

Programming Assignment 3: Report

(a) [10 points] The recursive relation that you need to use to compute `maximizeSentimentalValue()`.

`maximizeSentimentalValue(i, w)` is short as `mSV(i, w)` that tracks the maximum sentimental value with current items and weight.

$$mSV(i, w) = \begin{cases} 0, & \text{if } i = 0. \\ mSV(i - 1, w), & \text{if } w_i > w. \\ \max\{mSV(i - 1, w), v_i + mSV(i - 1, w - w_i)\} & \text{otherwise.} \end{cases} \quad (1)$$

(b) [30 points] The recursive relation that you need to use to compute `cleverWidthReduction()`.

The "content" value of each pixel is stored in a matrix `contents`. `i` index is the number of row from the top, and `j` index is the number of column from left. The "content" value of pixel at `i`-th row, `j`-th column is `contents[i][j]`.

The function calculating the minimum sum of content along a path from the 1-th row to the `h`-th row is named `minContentSum(i, j)`, where `i` and `j` are the height and width of the pixel that we are ending at. The valid `j` range of `contents` and range of matrix storing function `minContentSum(i, j)` result is from 1 to `w`, and the valid `i` range is from 1 to `h`. Function `minContentSum(i, j)` is short as `mCS(i, j)` below.

Each element in the dynamic programming result matrix `DP[i][j]` is computed by `mCS(i, j)`. Then we know the pixel where the vertical path ends is at the `h`-th row with the minimum sum of content. Tracking back from that pixel gives us a vertical path to delete. Then, delete and update (`width - desired_width`) times to get the desired width.

$$mCS(i, j) = \begin{cases} contents[i][j], & \text{if } i = 1 \text{ and } 1 \leq j \leq w. \\ \infty, & \text{if } j < 1 \text{ or } j > w. \\ contents[i][j] + \min \begin{cases} mCS(i - 1, j - 1), \\ mCS(i - 1, j), \\ mCS(i - 1, j + 1), \end{cases} & \text{if } 1 < i \leq h \text{ and } 1 \leq j \leq w. \end{cases} \quad (2)$$