

Unlocking A-Share Market Dynamics: Exploring ESG Impact on Volatility and Mean-Variance Portfolio

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1 Introduction

ESG is developed to evaluate the sustainability of corporate operations and their impact on social values from three dimensions: environment, society, and corporate governance. ESG criteria have gained substantial attention in recent years as investors increasingly prioritize sustainability and ethical considerations in their investment decisions. Understanding the relationship between ESG scores and stock market dynamics, particularly stock return volatility, is crucial for investors, policymakers, and corporate stakeholders.

According to Pedersen, ESG scores can provide information about company fundamentals on the one hand and influence investor preferences on the other (2020, p.572)[10]. Inspired by this, our article aims to study whether ESG indicators play a guiding role in stock selection and how to incorporate this indicator when building an investment portfolio in China's A-share market.

To verify ESG scores' impact on stock volatility, we use Ordinary Least Squares regression on listed companies in the Chinese A-share market. Then we incorporate ESG factors to construct investment portfolios. We modified the Markowitz Mean-Variance Model by introducing ESG score constraints and further explored the impact of ESG on Mean-Variance investors' preferences.

2 Literature Review

In recent years, investors have begun to consider the impact of non-financial factors in addition to the company's financial fundamentals when trading (Giese et al., 2019, p.69)[8]. The trading demand of investors unrelated to financial fundamentals have an impact on stock prices, and the sharp volatility of stock prices cause stock market risks. With the widespread adoption and deepening understanding of the ESG (Environmental, Social, and Governance) framework, ESG criteria has been integrated into investment portfolio construction process as an important non-financial factor. Research has shown that better ESG performance has the potential to increase firm value through lower firm

risk (Aouadi et al., 2018, p.1030)[2]. Sassen et al. (2016, p.867)[11] suggest a significant negative correlation between ESG scores and stock return volatility in European markets, indicating that firms with superior ESG performance experience lower volatility in their stock prices. Similarly, Alareeni et al. (2020, p.1409)[1] document a similar pattern in the US market, attributing the lower volatility to enhanced corporate governance practices and environmental stewardship. Our first research question will verify the negative impact of ESG on stock return volatility in the Chinese A-share market using similar methods compared to previous research.

Incorporating Environmental, Social, and Governance (ESG) factors into portfolio construction is essential, with the mean-variance model playing a pivotal role. This model balances the competing goals of maximizing profit while minimizing risk. Markowitz addressed this core challenge by developing a parametric optimization model that is broad enough to apply to a wide range of real-world scenarios yet straightforward for theoretical examination and numerical solution (Steinbach, 2001, p.31)[13]. At the end of 2016, Global Survey showed large and experienced investors were increasingly focusing on ESG investment practices. State Street's Center for Applied Research surveyed 582 institutional investors who have implemented or plan to implement ESG strategies. Increasingly number of institutional investors in Americas, EMEA and Asia-Pacific, plan to utilize the impact of ESG in their investment strategies (Eccles et al., 2017, p.125)[6].

To employ ESG investment strategies of varying types and degrees, Drut[5] (2010) integrated the incorporation of ESG scores directly into investors' utility function. Their study clarified that taking ESG into consideration restricts their investment universe and the return will be penalized in a mean-variance framework. Based on the Pedersen et al's research (2019, p.573)[10], investors can be categorized into three groups: Type-U (ESG-unaware) investors, Type-A (ESG-aware) investors and Type-M (ESG-motivated) investors. Essentially, Type-M investors seek a portfolio that strikes an optimal balance between high expected returns, low risk, and elevated average ESG scores. Pedersen et al. demonstrated and explained that the increasingly widespread adoption of ESG affects

portfolio selection and equilibrium asset prices.

Based on previous findings, we consider the inclusion of ESG metrics in the mean-variance model. We only focus on Type-M investors to study what role ESG specifically plays in people's investment behavior in different ESG-preferring investor populations, what can be achieved after considering ESG, and to quantify the costs and benefits caused by ESG metrics.

3 Research Questions

- Verify the impact of corporate ESG scores on stock return volatility in China's A-share market.
- Introduce ESG Scores to improve the Markowitz Mean Variance Model and study the impact of ESG on mean variance investors' preference.

4 Data

4.1 Data Description

The data in this article is mainly from CSMAR database, Sino-Securities Information Service Platform, and CFND database. In the first research question, we take the data of Chinese A-share listed companies from 2017 to 2022 from CSMAR as the research sample and analyzes the impact of ESG performance on the volatility of stock returns. The factor names and brief descriptions are shown in the table below.

In our factor selection process, we draw upon insights from prior research. For instance, Engelhardt (2021) advocates for incorporating various financial indicators to gauge company performance (p.7133)[7]. Additionally, we consider media oversight. The dissemination of information by multiple media outlets can mitigate information asymmetry in the market, indirectly enhancing the efficacy of ESG initiatives in influencing corporate

value and temporarily stabilizing stock prices. However, indiscriminate exposure to media scrutiny may backfire. Managers might resort to earnings manipulation and financial statement embellishment under media pressure, potentially leading investors astray in their decision-making.

Control Variables	Factor Description	
Volatility	The volatility of stock returns over the past 250 trading days	
esgscore	esg score given by Sino-Securities Information Service Company	
dummy audit	Credibility of audit reports	
Director Ratio	number of directors/number of supervisors	
TopTenHoldersRate	Shareholding ratio of top ten shareholders	
DA	debt to total assets ratio	
ROE	return on equity	[H]
media	log(number of media comments +1)	
PB	price to book ratio	
BM	book to market ratio	
ATO	total asset turnover ratio	
total asset log	log(value of total asset+1)	
dummy year	represent the year effect	
beta	systemic risks relative to the A-share market	

Table 1: Factor Description

In the second research question, we take the stock return of Chinese A-share listed companies from 2009 to 2023 from CSMAR and ESG scores from Sino-Securities Index Information Service.

4.2 Data Processing

For the first research question, we refer to the approach of Yang Zhuqing and Liu Shaobo (2013, p.75)[12]. We use the standard deviation of the return rate of individual stocks taking into account cash dividend reinvestment on past 250 trading days of the company within a year to represent stock price volatility (2013, p.75). To facilitate the interpretation of the coefficient, we expand the volatility by 100 times on the original basis. Besides, we perform logarithmic operations when dealing with the total asset variable.

To address missing values, we excluded data from companies that did not disclose financial indicators. Regarding missing values for media supervision, we assigned a value of 0 to the media supervision variable. This approach was adopted because CFND's media supervision data reflects the frequency of a company's review by mainstream media outlets in a given year. Therefore, if data for certain companies are missing, it implies that they were not subject to review by domestic mainstream media.

5 Methodology

5.1 ESG Score's Impact on Stock Return's Volatility

To investigate how ESG factors influence stock returns' volatility, we construct a regression model to verify the correlation between ESG and return volatility. Based on previous literature, we carefully select 10 prevalent and significant influential factors, covering company operational factors, management structure, Beta coefficients and so on, as independent variables.

According to Zhou (2021)[14], companies that actively fulfill ESG responsibilities and disclose them are more likely to attract media attention, thereby disseminating company-specific information to investors and affecting stock price volatility. Hence, we account for media influence and incorporate the ESG scores provided by the Sino-Securities Index Information Service's ESG Rating Index. We set the dependent variable as stock return volatility and conducted regression analysis using these factors.

To eliminate the influence of macroeconomic factors on the market, we include 5 year-dummy variables from 2017 to 2021. We construct the model as

$$\begin{aligned} \text{Volit} = & \beta_0 + \beta_1 \cdot \text{ESG}_{it} + \beta_2 \cdot \text{Media}_{it} + \beta_3 \cdot \text{Contral_Variable}_{1it} + \dots \\ & + \beta_n \cdot \text{Contral_Variable}_{nit} + \alpha_1 \cdot \text{Dummy_Year2017} + \alpha_2 \cdot \text{Dummy_Year2018} \quad (1) \\ & + \alpha_3 \cdot \text{Dummy_Year2019} + \alpha_4 \cdot \text{Dummy_Year2020} + \alpha_5 \cdot \text{Dummy_Year2021} \end{aligned}$$

The summary table of the regression results is listed below:

Dep. Variable:	Volatility	R-squared:	0.313
Model:	OLS	Adj. R-squared:	0.313
Method:	Least Squares	F-statistic:	500.1
Prob (F-statistic):	0.00	Log-Likelihood:	-68839.
No. Observations:	18666	AIC:	1.377e+05
Df Residuals:	18648	BIC:	1.379e+05
Df Model:	17	Covariance Type:	nonrobust

	coef	std err	t	P> t	[0.025	0.975]
constant	43.6311	0.071	616.172	0.000	43.492	43.770
beta	1.3932	0.072	19.320	0.000	1.252	1.535
ATO	-0.2619	0.072	-3.619	0.000	-0.404	-0.120
dummy audit	0.0764	0.072	1.064	0.287	-0.064	0.217
Director Ratio	0.1069	0.073	1.458	0.145	-0.037	0.250
esg score	-0.7792	0.075	-10.321	0.000	-0.927	-0.631
TopTenHoldersRate	-0.1946	0.074	-2.639	0.008	-0.339	-0.050
DA	1.5958	0.084	18.985	0.000	1.431	1.761
ROE	-0.0318	0.071	-0.446	0.656	-0.172	0.108
media	2.7373	0.085	32.266	0.000	2.571	2.904
PB Volatility	-0.1463	0.071	-2.059	0.039	-0.286	-0.007
BM	-1.9708	0.090	-21.892	0.000	-2.147	-1.794
total asset log	-4.0610	0.108	-37.618	0.000	-4.273	-3.849
dummy 2017	-4.6162	0.086	-53.558	0.000	-4.785	-4.447
dummy 2018	-1.4974	0.088	-17.109	0.000	-1.669	-1.326
dummy 2019	-2.1202	0.088	-24.209	0.000	-2.292	-1.949
dummy 2020	0.1362	0.088	1.540	0.124	-0.037	0.310
dummy 2021	0.1001	0.089	1.124	0.261	-0.074	0.275

Omnibus:	2184.723	Durbin-Watson:	1.394
Prob(Omnibus):	0.000	Jarque-Bera (JB):	6569.424
Skew:	0.623	Prob(JB):	0.00
Kurtosis:	5.625	Cond. No.	3.07

Notes:

[1] Due to the relatively small values of volatility, we multiply the volatility by 100 to better study the effects of various variables on it.

[2] To optimize the performance of the model and balance the coefficients of each term due to the significant differences in the magnitudes of the independent variables, we standardize the independent variables.

[3] For variable media, we assign zero to all the companies that have no record.

From the coefficients obtained from the regression, we find the ESG score's coefficient is negative, and the statistical value of t is very small. With the upper bound of the confidence interval less than zero, it indicates a statistically significant negative correlation between ESG and volatility.

5.2 Modified Mean-Variance Portfolio incorporating ESG

Variable	Meaning
w	Weight of the portfolio
μ	Expected return of the portfolio
γ	Risk aversion coefficient
δ	ESG preference coefficient
Σ	Covariance of portfolio
g	ESG score
g_{target}	Given target ESG score
μ_{target}	Given target expected return

Table 2: Meaning of Variables

In Table 2, we list the meaning of each variable.

5.2.1 Model: Mean-Variance meets sustainability goals

ESG assesses the sustainability of business operations and their impact on social values in three dimensions: environmental, social and corporate governance. Investors increasingly integrate ESG information into their decision-making processes. In the second part, this paper focuses on Type-M investors, characterized by their pursuit of portfolios that strike an optimal balance between high expected returns, low risk, and a consistently high average ESG score. Specifically, we address the investor's challenge of selecting a portfolio comprising N risky assets and a risk-free security. While traditional models predominantly consider the trade-off between portfolio return and risk, our enhanced model incorporates an ESG score factor into the objective function. Additionally, we introduce ESG preference coefficients to capture the influence of ESG considerations on portfolio construction.

$$\max_w \left\{ \underbrace{w^\top \mu - \frac{\gamma}{2} w^\top \Sigma w}_{\text{mean-variance}} + \underbrace{\delta \left(\frac{w^\top g}{w^\top 1} \right)}_{\text{ESG tilt}}, \text{ subject to } \begin{cases} w^\top 1 = 1 \\ 0 \leq w \leq 1 \end{cases} \right\} \quad (2)$$

In this equation, we use the average of Sino-Securities Index Information Service ESG scores of the stock in portfolios to represent ESG score factor. The ESG preference coefficient, denoted as θ , reflects the degree to which investors prioritize ESG performance. A higher θ signifies greater emphasis placed by investors on ESG criteria. The risk aversion coefficient, denoted as γ , to capture investors' attitude towards risk. Because it is not easy to short stocks in the Chinese market, the coefficients for each stock are specified to be between 0 and 1. This simplification facilitates the modeling process and ensures practical applicability within the context of the market dynamics under consideration.

5.2.2 Efficient Frontier and ESG-SR Frontier

Following the framework of the fundamental mean-variance model, we construct Efficient Frontier curves incorporating ESG factors. This attempt aims to elucidate the implications of ESG considerations on investment costs and benefits.

$$\min_w \left\{ \begin{array}{ll} w^\top 1 = 1, 0 \leq w \leq 1 & \text{basic constraint} \\ \sqrt{w^\top \Sigma w}, \text{ subject to } w^\top \mu = \mu_{\text{target}}, & \text{return constraint} \\ w^\top g = g_{\text{target}} & \text{ESG constraint} \end{array} \right\} \quad (3)$$

However, considering investment return, risk, and ESG scores simultaneously on the basic Efficient Frontier curve is difficult. In the basic Efficient Frontier curve, the tangent portfolio has the largest Sharpe rate. To visualize the impact of ESG scores on the decision-making of M investors, we aim to depict the trade-off between investment return, risk, and ESG scores graphically. According to Pedersen's study[10] (2019, p.575), investors have the ability to evaluate the trade-offs between return, risk, and ESG score independently. This suggests that the optimal trade-off between investment return and risk can be identified for specific ESG scores, utilizing the Sharpe ratio as a guiding metric to select portfolios with the highest Sharpe ratio.

$$SR(g_{\text{target}}) = \max_w \left\{ \frac{w^\top \mu}{\sqrt{w^\top \Sigma w}}, \text{ subject to } \left\{ \begin{array}{l} w^\top 1 = 1 \\ 0 \leq w \leq 1 \\ w^\top g = g_{\text{target}} \end{array} \right. \right\} \quad (4)$$

To ensure comprehensive consideration of ESG score coverage and the robustness of our findings, we partition the screened A-share stocks into 20 groups based on quartiles of their ESG scores. Subsequently, we randomly select one stock from each group, resulting in a total of 20 stocks to compose a new portfolio. By applying our formulated model, we derive the ESG-SR Frontier. Multiple iterations of random selections are conducted to generate diverse portfolios, facilitating the identification of common trends and characteristics among the resulting curves. Through this systematic approach, we aim to derive universally applicable conclusions that transcend specific stock selections and reflect broader market dynamics.

5.2.3 Effectiveness of ESG indicators

To assess the costs and benefits associated with the Environmental, Social, and Governance (ESG) indicator, we employ stock data spanning from 2009 to 2022. During this period, stocks are classified into 20 groups based on quartiles of their annual average ESG scores. Compute the weights of the corresponding portfolios separately using the modified mean-variance model.

6 Result and Discussion

6.1 Linear Regression

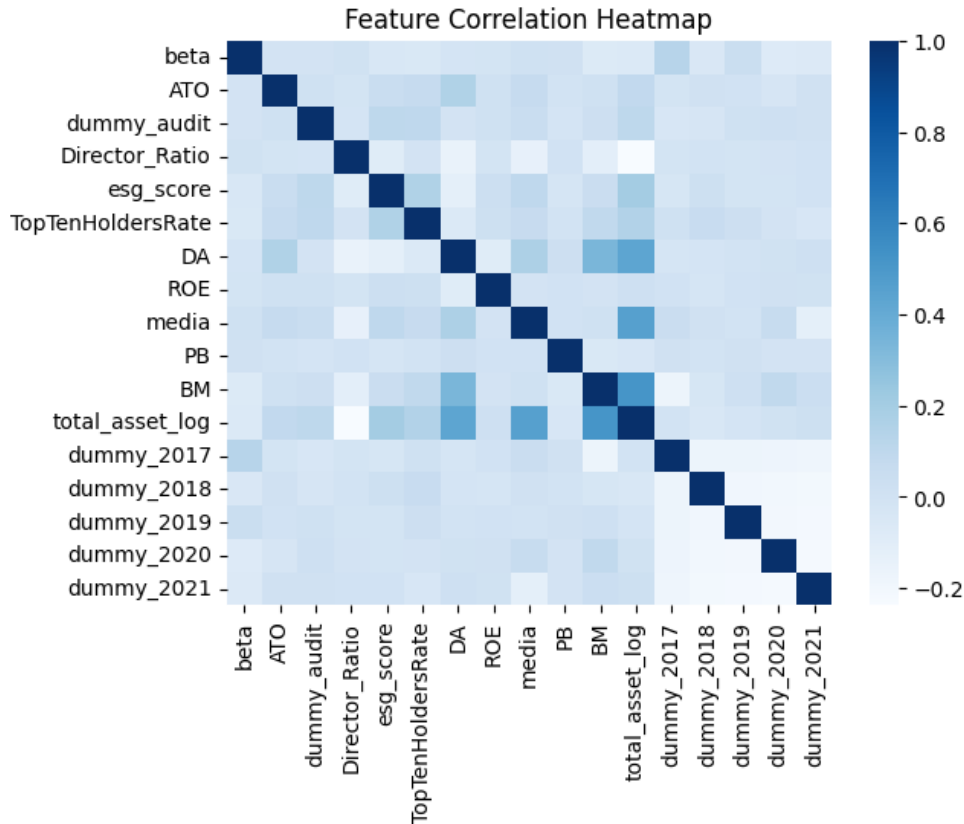


Figure 1: An example of multiple figures in one frame.

Through the independent variable correlation figure, we can see that there is relatively low collinearity among the independent variables. The advantage lies in its ability to avoid multicollinearity issues, allowing each variable to explain the variability of the target variable more independently. This contributes to enhancing the stability, interpretability, and generalization ability of the model.

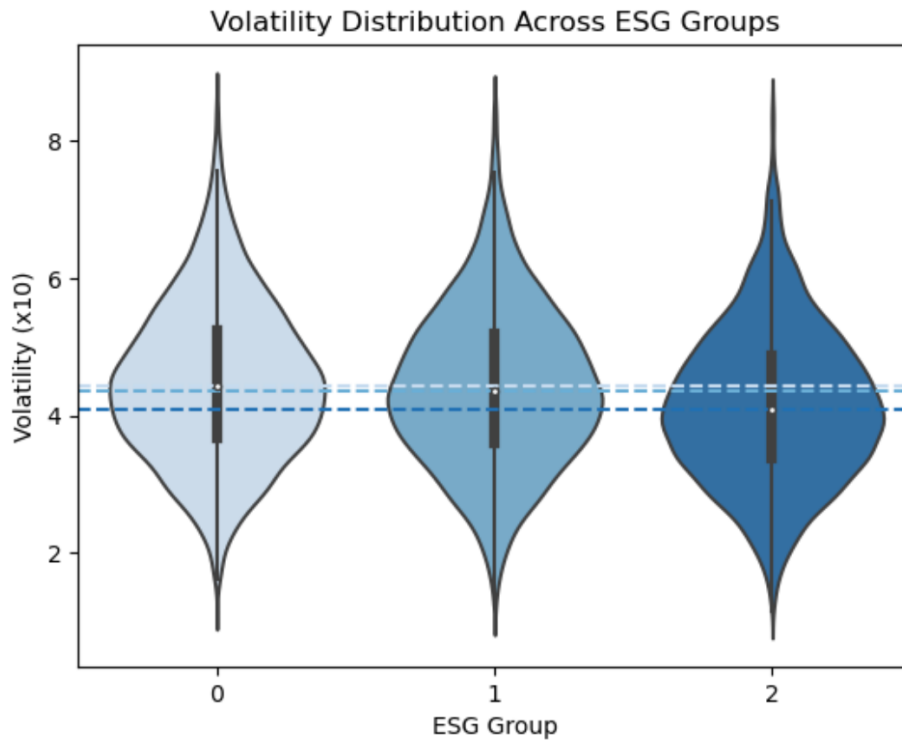


Figure 2: Feature Importance

We roughly grouped the data into three categories based on ESG scores to explore the distribution of stock return volatility within each group. The result is shown in Figure 2. It can be observed that the group with the highest ESG scores exhibits significantly lower volatility compared to the group with the lowest ESG scores. Furthermore, the group with the lowest ESG scores shows a more pronounced long and heavy tail effect in its distribution, indicating a greater number of high-volatility outliers. This further suggests that companies with lower ESG scores may experience larger stock price fluctuations and are more susceptible to idiosyncratic risks.

Therefore, we further confirmed that our OLS regression model is reliable. And from the regression result, we find that better ESG performance can exhibit significantly lower stock volatility. This finding offers the following insights:

1. For companies: From the perspective of firms, considering ESG factors in future operations can contribute to increased profitability, stability in stock prices, and enhanced market confidence. Using ESG ratings as a reference, companies can better focus on long-term development, optimize management structures, and generate higher returns while stabilizing market confidence, thus achieving optimal long-term benefits.

2. For investors: ESG scores may constitute an important factor in a stock's performance. Particularly for risk-averse investors, companies with higher ESG scores often demonstrate more sustainable business models, clear development strategies, and well-established management practices. Such companies' stock prices are proven to be more stable during long-term market fluctuations, enhancing their reliability for investors.

6.2 ESG-adjusted capital asset pricing model

Before delving into the specific findings, it is crucial to visually represent the relationship between ESG scores and stock returns. The graph spanning from 2015 to 2023 illustrates a notable increase in companies' focus on ESG, reflected in an overall upward trend in ESG scores. These scores exhibit a hump-shaped pattern concerning stock returns. A low ESG score indicates deficiencies in environmental, social, and governance practices, potentially leading to issues such as poor risk management and reputation harm. Such scores may indicate problems like environmental pollution, labor disputes, corruption, or mismanagement, heightening a firm's business risk and undermining investor confidence. Moreover, ESG-related challenges can tarnish a company's reputation, eroding consumer and investor trust in its offerings.

Conversely, excessively high ESG scores may also entail short-term drawbacks. For instance, improving ESG performance increases corporate costs and drains corporate resources. Margolis et al.[9] (2009) synthesized 251 studies on ESG and firms' financial

performance, with 214 (nearly 85%) suggesting no positive correlation between firms' financial performance and ESG. Cornell[4] (2020) concluded that environmental investment does not yield immediate profits, potentially leading to short-term stock return reductions.

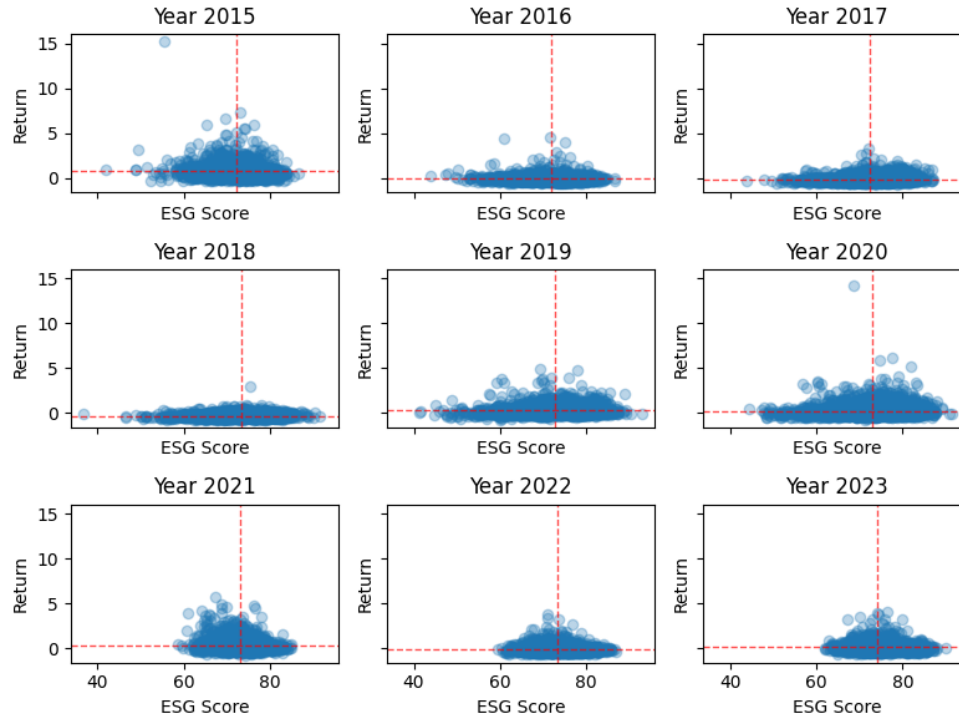


Figure 3: Visualization of relationship between ESG scores and stock returns, 2015-2017

6.2.1 Comparison of efficient frontier with/without esg constraints

The comparison of three different types of efficient frontier by using the 20 stocks of different levels of ESG is shown below.

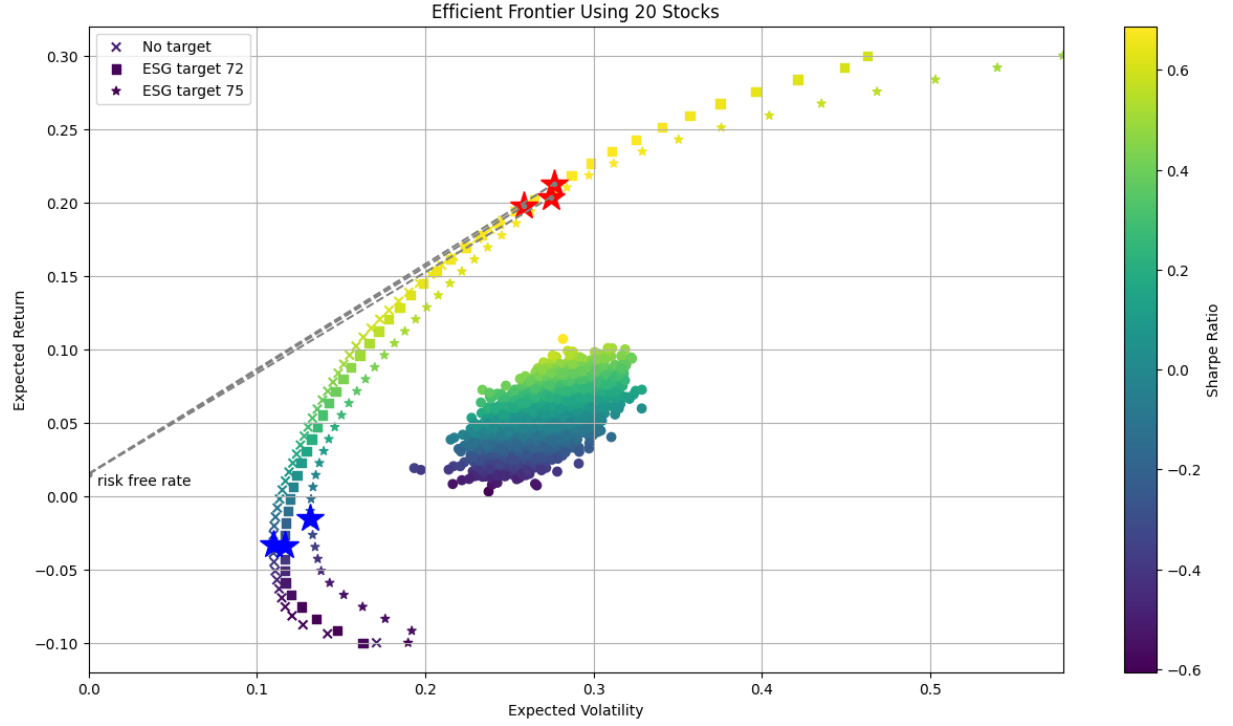


Figure 4: Efficient_frontier

Figure 4 illustrates the standard mean-variance frontier along with the associated tangent portfolio. The slope from the risk-free rate to the tangent portfolio represents the maximum Sharpe ratio (SR). This tangent portfolio is pivotal in maximizing the risk-adjusted returns given the available assets.

We delineate three distinct stylized frontiers. As investors seek heightened ESG scores, the frontier diverges from the unconstrained frontier, necessitating a trade-off wherein investors may need to reconcile potential diminution in returns and/or augmentation in volatility.

By utilizing equation 3, we can get the following result

Modification on equation 3	sharpe ratio value
No ESG constraint	0.7148029625436059
$g_{target} = 72$	0.7057171204466886
$g_{target} = 75$	0.6869058755944738

Table 3: Result of sharpe ratio of tangent portfolios

As Table 3 shows, the result is in accordance with the fact that restricting portfolios to have any ESG score other than that of the tangency portfolio must yield a lower maximum SR.

6.2.2 Analysis on ESG-SR frontier

In Figure 7, by utilizing Equation 4, for each level of ESG, we calculate the highest attainable Sharpe ratio (SR). We represent this association between ESG scores and the highest SR in terms of the ESG-SR frontier. The ESG-SR frontier is a useful way to illustrate the investment opportunity set when people care about risk, return, and ESG. (Risk and return can be summarized by the Sharpe ratio)

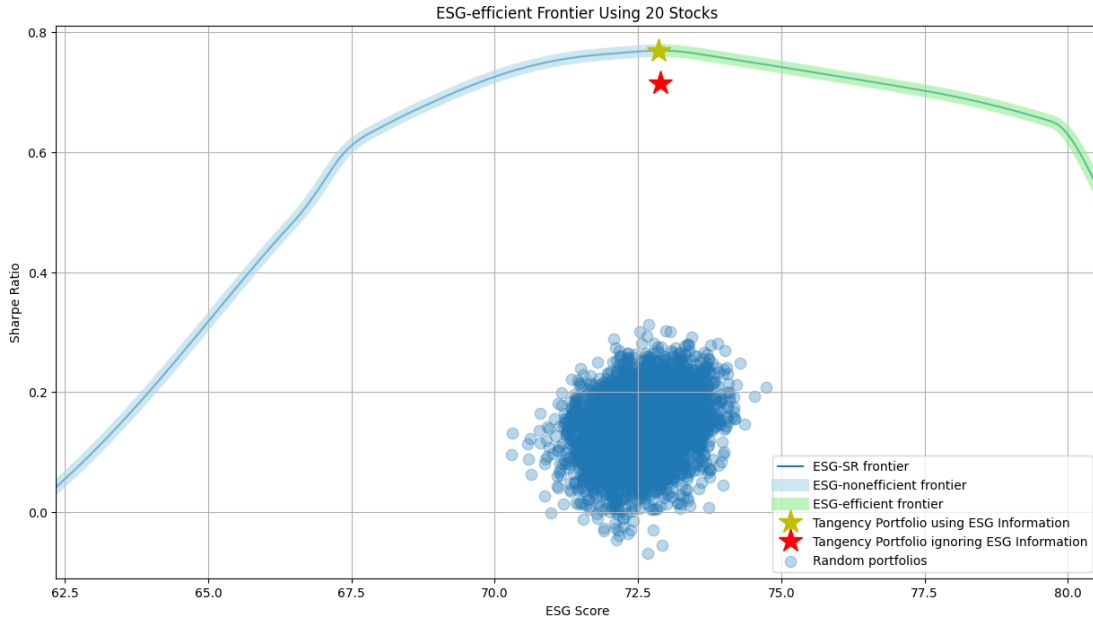


Figure 5: The ESG-SR frontier

Variable	Meaning
ESG-SR frontier	The association between ESG scores and the highest SR
ESG-nonefficient frontier	The ESG-nonefficient frontier offers investors the opportunity to enhance either their ESG scores or Sharpe ratios, or both, without sacrificing one for the other, so it is nonefficient.
ESG-efficient frontier	The ESG-efficient frontier offers optimal investment portfolios. However, due to the tradeoff between the Sharpe ratio and ESG scores, the ideal portfolio selection along this frontier varies based on one's preference for ESG criteria.
Tangency Portfolio using ESG information	The peak of the ESG-SR frontier.
Tangency Portfolio ignoring ESG information	The tangency portfolio constructed without considering ESG-related factors.
Random portfolios	Represents the relationship of sharpe ratio and ESG score among random portfolios.

Table 4: Meaning of variables in the legend of Figure 7

Tangency Portfolio Type	Using ESG information	Ignoring ESG information
ESG score	72.85803182579565	72.88156950765537
Sharpe Ratio	0.7690213207249059	0.7148029625436059
On ESG-SR frontier	True	False
On efficient-frontier without ESG constraint	False	True

Table 5: Comparison of Using/Ignoring ESG info

For diverse investor profiles, their portfolio options varies.

- Investors who prioritize both the Sharpe ratio (SR) and ESG factors should opt for a frontier portfolio positioned to the right of this portfolio on the ESG-efficient frontier,

as the ESG-SR frontier exhibits an inverted U-shape, indicating an optimal range for portfolio selection.

- Investors who lack familiarity with ESG metrics may opt for portfolios positioned below the frontier, as Table 5 shows. This decision could stem from their reliance on a tangency portfolio computation that overlooks the pertinent insights embedded within ESG scores, thus conditioning on less comprehensive information.

Maximum SR that incorporates this ESG proxy is about 7.6% higher than the maximum SR that ignores such information.

6.2.3 Effect verification of modified mean-variance model

The 2023 returns for each of the 20 sets of portfolios using the modified mean-variance model are shown below.

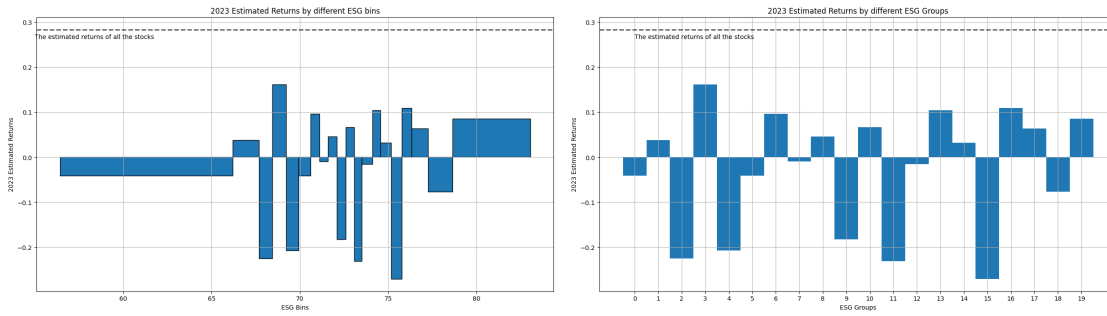


Figure 6: Returns of 20 sets portfolios

The dashed line in the figure represents the global optimal solution derived without constraining the ESG value. With an annual return of -0.037007 for the CSI in 2023, the modified mean-variance model is clearly valid. However, our analysis overlooks the impact of trading fees, restrictions on share quantities, as well as stop orders. Consequently, the calculated portfolio returns may be inflated. It is evident that the portfolio, when grouped by ESG, falls below the global optimal solution. This discrepancy arises because considering ESG performance restricts the choice to a specific range of stocks, potentially sacrificing a portion of investment returns. When grouped according to ESG, it can be seen that

portfolios with intermediate ESG scores perform slightly better. This is consistent with the previous analysis of the relationship between ESG and stock returns.

However, due to the multitude of corporate factors influencing ESG and the relative immaturity of the ESG scoring system in China, there is significant variability in the volatility among grouped stock return categories based on ESG scores. Nonetheless, ESG will become an important factor influencing investors' investment behavior, and stocks of companies with good ESG performance will have more stable long-term returns.

7 Conclusion

In this project study, we aimed to investigate the impact of corporate ESG scores on stock return volatility in China's A-share market and to enhance the Markowitz Mean-Variance Model by introducing ESG scores to study their impact on Mean-Variance investors' preferences.

Regarding our first research question, we constructed regressions, and the results confirmed that companies with higher ESG scores tend to exhibit lower stock volatility. This finding has significant implications for both companies and investors. By using ESG ratings as a reference, companies can better optimize management structures, plan for long-term development, instill confidence in the market, and investors can choose more stable strategies and construct less volatile portfolios.

Furthermore, considering the impact of ESG on volatility, we posed our second research question. We incorporated ESG performance considerations and introduced ESG tilt to adjust the Markowitz Mean-Variance Model. Generally, our study indicated that both excessively low and high ESG scores could lead an undesirable outcome. Additionally, the ESG-derived efficient frontiers demonstrated that investors need to make a sacrifice between lower returns and higher volatility when seeking higher ESG scores. Based on those findings, we provided different investing options for diverse profile investors.

In conclusion, our study provides valuable insights into the relationship between the ESG scores and stock return and volatility in China's A-share market, highlighting the

importance of considering ESG factors for both companies and investors, and proposing a mean-variance model that incorporates ESG factors for investors for consideration.

8 Limitations and Future Work

1. In exploring the regression model of ESG score's impact on individual stock volatility, we found that the feature importance of the constant term was relatively high. If there are significant biases or variances in the data, this influence may become more significant, as Figure 7 showed, indicating that our model might be affected by outliers. In the future, it may be beneficial to introduce additional factors to fully explain stock volatility, or to employ other regularization models to further reduce the variance of the constant term.

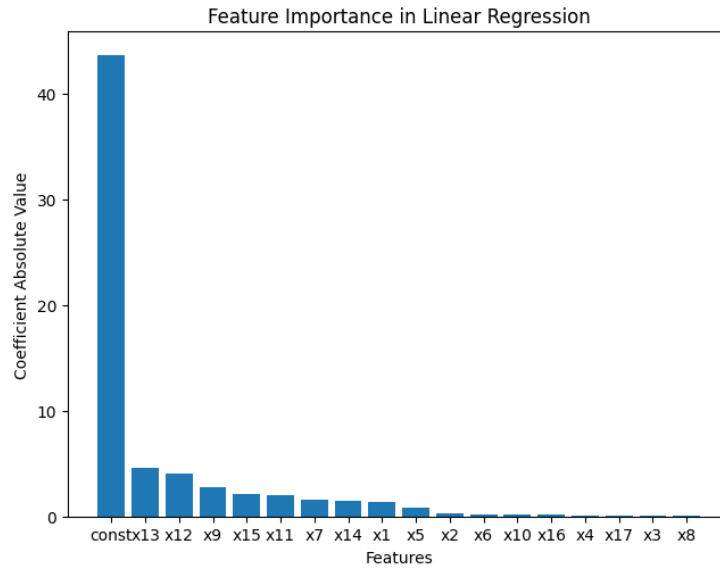


Figure 7: Feature Importance

2. We utilized the ESG ratings from Sino-Securities Index Information Service in our analysis, and the subjectivity of ESG rating agencies may have influenced the experimental results (Berg et al., 2022)[3]. Future studies might consider integrating ESG ratings from multiple agencies to mitigate rating errors and obtain more impartial results, thereby addressing the divergence of ESG ratings.



3. In constructing the Markowitz Mean-Variance Model, we simplified the model by restricting $w > 0$, i.e., we did not consider asset shorting. While short selling is often restricted but not entirely prohibited. Future research could explore introducing a lower limit L (a negative constant) on w or using $L = f(*)$ (using company information $*$ to estimate its short-selling restrictions) to develop the model and Efficient Frontiers that are more aligned with the market.

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We have developed a lightweight front-end interface tailored to deliver a user-friendly experience. Upon uploading a file, the interface seamlessly showcases the corresponding results derived from the ESG-adjusted Capital Asset Pricing Model (CAPM), which enhances user engagement and ensures accessibility to intricate financial analyses.

Figure 8: Demo of Web interface



9.2 Code

Coding for Research Question 1

```
1 import pandas as pd
2 from sklearn.linear_model import LinearRegression
3 from sklearn.preprocessing import StandardScaler
4 import statsmodels.api as sm
5 import seaborn as sns
6 import matplotlib.pyplot as plt
7 import numpy as np
8
9 # Data procession (scaling)
10 data = pd.read_excel("regression_raw_data.xlsx")
11 y = data['Volatility']*100
12 X = data.drop(columns=['Volatility'])
13 scaler = StandardScaler()
14 X_scaled = scaler.fit_transform(X)
15 X_with_const = sm.add_constant(X_scaled)
16
17 # OLS Regression
18 model_ols = sm.OLS(y, X_with_const).fit()
19
20 # Check the Coefficients
21 coefficients = model_ols.params
22 print("Coefficients:", coefficients)
23 print(model_ols.summary())
24
25 # Calculate feature correlation matrix
26 correlation_matrix = X.corr()
27
28 # Correlation Heatmap
```



```
29 sns.heatmap(correlation_matrix, annot=False, cmap='Blues')
30 plt.title('Feature Correlation Heatmap')
31 plt.show()
32
33
34 coef_abs = np.abs(model_ols.params)
35 coef_abs_sorted = coef_abs.sort_values(ascending=False)
36 plt.bar(range(len(coef_abs)), coef_abs_sorted)
37 plt.xticks(range(len(coef_abs)), coef_abs_sorted.index)
38 plt.tight_layout()
39 plt.xlabel('Features')
40 plt.ylabel('Coefficient Absolute Value')
41 plt.title('Feature Importance in Linear Regression')
42 plt.show()
43
44 colors = sns.color_palette("Blues", 3)
45
46 # Expand Volatility by 10 times
47 filtered_data = data.copy()
48 filtered_data['Volatility'] *= 10
49
50 # Calculate lower and upper bounds
51 lower_bound = filtered_data['Volatility'].quantile(0)
52 upper_bound = filtered_data['Volatility'].quantile(0.999)
53
54 # Filter data based on upper and lower bounds
55 filtered_data = filtered_data[(filtered_data['Volatility'] >= lower_bound) &
    (filtered_data['Volatility'] <= upper_bound)]
56
57
```



```
58 quantiles = [0, 0.33, 0.67, 1]
59
60 # Use a custom list of quantiles to split the data into four groups
61 filtered_data['ESG_group'] = pd.qcut(filtered_data['esg_score'], q=quantiles,
        labels=False)
62
63 # Use Seaborn to draw a violin plot and specify the color
64 ax = sns.violinplot(x='ESG_group', y='Volatility', data=filtered_data,
        palette=colors)
65 plt.xlabel('ESG Group')
66 plt.ylabel('Volatility (x10)')
67 plt.title('Volatility Distribution Across ESG Groups')
68
69 group_medians = filtered_data.groupby('ESG_group')['Volatility'].median()
```

Code for Research Question 2

```
1 import pandas as pd
2 import numpy as np
3 from scipy.optimize import minimize
4 import matplotlib.pyplot as plt
5 import scipy.interpolate as sci
6 import gradio as gr
7 import tempfile
8
9 def main(file):
10     df=pd.read_excel(file)
11     N=20
12     years = df['year'].unique()[-9:]
13
14     fig, axes = plt.subplots(3, 3, figsize=(8, 6), sharex=True,sharey=True)
```



```
15     axes = axes.flatten()
16
17     for i, year in enumerate(years):
18         data_year = df[df['year'] == year]
19         ax = axes[i]
20         ax.scatter(data_year['esg_score'], data_year['return'], alpha=0.3)
21         ax.set_title(f'Year {year}')
22         ax.set_xlabel('ESG Score')
23         ax.set_ylabel('Return')
24
25         mean_esg_score = data_year['esg_score'].mean()
26         mean_return = data_year['return'].mean()
27         ax.axhline(y=mean_return, color='red', linestyle='--', linewidth=1,
28                   alpha=0.7)
29         ax.axvline(x=mean_esg_score, color='red', linestyle='--', linewidth=1,
30                   alpha=0.7)
31
32     plt.tight_layout()
33
34     with tempfile.NamedTemporaryFile(suffix='.png', delete=False) as temp_file1:
35         plt.savefig(temp_file1.name)
36         temp_file1.close()
37         temp_file_path1 = temp_file1.name
38
39     df_pivot = df.pivot_table(index='year', columns='id', values='return')
40     df_pivot = df_pivot.dropna(axis=1)
41
42     average_esg_score_2017_2022 = df[df["year"] !=
```



```
max(df["year"])] .groupby('id')['esg_score'].mean()
43 average_esg_score_2023 = df[df['year'] ==
max(df["year"])] .groupby('id')['esg_score'].mean()
44
45
46 valid_ids = df_pivot.columns.tolist()
47 filtered_average_esg_score = average_esg_score_2017_2022.loc[valid_ids]
48 sorted_esg_score=filtered_average_esg_score.sort_values()
49
50 bins = pd.qcut(sorted_esg_score, q=N)
51
52 result = pd.DataFrame({
53     'esg_score': sorted_esg_score,
54     'quantile': bins
55 })
56
57
58 dfs = []
59 for _, group in result.groupby(bins):
60     group = group.drop(columns=['quantile'])
61     dfs.append(group)
62
63
64 sampled_df = pd.DataFrame(columns=dfs[0].columns)
65
66
67 for group_df in dfs:
68     sampled_row = group_df.sample(n=1, random_state=40)
69     sampled_df = pd.concat([sampled_df, sampled_row])
70
```



```
71     esg_score_df=sampled_df
72     esg_score_array=np.array(esg_score_df.values)
73
74     selected_columns=esg_score_df.index.to_list()
75     returns = df_pivot.loc[:, selected_columns]
76
77     risk_aversion=10
78     esg_coefficient=5/1000#2/1000
79     risk_free=0.015
80
81     returns_2017_to_2022 = returns[:-1]
82     returns_2023 = returns.tail(1)
83
84     expected_returns = returns_2017_to_2022.mean()
85     minimum_expected_return = min(expected_returns)
86     maximum_expected_return = max(expected_returns)
87     print("expected return min 20 stocks",min(expected_returns))
88     print("expected return max 20 stocks",max(expected_returns))
89     covariance_matrix = returns_2017_to_2022.cov(ddof=0)
90
91     def generate_ptfs(returns, N):
92         ptf_rs = []
93         ptf_stds = []
94         ptf_esgs=[]
95         for i in range(N):
96             weights = np.random.random(len(returns.columns))
97             weights /= np.sum(weights)
98             ptf_rs.append(np.sum(returns.mean() * weights))
99             ptf_stds.append(np.sqrt(np.dot(weights.T, np.dot(returns.cov(),
                weights))))
```



```
100         ptf_esgs.append(np.dot(esg_score_array.T,weights)/np.sum(weights))
101     ptf_rs = np.array(ptf_rs)
102     ptf_stds = np.array(ptf_stds)
103     ptf_sharpes = (ptf_rs-risk_free) / ptf_stds
104
105     return ptf_rs, ptf_stds,ptf_sharpes,ptf_esgs
106
107 def ptf_stats(weights):
108     weights = np.array(weights)
109     ptf_r = np.dot(expected_returns, weights)
110     ptf_std = np.sqrt(np.dot(weights.T, np.dot(covariance_matrix, weights)))
111     ptf_esg = (np.dot(esg_score_array.T, weights)/np.sum(weights))[0]
112     return np.array([ptf_r, ptf_std, (ptf_r - risk_free) / ptf_std, ptf_esg])
113
114 def objective_function(weights):
115     return -np.dot(expected_returns, weights) + 1/2*risk_aversion*
116         np.dot(np.dot(weights, covariance_matrix), weights)-
117         esg_coefficient*np.dot(esg_score_array.T,weights)/np.sum(weights)
118
119
120 def min_var(weights):
121     return np.sqrt(np.dot(weights, np.dot(covariance_matrix, weights)))
122
123
124 def sharpe_function(weights):
125     return -np.dot(expected_returns, weights)/np.sqrt(np.dot(np.dot(weights,
126         covariance_matrix), weights))
127
128
129 def efficient_frontier(start_r, end_r, steps):
130     target_rs = np.linspace(start_r, end_r, steps)
131     target_stds = []
132     for r in target_rs:
```




```
127         cons= ({'type': 'eq', 'fun': lambda weights:
                  np.dot(expected_returns, weights) - r},
128                {'type': 'eq', 'fun': lambda weights: np.sum(weights)-1})
129         bnds = [(0, 1)] * len(expected_returns)
130         res = minimize(min_var, x0=np.ones(len(expected_returns)) /
131                        len(expected_returns), bounds = bnds, constraints=cons)
132         target_std.append(res.fun)
133     target_std = np.array(target_std)
134     return target_rs, target_std
135
136 def efficient_frontier_with_esg(start_r, end_r, steps, esg_target_score):
137     target_rs = np.linspace(start_r, end_r, steps)
138     target_std = []
139     for r in target_rs:
140         cons= ({'type': 'eq', 'fun': lambda weights:
141                np.dot(expected_returns, weights) - r},
142                {'type': 'eq', 'fun': lambda weights: np.sum(weights)-1},
143                {'type': 'eq', 'fun': lambda weights:
144                     np.dot(esg_score_array.T,weights)/np.sum(weights)-esg_target_score})
145         bnds = [(0, 1)] * len(expected_returns)
146         res = minimize(min_var, x0=np.ones(len(expected_returns)) /
147                        len(expected_returns), bounds = bnds, constraints=cons)
148         target_std.append(res.fun)
149     target_std = np.array(target_std)
150     return target_rs, target_std
151
152 optimizer = minimize(objective_function, x0=np.ones(len(expected_returns))
153                      / len(expected_returns),
154                      bounds=[(0, 1)] *
```



```
len(expected_returns), constraints={'type': 'eq',
                                     'fun': lambda weights: np.sum(weights)-1})

151
152 mle_weights=optimizer.x
153 print("The top five weights",sorted(mle_weights)[-5:])
154 print("objective function value: ",optimizer.fun)
155 print("Status:",optimizer.success)
156
157 def portfolio_metrics_test(weights, returns):
158     portfolio_return = np.dot(weights, returns.mean())
159     return portfolio_return
160
161 print("Test sample by 2023")
162 test_returns=portfolio_metrics_test(mle_weights, returns_2023)
163 print("MLE Portfolio by all stocks - Expected Return:
        {:.4f}".format(test_returns))
164
165 def objective_function_group_return(weights,return_df,esg_score_array):
166     return -np.dot(return_df.mean(), weights) + 1/2*risk_aversion*
        np.dot(np.dot(weights, return_df.cov(ddof=0)), weights)-
        esg_coefficient*np.dot(esg_score_array.T,weights)/np.sum(weights)
167
168
169 test_returns_group=[]
170 for index,df in enumerate(dfs):
171     esg_score_array_group=np.array(df.values) #128
172     selected_columns_group=df.index.to_list()
173     returns_group = df.pivot.loc[:, selected_columns_group]
174     returns_group_2017_to_2022=returns_group[:-1]
175     returns_group_2023=returns_group.tail(1)
```



```
176     expected_returns_group_2017_to_2022=returns_group_2017_to_2022.mean()
177
178     optimizer_group = minimize(objective_function_group_return,
179                                x0=np.ones(len(expected_returns_group_2017_to_2022)) /
180                                len(expected_returns_group_2017_to_2022),
181                                args=(returns_group_2017_to_2022,esg_score_array_group),
182                                bounds=[(0, 1)] *
183                                len(expected_returns_group_2017_to_2022),constraints={'type':
184                                'eq', 'fun': lambda weights: np.sum(weights)-1})
185
186     mle_weights_group=optimizer_group.x
187
188     test_returns_group.append(portfolio_metrics_test(mle_weights_group,
189                                                       returns_group_2023))
190
191     print("Test sample by 2023 (group {})".format(index))
192     print("MLE Portfolio by all stocks - Expected Return:
193           {:.4f}".format(portfolio_metrics_test(mle_weights_group,
194                                                   returns_group_2023)))
195
196     bin_upper_limits = np.array(sorted([interval.right for interval in
197                                         set(bins.values)]))
198     bin_lower_limits = np.array(sorted([interval.left for interval in
199                                         set(bins.values)]))
200     print(bin_lower_limits)
201     print(bin_upper_limits)
202     plt.figure(figsize=(15,8))
```



```
197     plt.grid(True)
198     plt.axhline(y=test_returns, color='black', linestyle='--', linewidth=2,
199               alpha=0.7)
200     plt.text(56, test_returns-0.01, 'The estimated returns of all the stocks',
201             verticalalignment='top', horizontalalignment='left')
202     plt.bar(bin_lower_limits, test_returns_group,
203            width=(bin_upper_limits-bin_lower_limits), align='edge',
204            edgecolor='black')
205
206     plt.xlabel('ESG Bins')
207     plt.ylabel('2023 Estimated Returns')
208     plt.title('2023 Estimated Returns by different ESG bins')
209
210
211
212     with tempfile.NamedTemporaryFile(suffix='.png', delete=False) as temp_file2:
213         plt.savefig(temp_file2.name)
214         temp_file2.close()
215         temp_file_path2 = temp_file2.name
216
217
218     plt.figure(figsize=(15,8))
219     plt.grid(True)
220     plt.axhline(y=test_returns, color='black', linestyle='--', linewidth=2,
221               alpha=0.7)
222     plt.text(0, test_returns-0.01, 'The estimated returns of all the stocks',
223             verticalalignment='top', horizontalalignment='left')
224     # plt.bar(bin_lower_limits, test_returns_group,
225            width=(bin_upper_limits-bin_lower_limits), align='edge',
226            edgecolor='black')
227
228     x_values = range(len(test_returns_group))
```



```
219     y_values = test_returns_group
220
221     plt.bar(x_values, y_values, width=1)
222     plt.xlabel('ESG Groups')
223     plt.ylabel('2023 Estimated Returns')
224     plt.title('2023 Estimated Returns by different ESG Groups')
225     plt.xticks(x_values, x_values)
226
227
228     with tempfile.NamedTemporaryFile(suffix='.png', delete=False) as temp_file3:
229         plt.savefig(temp_file3.name)
230         temp_file3.close()
231         temp_file_path3 = temp_file3.name
232
233
234     ptf_rs, ptf_stds, ptf_sharpes, ptf_esgs=
235         generate_ptfs(returns_2017_to_2022, 5000)
236
237
238     plt.figure(figsize=(15, 8))
239     plt.scatter(ptf_stds, ptf_rs, c=ptf_sharpes, marker='o')
240     plt.grid(True)
241     plt.xlabel('Expected Volatility')
242     plt.ylabel('Expected Return')
243     plt.colorbar(label='Sharpe Ratio')
244     plt.title('5000 Randomly Generated Portfolios In The Risk-Return Space')
245
246     with tempfile.NamedTemporaryFile(suffix='.png', delete=False) as temp_file4:
247         plt.savefig(temp_file4.name)
248         temp_file4.close()
```



```
248     temp_file_path4 = temp_file4.name
249
250
251
252     opts = minimize(sharpe_function, x0=np.ones(len(expected_returns)) /
253                   len(expected_returns),
254                   bounds=[(0, 1)] * len(expected_returns), constraints=[
255                       {'type': 'eq', 'fun': lambda weights: np.sum(weights)
256                         - 1},
257                   ])
258
259     opts_72 = minimize(sharpe_function, x0=np.ones(len(expected_returns)) /
260                   len(expected_returns),
261                   bounds=[(0, 1)] * len(expected_returns), constraints=[
262                       {'type': 'eq', 'fun': lambda weights:
263                         np.sum(weights) - 1},
264                       {'type': 'eq', 'fun': lambda weights:
265                         np.dot(esg_score_array.T, weights) - 72},
266                   ])
267
268     opts_75 = minimize(sharpe_function, x0=np.ones(len(expected_returns)) /
269                   len(expected_returns),
270                   bounds=[(0, 1)] * len(expected_returns), constraints=[
271                       {'type': 'eq', 'fun': lambda weights:
272                         np.sum(weights) - 1},
273                       {'type': 'eq', 'fun': lambda weights:
274                         np.dot(esg_score_array.T, weights) - 75},
275                   ])
```



```
270     opt_var = minimize(min_var, x0=np.ones(len(expected_returns)) /
        len(expected_returns),
271                        bounds=[(0, 1)] * len(expected_returns), constraints=[
272                            {'type': 'eq', 'fun': lambda weights:
                                np.sum(weights) - 1},
273                        ])
274
275
276     opt_var_72 = minimize(min_var, x0=np.ones(len(expected_returns)) /
        len(expected_returns),
277                        bounds=[(0, 1)] * len(expected_returns), constraints=[
278                            {'type': 'eq', 'fun': lambda weights:
                                np.sum(weights) - 1},
279                            {'type': 'eq', 'fun': lambda weights:
                                np.dot(esg_score_array.T, weights) - 72}],)
280
281
282     opt_var_75 = minimize(min_var, x0=np.ones(len(expected_returns)) /
        len(expected_returns),
283                        bounds=[(0, 1)] * len(expected_returns), constraints=[
284                            {'type': 'eq', 'fun': lambda weights:
                                np.sum(weights) - 1},
285                            {'type': 'eq', 'fun': lambda weights:
                                np.dot(esg_score_array.T, weights) - 75}], )
286
287     target_rs, target_stds = efficient_frontier(minimum_expected_return,
        maximum_expected_return, 50)
288     target_rs_esg_72, target_stds_esg_72 =
        efficient_frontier_with_esg(minimum_expected_return,
        maximum_expected_return, 50, 72)
```



```
289 target_rs_esg_75,target_stds_esg_75 =
    efficient_frontier_with_esg(minimum_expected_return,
    maximum_expected_return, 50, 75)

290
291 plt.figure(figsize=(15, 8))
292 plt.scatter(ptf_stds, ptf_rs, c=(ptf_rs - risk_free)/ptf_stds, marker='o')
293 plt.scatter(target_stds, target_rs, c=(target_rs - risk_free)/target_stds,
    marker='x',label='No target')
294 plt.scatter(target_stds_esg_72, target_rs_esg_72, c=(target_rs_esg_72 -
    risk_free)/target_stds_esg_72, marker=',',label="ESG target 72")
295 plt.scatter(target_stds_esg_75, target_rs_esg_75, c=(target_rs_esg_75 -
    risk_free)/target_stds_esg_75, marker='*',label="ESG target 75")
296
297 plt.plot(ptf_stats(opts['x'])[1], ptf_stats(opts['x'])[0], 'r*',
    markersize=20.0)
298 plt.plot(ptf_stats(opts_72['x'])[1], ptf_stats(opts_72['x'])[0], 'r*',
    markersize=20.0)
299 plt.plot(ptf_stats(opts_75['x'])[1], ptf_stats(opts_75['x'])[0], 'r*',
    markersize=20.0)
300
301 plt.plot(ptf_stats(opt_var['x'])[1], ptf_stats(opt_var['x'])[0], 'b*',
    markersize=20.0)
302 plt.plot(ptf_stats(opt_var_72['x'])[1], ptf_stats(opt_var_72['x'])[0],
    'b*', markersize=20.0)
303 plt.plot(ptf_stats(opt_var_75['x'])[1], ptf_stats(opt_var_75['x'])[0],
    'b*', markersize=20.0)
304
305 plt.plot([0, ptf_stats(opts["x"])[1]], [risk_free,
    ptf_stats(opts["x"])[0]], linestyle='--', color='grey',marker='.')
306 plt.plot([0, ptf_stats(opts_72["x"])[1]], [risk_free,
```




```
ptf_stats(opts_72["x"])[0]], linestyle='--', color='grey',marker='.')
307 plt.plot([0, ptf_stats(opts_75["x"])[1]], [risk_free,
      ptf_stats(opts_75["x"])[0]], linestyle='--', color='grey',marker='.')
308
309
310 print("Sharpe values of tangent
      portfolios",ptf_stats(opts["x"])[2],ptf_stats(opts_72["x"])[2],
311      ptf_stats(opts_75["x"])[2])
312 plt.text(0+0.005, risk_free, 'risk free rate', verticalalignment='top',
      horizontalalignment='left')
313
314 plt.grid(True)
315 plt.legend()
316 plt.xlabel('Expected Volatility')
317 plt.ylabel('Expected Return')
318 plt.xlim(0, max(target_stds_esg_75))
319 plt.colorbar(label='Sharpe Ratio')
320 plt.title('Efficient Frontier Using {} Stocks'.format(N))
321
322 with tempfile.NamedTemporaryFile(suffix='.png', delete=False) as temp_file5:
323     plt.savefig(temp_file5.name)
324     temp_file5.close()
325     temp_file_path5 = temp_file5.name
326
327
328
329 x_lower = min(esg_score_array)[0]
330 x_upper = max(esg_score_array)[0]
331 x_range = np.linspace(x_lower, x_upper, 200)
332 print(x_lower)
```



```
333     print(x_upper)
334     # esg_target_val=60
335
336     sharpe_list=[]
337     for x in x_range:
338         optimizer = minimize(sharpe_function, x0=np.ones(len(expected_returns))
339                               / len(expected_returns),
340                               bounds=[(0, 1)] * len(expected_returns), constraints=[
341                                   {'type': 'eq', 'fun': lambda weights:
342                                     np.sum(weights) - 1},
343                                   {'type': 'eq', 'fun': lambda weights:
344                                     np.dot(esg_score_array.T, weights)-x},
345                               ])
346
347         sharpe_list.append(-optimizer.fun)
348
349     max_sharpe_index = sharpe_list.index(max(sharpe_list))
350     max_sharpe = max(sharpe_list)
351
352     plt.figure(figsize=(15, 8))
353
354     plt.plot(x_range, sharpe_list, label="ESG-SR frontier")
355     plt.plot(x_range[:max_sharpe_index+1], sharpe_list[:max_sharpe_index+1],
356              linewidth=10, alpha=0.6, color='lightblue', label="ESG-nonefficient
357              frontier")
358     plt.plot(x_range[max_sharpe_index+1:], sharpe_list[max_sharpe_index+1:],
359              linewidth=10, alpha=0.6, color='lightgreen', label="ESG-efficient
360              frontier ")
361
362     plt.plot(x_range[max_sharpe_index], max_sharpe, 'y*',
363              markersize=20.0, label="Tangency Portfolio using ESG Information")
364
```



```
355 plt.plot(ptf_stats(opts['x'])[3], ptf_stats(opts['x'])[2], 'r*',  
           markersize=20.0, label="Tangency Portfolio ignoring ESG Information")  
356 plt.grid(True)  
357 plt.xlabel('ESG Score')  
358 plt.ylabel('Sharpe Ratio')  
359 plt.xlim(min(x_range), max(x_range))  
360 plt.scatter(ptf_esgs, ptf_sharpes, s=80, alpha=0.3, marker='o', label="Random  
    portfolios")  
361 plt.legend()  
362 plt.title('ESG-efficient Frontier Using {} Stocks'.format(N))  
363 print("with ERG information", x_range[max_sharpe_index], max_sharpe)  
364 print("without ERG information", ptf_stats(opts['x'])[3],  
       ptf_stats(opts['x'])[2])  
365  
366 with tempfile.NamedTemporaryFile(suffix='.png', delete=False) as temp_file6:  
367     plt.savefig(temp_file6.name)  
368     temp_file6.close()  
369     temp_file_path6 = temp_file6.name  
370  
371     return temp_file_path1, temp_file_path4, temp_file_path5,  
372            temp_file_path6, temp_file_path2, temp_file_path3  
373  
374  
375 gr.Interface(  
376     main,  
377     inputs="file",  
378     outputs=gr.Gallery(),  
379     title="Mean-Variance Optimization including ESG Information",  
380     description="Upload an Excel or CSV file and get the DataFrame. The file  
    should have columns ['id', 'year', 'esg_score', 'return']").launch()
```