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CSE 252A Computer Vision I Fall 2019 - Homework 1
          Instructor: Ben Ochoa
          Assignment Published On: Tuesday, October 1, 2019
          Due On: Tuesday, October 8, 2019 11:59 pm
          Instructions
           · Review the academic integrity and collaboration policies on the course website.

    This assignment must be completed individually.

    All solutions must be written in this notebook

           • Programming aspects of this assignment must be completed using Python in this notebook.
           • If you want to modify the skeleton code, you can do so. This has been provided just to provide you with a framework for the solution.
           • You may use python packages for basic linear algebra (you can use numpy or scipy for basic operations), but you may not use packages that directly
             solve the problem.
           • If you are unsure about using a specific package or function, then ask the instructor and teaching assistants for clarification.
           • You must submit this notebook exported as a pdf. You must also submit this notebook as .ipynb file.
           • You must submit both files (.pdf and .ipynb) on Gradescope. You must mark each problem on Gradescope in the pdf.

    It is highly recommended that you begin working on this assignment early.

           • Late policy - Assignments submitted late will receive a 15% grade reduction for each 12 hours late (i.e., 30% per day). Assignments will not be accepted
             72 hours after the due date. If you require an extension (for personal reasons only) to a due date, you must request one as far in advance as possible.
             Extensions requested close to or after the due date will only be granted for clear emergencies or clearly unforeseeable circumstances.
          Welcome to CSE252A Computer Vision I! This course gives you a comprehensive introduction to computer vison providing broad coverage including low level
          vision, inferring 3D properties from images, and object recognition. We will be using a variety of tools in this class that will require some initial configuration. To
          ensure smooth progress, we will setup the majority of the tools to be used in this course in this assignment. You will also practice some basic image
          manipulation techniques. Finally, you will need to export this lpython notebook as pdf and submit it to Gradescope along with .ipynb file before the due date.
          Piazza, Gradescope and Python
          Piazza
          Go to Piazza and sign up for the class using your ucsd.edu email account. You'll be able to ask the professor, the TAs and your classmates questions on
          Piazza. Class announcements will be made using Piazza, so make sure you check your email or Piazza frequently.
          Gradescope
          See Piazza post on how to add CSE 252A in Gradescope. All the assignments are required to be submitted to gradescope for grading. Make sure that you
          mark each page for different problems.
          Python
          We will use the Python programming language for all assignments in this course, with a few popular libraries (numpy, matplotlib). Assignments will be given in
          the format of browser-based Jupyter/Ipython notebook that you are currently viewing. We expect that many of you have some experience with Python and
          Numpy. And if you have previous knowledge in Matlab, check out the <u>numpy for Matlab users</u> page. The section below will serve as a quick introduction to
          Numpy and some other libraries.
          Getting started with Numpy
          Numpy is the fundamental package for scientific computing with Python. It provides a powerful N-dimensional array object and functions for working with these
          arrays.
          Arrays
In [1]: import numpy as np
          array1d = np.array([1,0,0])
                                                 # a 1d array
          print("1d array :")
          print(array1d)
          print("Shape :", array1d.shape)
                                                # print the shape of array
          array2d = np.array([[1], [2], [3]]) # a 2d array
          print("\n2d array :")
          print(array2d)
          print("Shape :", array2d.shape)
                                              # print the size of v, notice the difference
          print("\nTranspose 2d :", array2d.T)
                                                     # Transpose of a 2d array
          print("Shape :", array2d.T.shape)
          print("\nTranspose 1d :", array1d.T)
                                                     # Notice how 1d array did not change after transpose (Thoughts?)
          print("Shape :", array1d.T.shape)
          allzeros = np.zeros([2, 3])
                                                  # a 2x3 array of zeros
          allones = np.ones([1, 3])
                                                  # a 1x3 array of ones
          identity = np.eye(3)
                                                  # identity matrix
          rand3 1 = np.random.rand(3, 1)
                                                 # random matrix with values in [0, 1]
          arr = np.ones(allones.shape) * 3
                                                   # create a matrix from shape
          1d array :
          [1 0 0]
         Shape : (3,)
          2d array:
          [[1]
           [2]
           [3]]
          Shape : (3, 1)
          Transpose 2d : [[1 2 3]]
          Shape : (1, 3)
          Transpose 1d : [1 0 0]
          Shape : (3,)
          Array Indexing
In [2]: import numpy as np
          array2d = np.array([[1, 2, 3], [4, 5, 6]]) # create a 2d array with shape (2, 3)
          print("Access a single element")
          print(array2d[0, 2])
                                                 # access an element
          array2d[0, 2] = 252
                                                         # a slice of an array is a view into the same data;
          print("\nModified a single element")
                                                         # this will modify the original array
          print(array2d)
          print("\nAccess a subarray")
          print(array2d[1, :])
                                                         # access a row (to 1d array)
          print(array2d[1:, :])
                                                         # access a row (to 2d array)
          print("\nTranspose a subarray")
          print(array2d[1, :].T)
                                                         # notice the difference of the dimension of resulting array
          print(array2d[1:, :].T)
                                                         # this will be helpful if you want to transpose it later
          # Boolean array indexing
          # Given a array m, create a new array with values equal to m
          # if they are greater than 0, and equal to 0 if they less than or equal 0
          array2d = np.array([[3, 5, -2], [50, -1, 0]])
          arr = np.zeros(array2d.shape)
          arr[array2d > 0] = array2d[array2d > 0]
          print("\nBoolean array indexing")
          print(arr)
          Access a single element
          Modified a single element
          [[ 1 2 252]
          [ 4 5 6]]
          Access a subarray
          [4 5 6]
          [[4 5 6]]
          Transpose a subarray
          [4 5 6]
          [[4]
           [5]
           [6]]
          Boolean array indexing
          [[ 3. 5. 0.]
          [50. 0. 0.]]
          Operations on array
          Elementwise Operations
In [3]: import numpy as np
         a = np.array([[1, 2, 3], [2, 3, 4]], dtype=np.float64)
                                                                     # scalar multiplication
          print(a * 2)
          print(a / 4)
                                                                     # scalar division
          print(np.round(a / 4))
          print(np.power(a, 2))
          print(np.log(a))
          b = np.array([[5, 6, 7], [5, 7, 8]], dtype=np.float64)
         print(a + b)
                                                                     # elementwise sum
          print(a - b)
                                                                     # elementwise difference
          print(a * b)
                                                                      # elementwise product
          print(a / b)
                                                                      # elementwise division
         [[2. 4. 6.]
          [4. 6. 8.]]
          [[0.25 0.5 0.75]
          [0.5 0.75 1. ]]
          [[0. 0. 1.]
          [0. 1. 1.]]
          [[ 1. 4. 9.]
          [ 4. 9. 16.]]
                       0.69314718 1.09861229]
          .0]]
          [0.69314718 1.09861229 1.38629436]]
          [[ 6. 8. 10.]
          [ 7. 10. 12.]]
          [[-4. -4. -4.]
          [-3. -4. -4.]
          [[ 5. 12. 21.]
          [10. 21. 32.]]
                       0.33333333 0.42857143]
          [[0.2
           [0.4
                       0.42857143 0.5
          Vector Operations
In [4]: import numpy as np
          a = np.array([[1, 2], [3, 4]])
          print("sum of array")
                                            # sum of all array elements
          print(np.sum(a))
                                            # sum of each column
          print(np.sum(a, axis=0))
                                            # sum of each row
          print(np.sum(a, axis=1))
          print("\nmean of array")
          print(np.mean(a))
                                            # mean of all array elements
         print(np.mean(a, axis=0))
                                            # mean of each column
          print(np.mean(a, axis=1))
                                            # mean of each row
          sum of array
          10
          [4 6]
          [3 7]
          mean of array
          2.5
          [2. 3.]
          [1.5 3.5]
          Matrix Operations
In [5]: import numpy as np
          a = np.array([[1, 2], [3, 4]])
          b = np.array([[5, 6], [7, 8]])
          print("matrix-matrix product")
          print(a.dot(b))
                                            # matrix product
          print(a.T.dot(b.T))
          x = np.array([1, 2])
          print("\nmatrix-vector product")
                                           # matrix / vector product
          print(a.dot(x))
          print(a@x) # Can also make use of the @ instad of .dot()
          matrix-matrix product
          [[19 22]
          [43 50]]
          [[23 31]
          [34 46]]
          matrix-vector product
          [ 5 11]
          [ 5 11]
         Matplotlib
          Matplotlib is a plotting library. We will use it to show the result in this assignment.
 In [6]: # this line prepares IPython for working with matplotlib
          %matplotlib inline
          import numpy as np
          import matplotlib.pyplot as plt
          import math
          x = np.arange(-24, 24) / 24. * math.pi
          plt.plot(x, np.sin(x))
         plt.xlabel('radians')
          plt.ylabel('sin value')
         plt.title('Sine Function')
          plt.show()
                                  Sine Function
              1.00
              0.75
              0.50
              0.25
              0.00
             -0.25
             -0.50
             -0.75
             -1.00
                    -3
          This brief overview introduces many basic functions from a few popular libraries, but is far from complete. Check out the documentations for Numpy and
          Matplotlib to find out more.
         Problem 1 Image operations and vectorization (1pt)
          Vector operations using numpy can offer a significant speedup over doing an operation iteratively on an image. The problem below will demonstrate the time it
          takes for both approaches to change the color of quadrants of an image.
          The problem reads an image "Lenna.png" that you will find in the assignment folder. Two functions are then provided as different approaches for doing an
          operation on the image.
          Your task is to follow through the code and fill in the "piazza" function using instructions on Piazza.
In [7]: import numpy as np
          import matplotlib.pyplot as plt
          import copy
          import time
          img = plt.imread('Lenna.png')
                                                      # read a JPEG image
          print("Image shape", img.shape)
                                                      # print image size and color depth
                                                       # displaying the original image
          plt.imshow(img)
          plt.show()
          Image shape (512, 512, 3)
           100
           200
           300
                        200
In [8]: def iterative(img):
              image = copy.deepcopy(img)
                                                         # create a copy of the image matrix
              for x in range(image.shape[0]):
                  for y in range(image.shape[1]):
                      if x < image.shape[0]/2 and y < image.shape[1]/2:
                           image[x,y] = image[x,y] * [0,1,1] #removing the red channel
                       elif x > image.shape[0]/2 and y < image.shape[1]/2:</pre>
                           image[x,y] = image[x,y] * [1,0,1] #removing the green channel
                       elif x < image.shape[0]/2 and y > image.shape[1]/2:
                           image[x,y] = image[x,y] * [1,1,0] #removing the blue channel
                       else:
                           pass
              return image
          def vectorized(img):
              image = copy.deepcopy(img)
              a = int(image.shape[0]/2)
              b = int(image.shape[1]/2)
              image[:a,:b] = image[:a,:b]*[0,1,1]
              image[a:,:b] = image[a:,:b]*[1,0,1]
              image[:a,b:] = image[:a,b:]*[1,1,0]
              return image
 In [9]: # # The code for this problem is posted on Piazza. Sign up for the course if you have not. Then find
          # # the function definition included in the post 'Welcome to CSE252A' to complete this problem.
          # # This is the only cell you need to edit for this problem.
          def piazza():
              start = time.time()
              image_iterative = iterative(img)
              end = time.time()
              print("Iterative method took {0} seconds".format(end-start))
             start = time.time()
              image_vectorized = vectorized(img)
              end = time.time()
              print("Vectorized method took {0} seconds".format(end-start))
              return image_iterative, image_vectorized
          # Run the function
          image_iterative, image_vectorized = piazza()
          Iterative method took 2.140733242034912 seconds
          Vectorized method took 0.018352031707763672 seconds
In [10]: # Plotting the results in sepearate subplots
          plt.subplot(1, 3, 1) # create (1x3) subplots, indexing from 1
          plt.imshow(img)
                            # original image
          plt.subplot(1, 3, 2)
          plt.imshow(image_iterative)
          plt.subplot(1, 3, 3)
          plt.imshow(image_vectorized)
          plt.show()
                                #displays the subplots
          plt.imsave("multicolor_Lenna.png",image_vectorized)
                                                                    #Saving an image
          Problem 2 Further Image Manipulation (7pts)
         In this problem you will solve a jigsaw puzzle using the 'jigsaw.png' provided with the homework. The solution of this jigsaw is the Lenna image we used
          above. There are a total of 16 jigsaw pieces of size 128x128x3 which together make up the 512x512x3 image. Not only is Lemma jumbled spatially, but some
          of the channels in jigsaw pieces are also permuted i.e. RGB to BGR and GRB.
          Your task is to put all the pieces to their respective locations and correct the channel permutations. To achieve this task, you are required to complete the three
          helper functions that will be used to solve this puzzle. You are NOT allowed to use any function other than the three provided here. Also, the code needs to be
          vectorised i.e. you are NOT allowed to use for loops to achieve this task.
In [66]: def getTile(jigsaw, tile_idx):
              This function returns a particular jigsaw piece
              jigsaw : 512x512x3 np.ndarray
              tile_idx : tuple containing the (i,j) location of the piece
              piece
                     : 128x128x3 np.ndarray
              assert isinstance(tile_idx,tuple), 'tile index must be a tuple'
              assert len(tile_idx) == 2, 'tile index must specify the row and column index of the jigsaw'
              # Write your code here
              piece = np.zeros((128,128,3)) # modify piece
              piece = jigsaw[tile_idx[0]*128: (tile_idx[0]+1)*128, tile_idx[1]*128: (tile_idx[1]+1)*128,:3]
              return piece.copy()
          def permuteChannels(tile, permutation):
              This function performs a permutation on channel
                           : 128x128x3 np.ndarray
              permutation : tuple containing (i,j,k) channel indices
              tile_permuted : 128x128x3 np.ndarray
              assert tile.shape == (128,128,3), 'tile size should be 128x128x3'
              assert isinstance(permutation, tuple), 'permutation should be a tuple'
              assert len(permutation) == 3, 'There are only 3 channels'
              #Write your code here
              tile[:,:,[permutation[0],permutation[1],permutation[2]]]=tile[:,:,[0,1,2]]
              tile_permuted = tile.copy()
              return tile_permuted.copy()
          def putTile(board, tile, tile_idx):
              This function put a jigsaw piece at a particular location on the board
              board: 512x512x3 np.ndarray
              tile: 128x128x3 np.ndarray
              tile_idx : tuple containing the (i,j) location of the piece
              img : 512x512x3 np.ndarray
              assert board.shape == (512,512,3), 'canvas size should be 512x512x3'
              assert tile.shape == (128,128,3), 'tile size should be 128x128x3'
              assert isinstance(tile_idx, tuple), 'tile index must be a tuple'
              assert len(tile_idx) == 2, 'tile index must specify the row and column index of the jigsaw'
              # Write your own code here
              img = board.copy() # modify img
              img[tile_idx[0]*128:(1+tile_idx[0])*128, tile_idx[1]*128:(1+tile_idx[1])*128, 0:] = tile
              return img
          TILE_SIZE = 128
          source = [(0,0),(0,1),(0,2),(0,3),
                     (1,0),(1,1),(1,2),(1,3),
                     (2,0), (2,1), (2,2), (2,3),
                     (3,0), (3,1), (3,2), (3,3)
          # Fill in the target list with the corresponding piece locations
          target = [(0,2),(2,1),(1,0),(2,2),
                     (1,2),(0,0),(3,2),(0,3),
                     (2,0),(3,0),(0,1),(3,1),
                     (3,3),(1,3),(1,1),(2,3)
          #Fill in the respective channel permutations
          channelPermutation = [(2,1,0),(0,1,2),(1,0,2),(2,1,0),
                                 (0,1,2), (0,1,2), (1,0,2), (2,1,0),
                                 (1,0,2),(0,1,2),(0,1,2),(2,1,0),
                                 (0,1,2), (0,1,2), (0,1,2), (1,0,2)
          jigsaw = plt.imread('jigsaw.png')
          board = np.ones(jigsaw.shape)
          for i in range(16):
              tile = getTile(jigsaw, source[i])
              tile = permuteChannels(tile, channelPermutation[i])
              board = putTile(board, tile, target[i])
          print("Jigsaw Puzzle")
          plt.imshow(jigsaw)
          plt.show()
         print("Solution")
          plt.imshow(board)
         plt.show()
          Jigsaw Puzzle
```

200 300 400

100

Solution

100

200

300