

Inference 1: Hypothesis testing (cont)

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Which test to use

- ▶ Depends on data
- ▶ S (test stat) depends on H_A (alternative)
- ▶ justifying the assumptions = CRUCIAL.

Tests we learn	num	cat	cat. vs cat.	num. vs cat.
Fisher's exact			✓	
permutation (randomization)	✓	✓	✓	✓
chi-square			✓	
z-test for proportions		✓		
t-test	✓			
two-sample t-test				✓
ANOVA				✓

Permutation test: computability > precision

Fisher's exact test failed to compute on class vs survived. What to do?

Permutation test: puts computability first.

Key ideas:

- ▶ Approximate $\mathbb{P}(S \geq s | H_0)$ by simulating the distribution of S under H_0 .
- ▶ Simulate S under H_0 by resampling the data without replacement.

Data example: see code.

Advantages?

Disadvantages?

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Advantages?

- ▶ Replace math (thinking) by simulation (brute force)
- ▶ Always return an answer
- ▶ Apply to basically any situation (any data type, any H_0/H_A , any test statistic)

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Disadvantages?

- ▶ May not have nice theoretical properties (eg: not maximal power etc)
- ▶ If distribution is complicated, must sample for a long time
- ▶ May not be reproduceable exactly: different simulation could give slightly different p -values