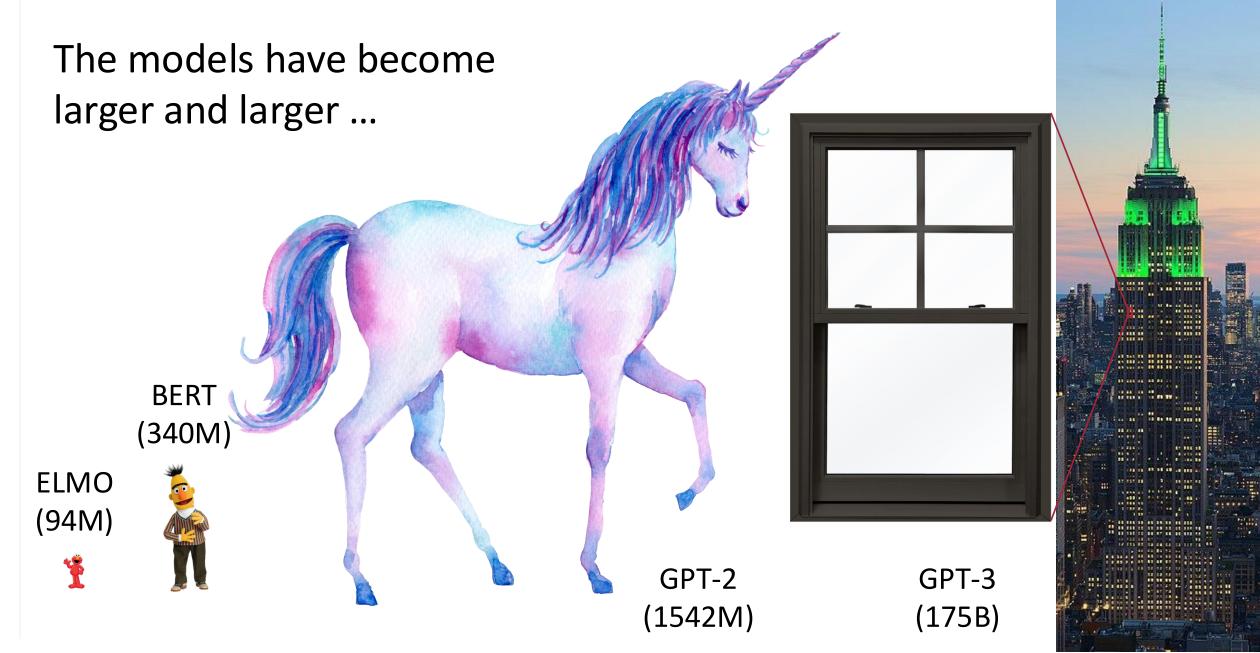
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#### **Teacher Forcing**: using the ground truth as input.



## **Bidirectional Encoder Representations from Transformers** (BERT)

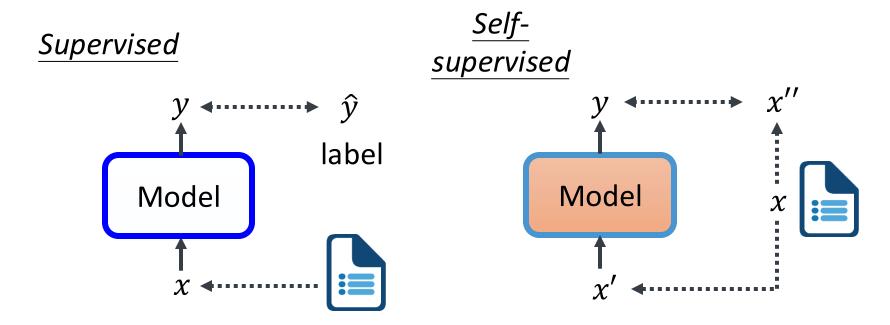


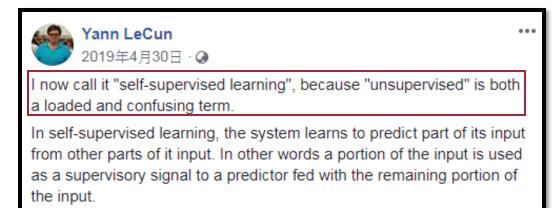


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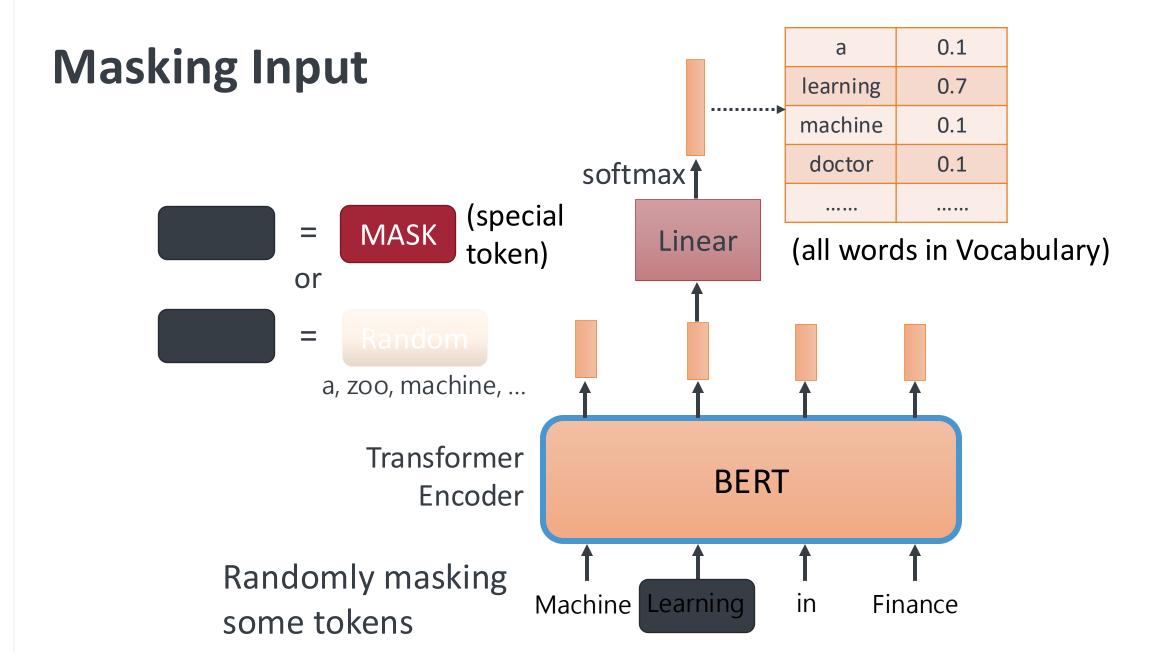
## **Self-supervised Learning**



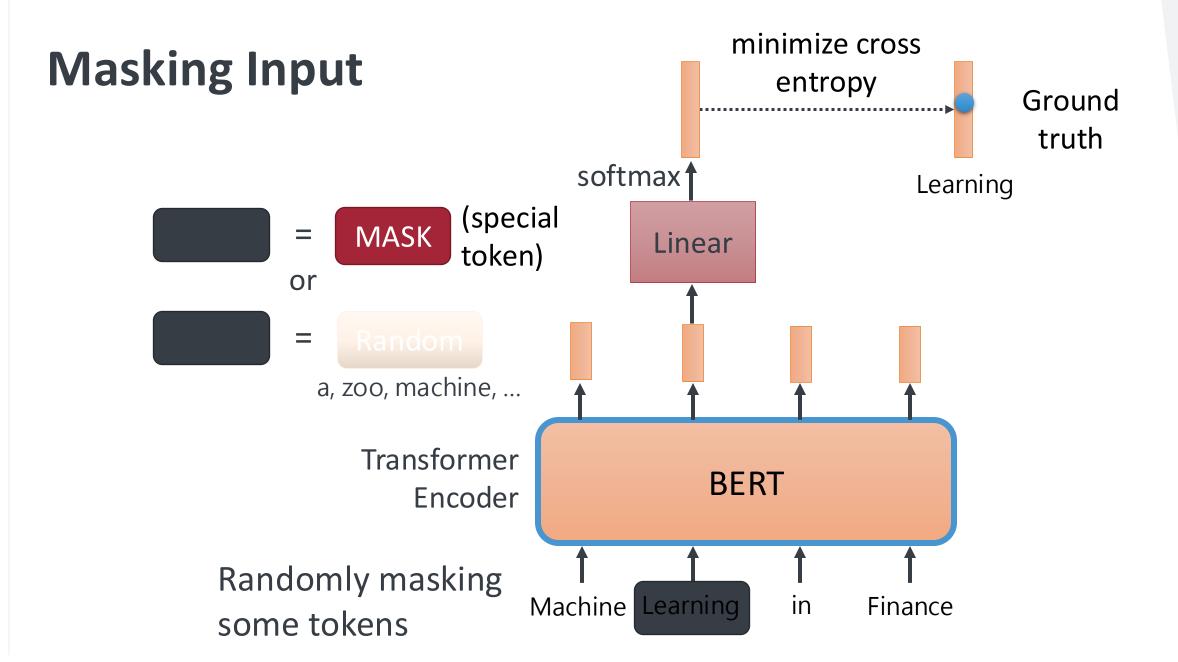


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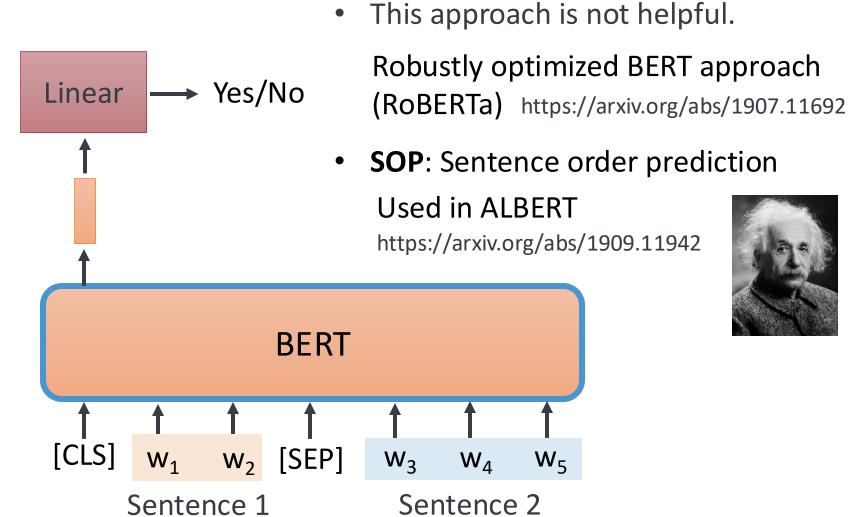
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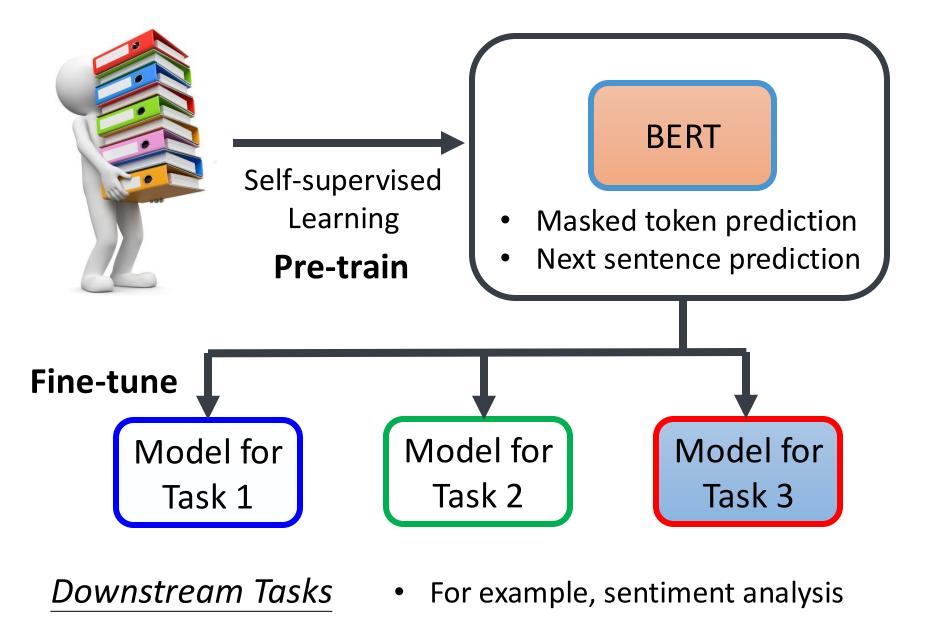


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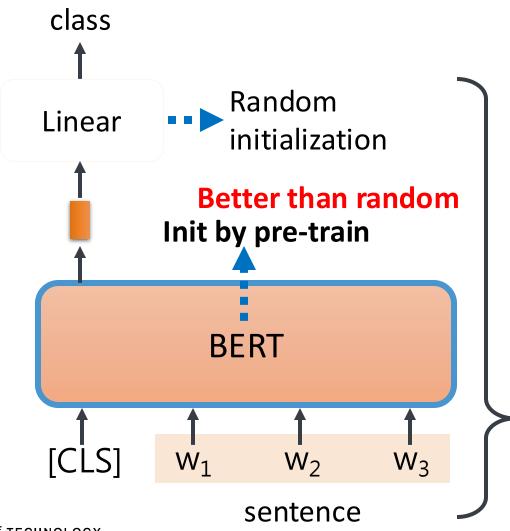
**50** 

#### **Next Sentence Prediction**





## **Sentiment Analysis using BERT**

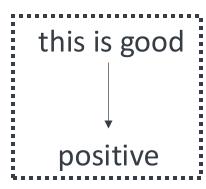


Input: sequence

output: class

Example:

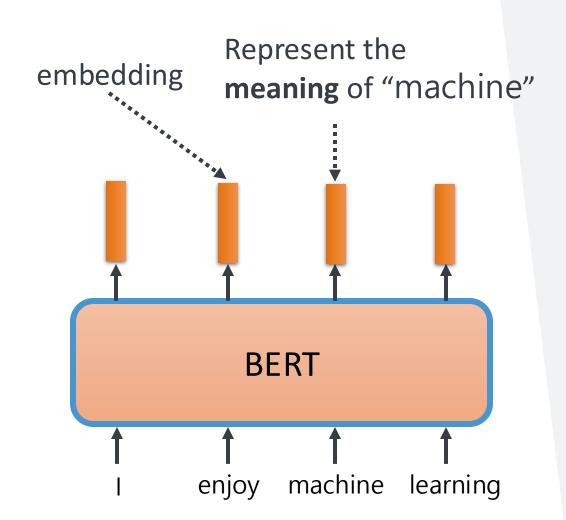
Sentiment analysis



This is the model to be learned.

## Why does BERT Work?

- BERT can be used as embedding
- Compared with embeddings models like Word2Vec, BERT considers context
  - "Apple launches the new iPad."
  - "My favorite fruit is Apple."
- Recall how Word2Vec is trained
  - Continuous Bag of Words is similar to the self supervised learning in BERT



I eat an apple every morning for breakfast.

The apple tree in the garden is full of red fruits.

An apple a day keeps the doctor away.

She sliced the apple into small pieces for the salad.

This apple tastes sweet and juicy.

Apple is known for its innovation.

I bought my first Apple laptop last year.

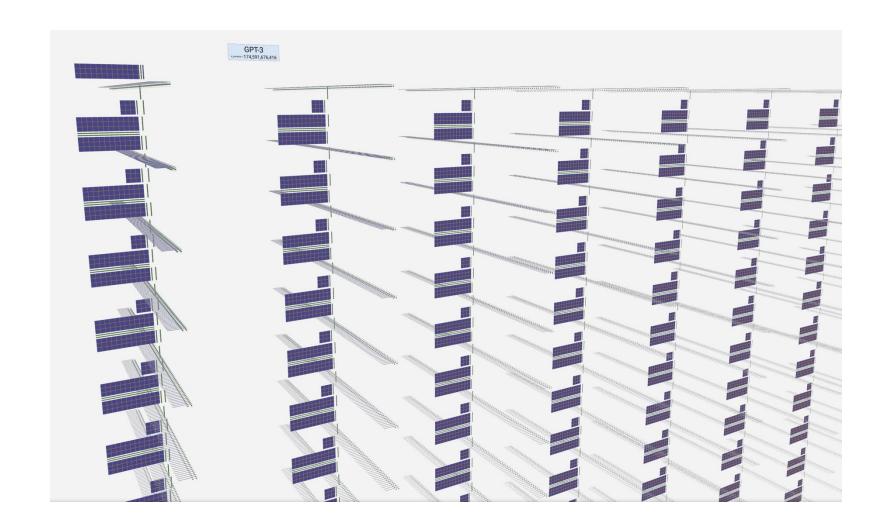
Apple released the latest version of iOS yesterday.

Many people love Apple's user-friendly interface.

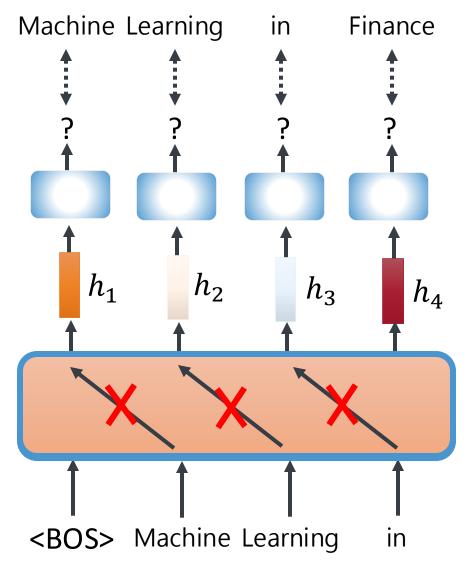
Apple's headquarters is located in California of TECHNOLOGY

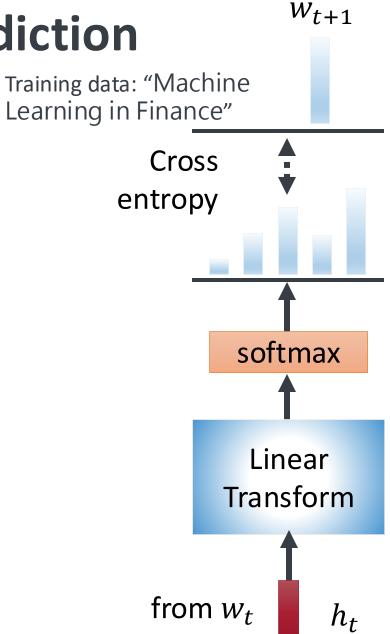
## **Generative Pre-trained Transformer (GPT)**

## **Generative Pre-trained Transformer (GPT)**



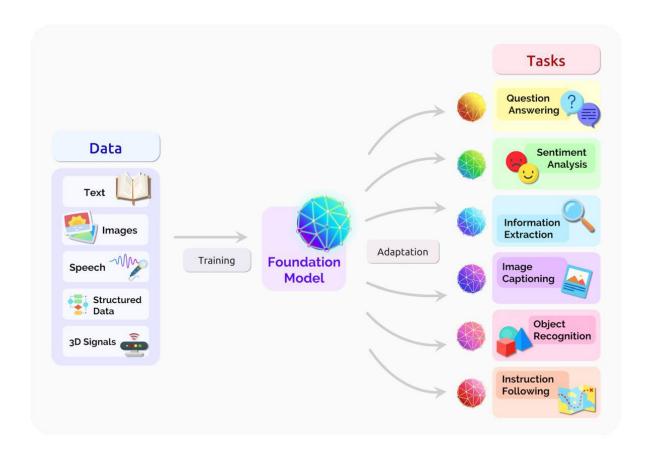
## **Training GPT: Next Token Prediction**





#### **Pretraining: Scaling Unsupervised Learning on the** Internet

- Key ideas in pretraining
  - Make sure your model can process large-scale, diverse datasets
  - No need for labeled data (otherwise you can't scale!)
  - Compute-aware scaling

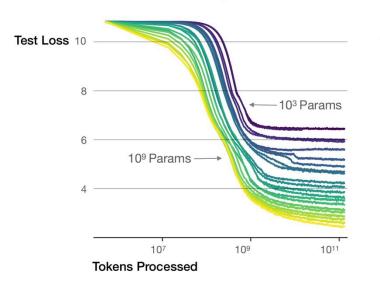


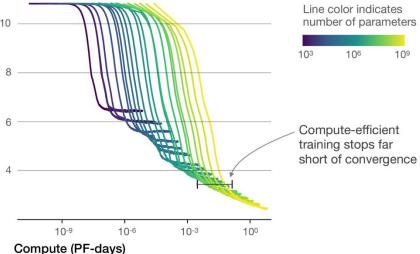
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### **Scaling Laws**

Larger models require **fewer samples** to reach the same performance

The optimal model size grows smoothly with the loss target and compute budget





#### [PDF] Scaling laws for neural language models

J Kaplan, S McCandlish, T Henighan, TB Brown... - arXiv preprint arXiv ..., 2020 - arxiv.org

... We study empirical **scaling laws** for **language model** performance on the cross-entropy loss. The loss scales as a power-**law** with **model** size, dataset size, and the amount of compute ...

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### Acknowledgement

The lecture note has benefited from various resources, including those listed below. Please contact Zonghao Yang (zyang99@stevens.edu) with any questions or concerns about the use of these materials.

- Lecture Notes on self-attention, sequence-to-sequence modeling, and BERT from ML 2021 Spring by Hung-Yi Lee at National Taiwan University
- Lecture Notes on Pretraining from CS224N 2025 Winter at Stanford University

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# THANK YOU

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