Inference 2: Fitting models to data: Variable selection

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Multiple regression

Multiple regression = more than one input variables. Model:

$$Y = \beta_0 + \beta_1 X_1 + \dots + \beta_k X_k.$$

 X_1, \ldots, X_k : input variables. Can be either numerical or indicator. Examples

- We saw: one categorical with k + 1 categories recoded as k binaries
- ▶ teacher: salary vs degree + fulltime + years
- marioKart: totalPrice vs everything else

Multiple regression: diagnostics

Model: $Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + \cdots + \beta_k X_{ki} + \epsilon_i$.

Assumptions on the ϵ_i 's:

- Independence
- Normally distributed
- Constant variance

Examples: teacher, marioKart

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What should we do? Variable selection.

Variable selection: bigger \neq better

Variable selection = discard useless X's, put in useful X's. A variable is useful if it does ONE or more of the following:

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eg: we ran: teacher: total vs degree + year why not fit teacher: total vs degree + year + fulltime + fica + retirement?
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retirement?

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Good tools

- pairwise plots of all variables
- scatterplot: predicted vs observed
- adjusted R²: R² with a penalty on number of variables in model
- p-values of the coefficients

Remedies

- Exclude useless inputs
- transform inputs (eg: salary²)

Example: teacher, marioKart.
Rule of thumb: Simple = best

How to select variables?

Variable selection strategies:

- ► Backward: put all variables in, then gradually remove the useless ones
- Forward: put in one variable at a time
- ► Stepwise: backward + forward at the same time

Criterion: adjusted R^2 , **AIC**, BIC etc

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Good news: R can do this automatically for you!

Bad news: R is not that smart. YOU need to check if the results

make sense.