Name: Yangchen Ye (yye02) Assignment: Project 3: Queue the Stacking of the Deque Date Submitted: Sunday, March 17, 2019 11:44:42 AM EDT Current Grade: Needs Grading Submission Field: There is no student submission text data for this assignment. Comments: There are no student comments for this assignment. Original filename: Stack.py Filename: Project 3 Queue the Stacking of the Deque yye02 attempt 2019-03-17-11-44-42 Stack.py Original filename: Linked List Deque.py Filename: Project 3 Queue the Stacking of the Deque yye02 attempt 2019-03-17-11-44-42 Linked List Deque.py Original filename: Linked List.py Filename: Project 3 Queue the Stacking of the Deque yye02 attempt 2019-03-17-11-44-42 Linked List.py Original filename: Delimiter Check.py Filename: Project 3 Queue the Stacking of the Deque yye02 attempt 2019-03-17-11-44-42 Delimiter Check.py Original filename: Queue.py Filename: Project 3 Queue the Stacking of the Deque yye02 attempt 2019-03-17-11-44-42 Queue.py Original filename: Writeup.pdf Filename: Project 3 Queue the Stacking of the Deque yye02 attempt 2019-03-17-11-44-42 Writeup.pdf Original filename: Hanoi.py Filename: Project 3 Queue the Stacking of the Deque yye02 attempt 2019-03-17-11-44-42 Hanoi.py Original filename: DSQ Test.py Filename: Project 3 Queue the Stacking of the Deque yye02 attempt 2019-03-17-11-44-42 DSQ Test.py Original filename: Array Deque.py Filename: Project 3 Queue the Stacking of the Deque yye02 attempt 2019-03-17-11-44-42 Array Deque.py

CSCI 241 Data Structures Project 3: Queue the Stacking of the Deque

Your submission for project 3 will be graded according to the following rubric. You will receive a score in each category. Your total project score will be the sum of all category scores. Categories and their weights may change with each project.

	Exemplary 100%	Good 90%	Satisfactory 75%	Marginal 60%	Unacceptable 0%
Adherence to Specifications 20%	There are no deviations from the specifications. Items are named correctly. All files are present in the submission. The implementati on and writeup both reflect a deep understandin g of the project's purpose and how the specifications reinforce the relevant material.	Most components of the submission adhere to specifications . Some issues remain. Examples may include spelling or case of specified names or other editorially minor issues.	Many components of the submission conform to specifications , but key elements are incorrect. Examples may include incorrect performance measurement s, algorithmic deviations from what we cover in class, or use of built-in Python features instead of custom implementati ons.	The submission attempts to follow the instructions, but fundamental issues persist. There is a clear misunderstan ding as to the specifications and how they relate to the material at hand.	The submission may substantially incomplete. It may be missing specified components. It may implement items in ways other than specified or covered. The submission conveys either illiteracy or ignorance of the specifications.
Your Score					

	Exemplary	Good	Satisfactory	Marginal	Unacceptable
	100%	90%	75%	60%	0%
Functionality / Testing 30%	The submission passes all test cases. Output is formatted correctly. There is no unspecified output. Main code is conditioned to be separate from class or function definitions. There is evidence of extensive thought behind testing of code. Applications based on the project's data structures work perfectly. Unit tests are well-designed with consideration to coverage and overlap.	The submission produces the correct result, but minor issues such as formatting. A reasonable attempt was made to cover most test case possibilities, and those tests take advantage of provided examples. Applications based on the project's data structures are mostly correct. Unit tests cover most cases well, but miss some possibilities.	There is evidence that the implementati on does not consider problematic cases or special cases. The program may crash on a few test cases. Some testing is present, but it is incomplete and may not be based on the provided examples. There are some significant issues in the applications based on the project's data structures. Unit tests are sparse and missing significant coverage, but a reasonable effort is evident.	The implementati on is fundamentall y incorrect. Multiple cases fail, or the program crashes in multiple scenarios. The submission fails to convey a sufficient understandin g of the material. There is insufficient testing present to demonstrate any meaningful correctness of the code. Applications do not function correctly. Unit tests consider only basic possibilities or test too many things at a time.	The program crashes on most inputs. It contains errors that imply it could not have run during development. Of the test cases that do not crash, many fail with incorrect results. Little to no effort is evident with respect to confirming functionality. Application(s) are missing. Unit tests, if present at all, vary significantly from the examples provided from project 2. Main sections other than DSQ_test contain code. Insufficient time spent on testing is apparent.
Your Score					

	Exemplary 100%	Good 90%	Satisfactory 75%	Marginal 60%	Unacceptable 0%
Performance 10%	The implementati on takes advantage of all opportunities to improve performance.	The implementati on is generally efficient, but some steps could be taken to improve performance	The implementati on misses many opportunities to improve performance. Steps are taken without regard to their cost.	The implementati on is naïve with respect to performance. Some sections of code take significantly longer than the algorithms described in class.	The implementati on takes so long to run as to interfere with grading. it contains unnecessary loops or repetition of steps. If sections of code perform at all, they are extremely inefficient.
Your Score					

function, and class names are but names could be descriptive. Comments explain sections of code where necessary. Indentation is consistent and deliberate. Test code is well function, and class names but names to that should be moved to functions. Names are not reflective of what they reference. Inconsistent white space. The implementatio n contains unnecessary special cases. repeated code that should be moved to functions. Names are not reflective of what they reference. Inconsistent white space. The implementatio n contains reliability. Functions return value in appropriation features for the problem hand. Complex implementation not reflective of what they reference. Inconsistent white space. The implementation reliability. Functions return value in appropriation features for the problem hand. Complex implementation of what they reference. Inconsistent implementation in contains reliability. Functions return value in appropriation features for the problem hand. Complex implementation of what they reference. Inconsistent implementation implementation is consistent and deliberate. Test code is well		Exemplary 100%	Good 90%	Satisfactory 75%	Marginal 60%	Unacceptable 0%
		function, and class names are descriptive. Comments explain sections of code where necessary. Indentation is consistent and deliberate. Test code is well structured like the provided	structured, but names could be more descriptive. Some sections of code are not obvious and could benefit from additional	repeated code that should be moved to functions. Names are not reflective of what they reference. Inconsistent white space. The implementation contains unnecessary	Complex implementations are not commented. Names are poorly chosen. Repeated code degrades reliability. Functions return values inappropriatel	The implementatio n conveys a fundamental misunderstand ing of basic programming structures, regardless of language. Loops and conditionals are inappropriatel y interchanged. Incorrect variables are used for computation. Sections of code are unreachable
Your Score	Score					

	Exemplary 100%	Good 90%	Satisfactory 75%	Marginal 60%	Unacceptable 0%
Writeup 30%	The writeup indicates a deep understandin g of the material at hand. It employs illustrations, prose explanations, and examples to justify claims. It describes in detail the algorithmic steps that lead to performance variations (or for projects 2 and later, formal performance analysis). The document contains few if any grammatical errors.	The writeup is content-complete and generally correct, but presentation is lacking. It may fail justify some claims with illustrations or examples. It indicates that the general concepts are clearly understood, but minor improvemen ts in presentation would benefit the reader.	The writeup convers the specified material, but in a minimal way. It draws some incorrect conclusions, or offers incorrect or incomplete justifications. Minimal effort to distinguish this submission among others is present.	The writeup is not structured as a prose document, or contains only cursory responses to the required items. The writeup appears to have been an afterthought of the implementatio n instead of an integral component of the project. No effort to distinguish this submission among others is present.	The writeup is missing or fails to address the required items. If it is present, it is so brief as to indicate a lack of sufficient time, analysis, and construction of rational argument.
Score 28/30	+				

There are four results files present in this document.

First we re-run the tests for your linked list. If any tests still fail, 11 points will be subtracted from your rubric-based score. It is not possible to receive an A on this project if errors remain in your linked list implementation.

The next test results evaluate your deque, stack, queue, and Hanoi implementations using your Array_Deque backend.

The third test results evaluate your deque, stack, queue, and Hanoi implementations using your Linked_List_Deque backend.

Finally, the fourth test results evaluate your Delimiter_Check. This results are based on your Linked_List_Deque backend.

17 pages for this writeup is excessive. You should be able to adequately discuss these sections in max 7 pages, but more realistically 5

Performance Analysis of the Methods in *Deque*, *Stack*, *Queue* classes

Nice discussion on these implementation details

Comparison of two ways of implementing Array Deque class:

I have considered two different ways of implementing an array deque: one is to keep track of two attributes, a reference to the front position and the size of the deque, and to initialize the front position at point 0 in an empty deque; the other is to keep three attributes, a reference to the front, a reference to the back and a size, and in this way I initialize the front and back reference both to be None in an empty deque.

Obviously, the consistency is sacrificed in the first implementation, because the front reference is supposed to point to the actual front position in the deque that has a value in it, while in my first implementation, the front references actually points to the position after the actual front position when the deque is empty initially or reduced to be empty in operations. The motivation I attempted to implement the deque this way is that by not setting the front reference to be None, I need not to add an *if* statement in every push method to catch the situation where the reference is at None and the reference arithmetic cannot be validly executed. However, I wrote both implementations down and compared their simplicity, and I don't find the first one significantly better:

```
First implementation:
```

```
def push front(self, val):
    if self. size == self. capacity:
       self. grow()
    self. front = (self. front - 1 + self. capacity) % self. capacity
    self. contents[self. front] = val
    self. size = self. size + 1
Second implementation:
def push front(self, val):
    if self. size == self. capacity:
       self. grow()
    if self. front is None:
       self. front = 0
       self. back = 0
    else:
       self. front = (self. front - 1 + self. capacity) % self. capacity
    self. contents[self. front] = val
    self. size = self. size + 1
```

You should not have direct source code in your writeup because you already have your .py files, so, it is redundant.

Both implementations can push the value to the right place. The difference is tiny: the *if* statement in my second implementation is very simple. So, I don't think it's worthy of

sacrificing the consistency of my structure. Also, the difference between keeping a reference to the back position or not is not significant: in the first case one more step should be added to each push and pop method, while in the second case an arithmetic expression, which is slightly more costly should be added in the methods that involves the back position to find that back position. Since the first approach better carries out the beauty of a consistent data structure, I chose to use it.

Therefore, after examination, my Array_Deque finally prefers the second implementation, that is, I kept three attributes, front, back and size, and initialized front and back both to be None.

Performance Analysis of Deque methods:

init (self):

The worst-case performance of the constructer of implementations of *Deque* abstract base class is constant time O(1).

In the Array-based implementation, the work done by the constructer is fixed and there's no possible input value scale. The constructer first initializes an attribute <code>self.__capacity</code> to be 1, and then initializes an empty array <code>self.__contents</code> of the size of <code>self.__capacity</code>; then the constructer initialized two reference attribute, <code>self.__front</code> and <code>self.__back</code> both to point to None, and it finally initializes an attribute <code>self.__size</code> to be 0. All the works above are done in Python in constant steps. Therefore, the total performance time is a constant O(1). Also, in the Linked List-based implementation, the constructer does constant-time work which is just creating a linked_list object to store the data. Since it has been shown in the writeup of project2 that constructing a linked_list object in my implementation is constant time, this deque implementation's constructer is also constant time.

__str__(self):

The worst-case performance of the $_str_()$ method of the implementations of *Deque* abstract base class is linear time O(n).

In the Array-based implementation, the $_str_()$ method has to loop (self. $_size-1$) times to see and get every value stored in the deque (because the loop ends at one position before the back position, for the string operation done to the last element is different in that "," should not be appended after the last element), which is a function of n. Given that inside each loop the work is constant, only involving an index arithmetic to locate the index and a string conjunction operation, which are both able to be executed in constant time, the total performance of $_str_()$ method is a function of n times a constant function plus a constant function that represents the remaining work of formatting the string. Therefore, the total performance is a function of n, which is linear time O(n).

In the Linked List-based implementation, the $_str_()$ method just calls the $_str_()$ method in the Linked_List class, which has been shown to be linear time O(n), and it basically does the same work as looping through the whole list, doing constant work inside

each loop, and doing constant work for the remaining part of the method. Therefore, the worst-case performance of $_str_()$ method in a Linked_List-based deque implementation is linear time O(n).

len (self):

The worst-case performance of the $_len_(l)$ method in the implementations of deque class is constant time O(1).

In the Array-based implementation, __len__() method just returns an instance variable, self.__size, without doing any count or loop. Since self.__size is kept as an attribute and updated every time the length of the deque is changed, in this particular method it is just constant time to look and return a value that is always stored at hand.

In the Linked_List-based implementation, the __len__() method just calls the __len__() method in the Linked_List class, which I have shown in the previous writeup to be constant time for the same reasons.

Great grow discussion

__grow(self)(exclusively array-based implementation)

The asymptotic performance of $_grow()$ method in an Array-based implementation of deque class is linear time O(n). The linear part of this method is that it has to loop through every values in the current self. $_contents$ and pass them to the $new_contents$, which is a loop of n times. Since passing a value of one cell in an array to another cell in another array is a constant-time work, the total performance of this passing operation is a function of n, which is linear. Apart from this part, the remaining work is all constant time: constructing an empty array of twice length as the existing one, pointing the attribute self. $_contents$ to the newly constructed array, and updating the self. $_capcacity$. Therefore, the total performance of the method is also a function of n, which is linear time O(n),

push front(self, val):

The asymptotic performance of this method is different in the two implementations of deque class.

In the Array-based implementation, the worst-case asymptotic performance of the $push_front()$ method is linear time O(n). This is because of the $_grow()$ method that is called inside the $push_front()$ method. In the worst case, this linear time $_grow()$ method is executed, making the total performance of the $push_front()$ method a function of n plus a constant function which is the constant work of adding the value as the new front. However, the amortized performance of the $push_front()$ method in and array-based deque class is constant time O(1), because a consecutive n calls of $push_front()$ in an array-based deque should run at total O(n) times. If it is reasonable to assume there's no need to frequently resize the array, i.e., if the array-based deque is expected to remain at a moderate length (e.g, every $push_front()$ is preceded by a pop so that the push will always run without calling the linear $_grow$ method), the performance of $push_front()$ can be even more efficient. The other work of advancing the reference of front circularly through the array

and assign the value to that new front position are all constant time O(1).

In the Linked-List-based deque implementation, the worst-case asymptotic performance of the $push_front()$ method is constant time O(1). In this implementation, either the list is already empty, so the $push_front()$ method calls an $append_element(val)$ method in the linked list class, or the list is not empty, and an $insert_element_at(val,0)$ is called. Both methods are constant time O(1) in a linked list class because a linked list supports constant-time access to its header and trailer attribute that can be used to conveniently modify the head and tail position. Therefore, the total performance of $push_front()$ method in a linked_list-based deque is always constant time O(1).

Great discussion of the comparison between the two pushes.

Comparison of linked-list push() and array push():

It seems that a linked list-based implementation outperforms the array-based implementation, since the worst-case performance of the former is linear time O(1) while that of the latter is linear time O(n). However, if the grow() is not called in an arraybased implementation, then the *push front()* in an array is slightly faster and uses less memory space than a linked list *push front()*. This is because for a linked list to insert or append element, a Node object has to be created and stored first, which cost memory and time, and there are more references needed to be set (the prev, next of the constructed Node, the prev of the Node after that constructed Node, and the next of the previous one). Whereas in an array, at most two reference has to be modified (front and back, in the case where they're initially None). Therefore, since the amortized performance of two implementations are the same, and the array-based *push front()* may have slightly smaller coefficient and better memory use, it is reasonable to prefer an array-based deque when there the deque is not expected to grow frequently. On the other hand, if the deque is expected to go very long, the demerit of grow() methods would outweigh the advantage of array implementation, and it is better to use a linked list-based deque. Furthermore, if the expected size of the deque is relatively small, and the number of *pushing* operations are also small, then it is also reasonable to prefer a linked-list-based deque because in a small number of operations, the linearity of grow() would take up a large proportion, making the total performance of array-based deque inefficient.

Therefore, the principle of determining which implementation to use should be this: **if** the deque for my project is implemented by an array, what is the proportion of __grow methods that are executed to the total times of operations in my deque? If this proportion is large, as in the case of a very short deque and a continuously growing deque, then the array-deque is outperformed by linked list-deque in efficiency; while if this proportion is expected to be small, then the array-based deque should be preferred for slightly faster performance and great improvement in memory use.

pop_front(self)

The worst-case asymptotic performance of $pop_front()$ method in the two implementations of deque abstract base class is the same constant time O(1).

In an array-based implementation, the $pop_front()$ method does three things: preserve the value at the current front position, make the front reference "-1", according to my selection of front direction, and decrement the size. These works can all be done in constant times because they only involve directly modifying or accessing the attributes. Further, the if statement catches the worst case in this method, i.e., the size goes to 0 after popping. In this case, two more constant-time work is done to set the front and back reference to be None. Therefore, the total performance of this method in array-based deque is a sum of constant functions, which is also constant time O(1).

In a linked-list-based implementation, the worst-case performance of $pop_front()$ method is also constant time O(1), because in the worst case, the $remove_element_at(0)$ is called, which is constant time in a linked list class because the loop is not executed.

For the same reason as above, the array-based implementation is slightly faster and uses less memory space than linked list, namely that the array involves less modification of references and doesn't need extra space to store a Node object.

peek front(val)

The worst-case performance of $peek_front()$ method in both implementations of deque abstract base class is constant time O(1).

In the array-based implementation, the work is just to return the value in *self.__contents* at the position of *self.__front*. Since both attributes are kept track of in the class, this work is constant time O(1).

In the linked-list-based deque implementation, when the deque is not empty, which is the worst case, $get_element_at(0)$ is called. This method in a linked list class is constant time as has been shown in the previous writeup, because linked list supports constant-time access to its head position by header.next. Therefore, the $peek_front()$ is constant time O(1). For the same reason, the array-based implementation uses less memory space than linked list, namely that the array doesn't need extra space to store a Node object.

push/pop/peek back()

The worst-case asymptotic performance and performance feature of <code>push/pop/peek_back()</code> methods are exactly the same as <code>push/pop/peek_front()</code>. This is justified because in the array-based implementation, I have both the front and back reference stored as attributes, so modifying both ends can follow the same procedure; and in a linked list, operations on the head position and tail position are equally efficient because of the constant-time access to both positions.

Performance Analysis of Stack Methods

__init__(self)

The worst-case performance of the constructer of Stack class is constant time O(1). The constructer of Stack class calls a function get deque(). This function either returns an array-

deque object or returns a linked-list-deque object by calling their respective constructer, depending on the parameter sent to it. Since it has been shown above that either of the constructers of array-deque or linked list-deque is constant time. The performance of $get_deque()$ function is constant time O(1). Therefore, the performance of the constructer is also constant time O(1).

str (self)

The worst-case performance of the $_str_()$ method is linear time O(n). Since the $_str_()$ method in Stack class just calls the $_str_()$ method in the deque abstract base class, its performance should be identical to that in the deque class; and since it has been shown that the $_str_()$ method in the deque class is linear time no matter which implementation is chosen, the $_str_()$ method in the Stack class is also linear time no matter it is implemented with an array-deque or a linked list-deque.

len (self)

For the same reason as above, the worst-case performance of <u>__len__()</u> method in a *Stack* class is the same as the performance of <u>__len__()</u> method in either deque implementation, which is constant time O(1).

push(self, val)

Since the *push()* method in the *Stack* class calls the *push_front()* method in either implementation of the deque abstract base class, the performance feature of this method is identical to that in Array-deque or Linked list-deque, which I have discussed above.

To briefly recap, if the Stack is implemented with an array, then the worst-case asymptotic performance of the push() method is linear time O(n) because of the linear $_grow()$ method. However, if it is reasonable to suppose the $_grow()$ is not frequently executed, then the amortized performance of push() method is constant time O(1).

On the other hand, if the Stack is implemented with a linked list-deque, then the worst-case performance of the push() method is constant time O(n) with slighter bigger coefficient and more memory use than the array-push without the grow() method.

pop(self)

From the same line of reasoning, the performance feature of pop() method in the Stack class is identical to one of the $pop_front()$ method of the two implementations of the deque abstract base class. In this case, the worst-case performance of $pop_front()$ method in either array-deque or linked list-deque is constant time O(1). Therefore, the worst-case performance of pop() method in a Stack class is constant time O(1).

peek()

From the same line of reasoning, the worst-case performance of peek() method in the Stack class is constant time O(1) because in either an array-based deque or a linked list-based

Nice job discussing the performance of stack and queue for both deque implementations (array and linked list).

deque, the *peek front()* method cost constant time O(1).

Performance Analysis of Queue Methods

init	(self)
$\iota\iota\iota\iota\iota\iota$	(seij)

The worst-case performance of the constructer of *Queue* class is constant time O(1), which is the same as that of *Stack* constructer. The two constructers do exactly the same work as calling the $get_deque()$ function and use the returned deque from that function as an instance variable. Therefore, their performance feature is also identical, which is worst-case O(1).

str (self)

The worst-case performance of the $_str_()$ method in the *Queue* class is linear time O(n). Since this $_str_()$ method calls the $_str_()$ method in one of the implementations of the deque abstract base class, the work done by it is identical to the work of one of the implementation's $_str_()$ method depending on the return value of get_deque function. Given that the array-deque and the linked list-deque both have a linear worst-case performance $_str_()$ method, the $_str_()$ method in the gueue class which uses either of them must also be linear time g(n).

len (self)

The worst-case performance of the $_len_()$ method in the Queue class is constant time O(1). The reason is the same as that of $_str_()$ method: the $_len_()$ method in the Queue class calls the $_len_()$ method in either of the two implementations of the deque abstract base class, and both of them are constant time as have been shown above. Therefore, no matter which deque is used, the $_len_()$ method in the Queue costs constant time O(1).

enqueue(self, val)

The performance feature of the enqueue() method is similar to the push() method in the Stack class, since the push() calls the $push_front()$ in either of the two deque implementations and the enqueue() calls $push_back()$, and the performance feature of $push_front()$ and $push_back()$ in a deque implementation has been shown to be similar. Therefore, if the Queue class uses an array-deque as its instance variable, then the worst-case asymptotic performance of the enqueue() method is linear time O(n) because of the linear $_grow()$ method. However, if there's good reasons to expect the $_grow()$ function is not frequently executed as opposed to the total number of enqueue(), then the amortized performance is constant time O(1), and the memory use is relatively small.

On the other hand, if the *Queue* uses a linked list-deque to store data, then the asymptotic performance of the *enqueue()* method is constant time O(1), but with slightly higher coefficient than the array-based *enqueue* without executing the $_grow()$, and it cost more

memory space to store the created Node object.

```
dequeue()
```

The worst-case performance of the dequeue() method is the same as that of the pop() method in the Stack class, which is constant time O(1). The reason is the same: it calls the $pop_front()$ method in either of the two deque implementations that is used to store data, and either of them has worst-case constant time performance, which has been shown above. Therefore no matter which one is used, the dequeue() method in the Queue class is constant time O(1).

Performance analysis of choosing front and back position

First of all, in my array-based implementation of the *deque* class, I choose the "-1" in the array cell operation to be the front direction, and "+1" to be the back direction, which means in pushing front and popping back, the front/back reference should "-1", and in pushing back and popping front, the back/front reference should "+1". Then, in the linked-list-based implementation of the *deque* class, I use the descriptive head position in the linked list as the front of my deque and the tail in the list as my back.

I want to clarify first that my choice of front and back position doesn't matter in the performance analysis of either array or linked list based deque.

In an array-deque, if I choose the front as the way I did, then in the *push_front()* method, the index arithmetic should be:

```
self.__front = (self.__front - 1 + self.__capacity) % self.__capacity
and in the push_back() method the arithmetic is:
    self.__back = (self.__back + 1) % self.__capacity
```

It can be clearly seen that if I choose the reverse way as I did, then two arithmetic should reverse accordingly, but the overall performance is strictly the same since both front and back operation should be frequently called of a deque. The same goes for the two *pop()* method.

Further, in a linked list-based implementation, the choice of front and back doesn't matter either. In my choice, the *push_front()* method would have the *if* statement to catch the situation where the deque is empty:

```
def push_front(self, val):
    if len(self.__list) == 0:
        self.__list.append_element(val)
    else:
        self.__list.insert_element_at(val,0)
and in the push_back() method there need not be such conditional:
    def push_back(self, val):
        self.__list.append_element(val)
If I choose the tail to be front and head to be back, then just the reverse happens: my
```

Well I am impressed by the level of discussion, this is not required for these writeups.

push_front() position would be straightforward but the *push_back()* have to have a conditional to handle the empty deque. And the overall performance of my deque structure is strictly the same.

For the implementation of *Stack* and *Queue*, I choose the original front position in the array-deque and the head position in the linked list-deque as their front and the corresponding back as their back. I do this way for the readability and consistency of my code, for in this way, the *push* and *pop* in the *Stack* corresponds to *push_front* and *pop_front*, which is consistent with the definition of a *Stack* and is easily understandable; and similarly, in a *Queue*, the *enqueue* and *dequeue* correspond to *push_back* and *pop_front*, which is also very consistent and easy to recognize.

I recognized some reasons for doing other wise, i.e., to simplify the *push* or *enqueue* so that they need not involve an *if* statement which catches the case where the list is empty and the linked list-deque *insert* method cannot be executed. I want to argue that given what we're expected to do, this makes no difference on the overall performance of the two classes, *Stack* and *Queue*. First, in a linked list-based deque implementation, no matter which position I set to be front, *head* or *tail*, one of the *push_front* and *push_back* has to have an *if* statement for the above use. If I set the *head* to be the front, then I have to consider the empty list case in my *push_front* method; on the other hand, if I set the *tail* to be front, then I have to consider the empty case when I call the *push_back* method. No matter how I choose the front, one method has to be conditional and slightly more complicated than the other, which is because of the nature of my linked-list class.

This being established, now consider the *Stack* and *Queue*. The *Stack* class needs *push_front* method while the *Queue* class needs *push_back* method. This means that no matter how I choose the front and back position, one of the *Stack* and *Queue* class has to have a push method that has an *if* conditional. The choice of front and back position matters when only a *Stack* or only a *Queue* is to be implemented, but not when both are implemented.

However, there is one way to escape my problem: to use reverse front in *Stack* and *Queue* class, i.e., in a *Stack* class, call *push_back* and *pop_back* while in the *Queue* class call *push_back* and *pop_front*. This way, the push method in the two classes are the same, so it is possible to choose the appropriate front to simplify the method. This, I argue, will cost greater trouble, which is with the string representation. Since the __str__() method in my deque implementations only supports representing the deque from front to back, if the *Stack* class has the front of the deque as its back and the back of the deque as its front, then it can no longer use the __str__() of the deque to represent its elements in string. If the *Stack* class has to loop through its element to have its own __str__() method, it will cause huge change to the whole structure and greatly undermine the consistency and simplicity of the whole deque-stack-queue structure. I don't think this cost is worth paying, since the performance improvement is really slight.

Unit Test Cases for the Deque Class

In testing the *deque* class methods, I focus especially on testing the possible difficulties on the array-based implementation of the *deque* class. The linked list-based *deque* is antecedently more reliable because it doesn't build the structure from scratch, but just calls the corresponding methods in the linked list class which I have tested in the previous project. Due to the fact that a doubly linked list, if only considered of its most efficient operations, works very much like a deque in itself, I think the linked list-based *deque* should work fine as long as the linked list works fine.

For the array-based deque implementation, the structure of a deque is constructed within a circular array by keeping track of three attributes, front, back and size. Since every method that updates the array-deque would change some of these attributes and is possible to affects subsequent operations, the test of array-deque should explicitly include tests that ensures that a sequence of different operations, which involves different ways of updating the three attributes, can work fine. This kind of test should be added to the standard tests similar to that of the linked list class that test the efficacy of single method.

Therefore, following this principle of "standard one method test + deliberately designed test of a sequence of different methods", and based on the feature of a deque, I designed the following blocks of test code:

Testing *push_front()* and *push_back()*:

The first block of test code is to test that I can successfully update my deque by passing values to the front or back position. The success means three things: first, I should have a successfully updated deque which can be represented in the string in the right format; second, I should have a successfully updated size attribute, which reflects in the right output of __len__() method; third, I should have my front and back reference rightly updated so that following operations based on these references can work without causing problems. The third overlaps with the first to some degree, but it is a separate demand of my testing purpose because in principle it is possible for one of my *push* or *str* call to produce a rightly updated deque but causing problem in the reference somehow that the following different function call will fail. In this block I have the following test:

```
def test_empty_deque_string(self):
```

this is to test the __str__() method can output the empty deque in the right format. def test_get_empty_length(self):

this is to test the __len__() method can output the length of an empy deque rightly. def test_push_front_empty(self):

this is to test the *push_front()* method can successfully update an empty string to a string with one element.

```
def test_get_one_length_front(self):
```

this is to test the length of such updated deque is right.

```
def test_push_front_one(self):
```

this is to test the *push_front()* methodcan successfully add an element to a deque with one element at the front, and the updated deque is formatted rightly def test get two length front(self):

this is to test the length of the updated deque by the above operation is right.

. . .

Note: I explicitly uses the *push* methods three times to eventually test the string format and length of a deque with 3 element; this is not necessary, but I want to do this because I want to have the __grow() method executed twice to see it works fine without causing problems.

```
def test_push_back_empty(self):
  def test_push_back_one(self):
```

This is where I do the same test as above, but with the *push_back()* method to test the same efficacy of *push_back()* method on its own: updating the deque in the right way, and successfully updating the length.

```
def test_front_back(self):
    self.__deque.push_front('Data')
    self.__deque.push_back('Structure')
    self.assertEqual('[ Data, Structure ]', str(self.__deque))
def test_back_front(self):
    self.__deque.push_back('Data')
    self.__deque.push_front('Structure')
    self.assertEqual('[ Structure, Data ]', str(self._deque))
```

After testing and knowing that the *push_front()* and *push_back()* methods are both efficacious in themselves, I add these two tests to see that they can work well after each other, i.e., the call of one method updates the front and back reference both in the right way that the following other method can work perfectly.

```
def test_get_two_length_front_back(self):
def test_get_two_length_back_front(self):
```

In these two methods I do the same thing as above, updating the deque using a consecutive *push_front(back)* and *push_back(front)*, and see the length is updated rightly. This is not 100% necessary given that it has been shown that both *push_front()* and *push_back()* can update the length rightly. But I still do this test for consistency.

Testing pop front() and pop back():

In the second block of test code, I purpose to test the efficacy and reliability of my pop

methods. For each *pop* method in itself, there are three things to test: first, the return value is right; second, the remaining deque is right and the value is successfully popped out of the deque; third, the length is rightly updated. Besides the above, I want to show that my *pop* methods update the front and back reference in the right way that following operations can succeed. For this aim, I tested the efficacy of pushing values after popping, and see the deque and length are both rightly updated. I have the following test codes:

```
def test_pop_front_empty_return_value(self):
    to_return = self.__deque.pop_front()
    self.assertEqual(None, to_return)

def test_pop_front_empty_remaining_deque(self):
    to_return = self.__deque.pop_front()
    self.assertEqual('[ ]', str(self.__deque))

def test_pop_front_empty_length(self):
    to_return = self.__deque.pop_front()
    self.assertEqual(0, len(self.__deque))

def test_pop_back_empty_return_value(self):
    def test_pop_back_empty_remaining_deque(self):
    def test_pop_back_empty_length(self):
```

This is to explicitly show that *pop_front()* and *pop_back()* should have no effect on an already empty deque, i.e., no value is returned, the deque is exactly unchanged, and the length is 0.

```
def test_pop_front_leaving_empty_return_value(self):
def test_pop_front_leaving_empty_remaining_deque(self):
def test_pop_front_leaving_empty_length(self):
...
def test_pop_back_leaving_one_return_value(self):
def test_pop_back_leaving_one_remaining_deque(self):
def test_pop_back_leaving_one_length(self):
```

These tests are to show that *pop_front()* and *pop_back()* meets the three conditions above in updating nonempty deques.

```
def test_pop_front_leaving_one_push_front(self):
    self.__deque.push_front('Data')
    self.__deque.push_front('Structure')
    to return = self. deque.pop_front()
```

```
self.__deque.push_front('Ye')
self.assertEqual('[ Ye, Data ]', str(self.__deque))

def test_pop_front_leaving_one_push_back(self):
    self.__deque.push_front('Data')
    self.__deque.push_front('Structure')
    to_return = self.__deque.pop_front()
    self.__deque.push_back('Ye')
    self.assertEqual('[ Data, Ye ]', str(self. deque))
```

Then, after making sure that *push_front()* and *push_back()* methods are both efficacious in themselves, I test to see that they're a part of a reliable structure, i.e., calling them can update the front and back reference in the right way that following work can be done without problem. For this purpose, I tested to push values after popping and see that the deque is updated in the right way and length is right.

```
def test_pop_back_leaving_one_push_front(self):
def test_pop_back_leaving_one_push_back(self):
```

This is to test the same thing with pop back()

Testing peek front() and peek back():

In the third block of test I tested the *peek* methods that access and returns the front or back value without changing the deque. In this block of test, I don't have to worry about the impact of *peek* on further operations because *peek* methods are not expected to update any attribute; rather, I have to ensure that *peek* has absolutely no impact on any other operations. Therefore, what I have to test are three things: first, the return value is right; second, the deque is left exactly unchanged; third, the length is left unchanged. After testing these, I should add a few tests to show that any operations after *peek* can work well:

```
def test_peek_front_empty_return_value(self):
    def test_peek_front_empty_remaining_deque(self):
    def test_peek_front_empty_length(self):
```

These tests are to test that *peek_front()* meets the three conditions above, i.e., it returns the right value, leaves the deque unchanged and leaves the length unchanged. Also, *peek_front()* should have no effect on an empty deque: None is returned, the deque is still empty, and the length is still 0.

```
def test_peek_back_empty_return_value(self):
def test_peek_back_empty_remaining_deque(self):
```

```
def test_peek_back_empty_length(self):
...

These are to test the same thing with peek_back()

def test_peek_front_push_front_remaining_deque(self):
    self.__deque.push_front('Ye')
    to_return = self.__deque.peek_front()
    self.__deque.push_front('Yangchen')
    self.assertEqual('[ Yangchen, Ye ]', str(self.__deque))

def test_peek_front_push_front_length(self):
    self.__deque.push_front('Ye')
    to_return = self.__deque.peek_front()
    self.__deque.push_front('Yangchen')
    self.assertEqual(2, len(self.__deque))
```

Then, after testing the *peek_front()* and *peek_back()* both work well in themselves, I added these codes to show that they're capable of being integrated in a reliable structure, i.e., any subsequent deque operations can work successfully after calling *peek_front()*.

```
def test_peek_back_push_front_remaining_deque(self):
def test_peek_back_push_front_length(self):
...
These are to do the same test with peek_back.
```

Unit Test Cases for the Stack and Queue Classes

The test cases for *Stack* and *Queue* classes are following the same logic for testing *deque* class, and they need not be so detailed and tedious as in *deque* class tests. After all, the *Stack* and *Queue* methods are just a subset of the methods in *deque* class, and once we have ensured that all methods in the *deque* class works well in themselves and as an integrated solid structure, the methods in *Stack* and *Queue* class should work well automatically. The specific purpose of my test codes about *Stack* and *Queue* classes is to see that the methods in these two classes correctly call the corresponding methods in the *deque* class. If this is not so, then I can clearly see that the corresponding method in the *deque* class passed the test while the method in the *Stack* or *Queue* class fails. This is the only possibility that my *Stack* and *Queue* classes can work badly once I have assured that my *deque* class works finely. Further, since in such cases the methods in *Stack* and *Queue* classes must fail the test on their own, I don't need to test a sequence of methods called one after another as I have done in testing the *deque* structure. Therefore, the test blocks I have for *Stack* and *Queues* are just duplicates of the blocks I have for *push* and *pop* in my

deque structure respectively, and I don't need to test the combined effects of the methods as a reliable whole structure.

The performance observation of Hanoi

```
My algorithm for solving the Hanoi problem is as follows:
def Hanoi(n):
    source = Stack()
    dest = Stack()
    aux = Stack()
    i = n-1
    while i \ge 0.
        source.push(i)
        i = i - 1
    Hanoi rec(n-1, source, aux, dest)
def Hanoi rec(n, s, a, d):
    print(n, s, a, d)
    # TODO replace pass with your base and recursive cases.
    if n == 0:
         d.push(s.pop())
    else:
         Hanoi rec(n-1, s, d, a)
         d.push(s.pop())
         Hanoi rec(n-1, a, s, d)
    print(n, s, a, d)
    print()
```

It is a recursive function; and suppose the performance time of solving the Hanoi problem with n discs is T(n). Then it is observed that:

- (1) T(1) = 1, since when n=1, the work is constant, just involving a *pop* and a *push* of two stacks, which have been shown to be constant time.
- (2) T(n) = 2T(n-1) + 1, since to perform any Hanoi(n) involves performing two Hanoi(n-1) and a constant-time work of popping and pushing.

From (1) and (2) it can be seen that T(n) grows geometrically, and by observing that: T(1): 1, T(2): 3, T(3): 7, T(4): 15... I made the conjecture that $T(n) = 2^n$ -1, which is exponential time.

My conjecture can be proved by mathematical induction:

```
Proof: T(n) = 2^n-1 holds for all n \ge 1,
```

Well done with this Hanoi performance analysis, however, make sure you are also discussing what the problem is, what your solution is, why your solution solves the problem, and then finally what the performance analysis is

Step1: when n = 1, $T(1) = 2^{1}-1 = 1$ is true, therefore, $T(n) = 2^{n}-1$ is true when n=1. Step2: assume that $T(n) = 2^{n}-1$ is true when n=k, $k \ge 1$ i.e., $T(k) = 2^{k}-1$. Then, consider T(n+1); n+1 = k+1, $T(k+1) = 2T(k) + 1 = 2*(2^{k}-1) + 1 = 2^{k+1}-1$; which is true. Therefore, $T(k+1) = 2^{k+1}-1$ is true for all $k \ge 1$ as long as $T(k) = 2^{k}-1$.

Therefore, combining Step1 and Step2 by the principle of mathematical induction, it is proved that $T(n) = 2^{n}-1$.

Discussion of the decision not to raise exceptions

I think the decision not to raise exceptions in my *deque* implementations is appropriate, and actually is consistent with what an exception is expected to do.

I think the exception is usually used to catch unexpected input such that, if it enters the program, the program will confront the risk of crash. For example, in my linked list class, an IndexError exception is raised when my user tries to call <code>insert_element_at(val, -1)</code>. This is because I cannot let -1 enter my program as a parameter and be passed into my loop <code>for k in range(-1)</code>, which is an unacceptable index. For similar reasons, I cannot let my user pass a value bigger than or equal to <code>len(list)</code> as a parameter into my program because that would cause my index to point to <code>self.__trailer</code>, or some place after it, which is undefined. In all above situations, I have urgent and compelling reasons to block an invalid operation <code>by users</code> through an exception, otherwise the consistency of my program will be undermined.

However, the situation is different in my *deque* implementations. In my *deque* implementation, there are no such invalid inputs that have to be blocked and informed to the users by an exception: the only input the users have to pass are values, which cannot be invalid. If there's no index, you cannot raise an *IndexError*. What my methods in my *deque* implementation has to do, i.e., check if the deque is empty before popping or peeking anything, are not interacting with user input, but just part of the methods' inner logic. I think in these cases it is appropriate to not raise exceptions and interrupt with the users' work flow. In other word, exception handles situations that are unexpected by the inner logic of the method, often posed by invalid user inputs, while in my *deque* classes, there're no **unexpected** situations, because "popping an empty deque should have no effect" is what has already been expected by the inner logic of pop methods. Therefore, I suggest not raising an exception for that. A similar case happens in the *rotate_left()* method of my linked list class. In that method, "rotating an empty list should have no effect" is something that has already been expected in the logic of the method, so no exception is raised to handle this situation.

Despite what being argued, the method of returning None in my functions instead of raising an exception has its drawbacks. The first one that comes into my mind is that a deque with one element "None" would be indistinguishable from an empty deque. All of

Well done with this Raise Exception section.

the pop_front(), pop_back(), peek_front(), peek_back() will return exactly the same value when called on both two deques. For this reason, when my user calls a pop method and finds that the returned value is None, he would not be able to determine what this really means: does this None mean that my deque is empty? Or does this mean the front/back value stored in my deque is None? This limitation would remain even if I change the return value to be anything, like a string "your deque is empty": as long as the return value is itself a valid value that can be stored in a deque, the two situations will be indistinguishable. However, since it is very unlikely that my user would use a deque to store a string "your deque is empty", this alternative might work better than the one I'm taking now; but to ultimately resolve this problem, I suggest I should raise a specific type of Empty exception, which is in its essence a different type of returning so the user cannot mistake the message for any possible value stored in the deque. This is similar to what

Overall, great job with this writeup. Things to improve are making sure to be concise with your discussions and your Hanoi section. As commented above, so many pages is really overkill for this type of writeup and some of your discussions, while really well done, were not necessary. Also, as commented your Hanoi performance analysis was well done, but can be confusing to a reader without the context of what the problem and your solution is. Also, you are also missing your delimiter check section. You should be writing a performance analysis for every program you write in this class.

```
from Deque import Deque
class Array Deque(Deque):
 def __init__(self):
    # capacity starts at 1; we will grow on demand.
    self.__capacity = 1
    self.__contents = [None] * self. capacity
    self.__front = None
   self.__back = None
    self. size = 0
 def __str__(self):
    if self. size == 0:
     return '[ ]'
    else:
     result = '[ '
     for k in range(self. size-1):
        index = (self.__front + k) % self.__capacity
        result = result + str(self. contents[index]) + ', '
      result = result + str(self.__contents[self.__back]) + ' ]'
      return result
 def len (self):
    return self. size
 def grow(self):
    new_capacity = self.__capacity * 2
    new_contents = [None] * new_capacity
    for k in range(self. size):
      index = (self.__front + k) % self.__capacity
      new_contents[k] = self.__contents[index]
    self. contents = new contents
    self.__capacity = new_capacity
    self.\_front = 0
    self.__back = self.__size - 1
 #I use left "-1" as the front direction and right "+1" as the back
direction, so
  #pushing front and popping back should result in the "-1" of front/back
reference
 #and pushing back and popping front should result in the "+1" of
 #back/front reference
 def push front(self, val):
    if self.__size == self.__capacity:
```

```
yye02_Array_Deque.py.rtf
```

```
self.__grow()
    if self.__front is None:
     #if the deque is empty, a push should initiallize the front and back
reference to 0
      self.__front = 0
      self._ back = 0
     self.__front = (self.__front - 1 + self.__capacity) %
self. capacity
    self.__contents[self.__front] = val
    self. size = self. size + 1
 def pop front(self):
    if self. size == 0:
      return
    value = self.__contents[self.__front]
    self. front = (self.__front + 1) % self.__capacity
    self.__size = self.__size - 1
    if self. size == 0:
     #if the deque is empty after popping, reset the front and back
reference to None
     self.__front = None
      self.__back = None
    return value
 def peek front(self):
    if self.__size == 0:
      return
    return self. contents[self. front]
 def push_back(self, val):
    if self. size == self. capacity:
     self.__grow()
    if self.__back == None:
      self.__front = 0
     self.__back = 0
    else:
      self.__back = (self.__back + 1) % self.__capacity
    self.__contents[self.__back] = val
    self.__size = self.__size + 1
  def pop back(self):
    if self. size == 0:
     return
    value = self. contents[self. back]
```

```
self.__back = (self.__back - 1 + self.__capacity) % self.__capacity
self.__size = self.__size - 1
if self.__size == 0:
    self.__back = None
    self.__front = None
    return value

def peek_back(self):
    if self.__size == 0:
        return
    return self.__contents[self.__back]
```

```
import sys # for sys.argv, the command-line arguments
from Stack import Stack
def delimiter check(filename):
 # TODO replace pass with an implementation that returns True
 # if the delimiters (), [], and {} are balanced and False otherwise.
  delimiter dict = {
    '(':')',
    `(`!`j',
    '{':'}'
  }
  Reference stack = Stack()
 file = open(filename)
  content = file.read()
  for ch in content:
    if ch in delimiter dict.keys():
      Reference stack.push(ch)
    elif ch in delimiter dict.values():
      if len(Reference stack) == 0:
        return False
      elif ch != delimiter dict.get(Reference stack.pop()):
        return False
  file.close()
  return len(Reference stack) == 0
if name == ' main ':
 # The list sys.argv contains everything the user typed on the command
 # line after the word python. For example, if the user types
 # python Delimiter Check.py file to check.py
 # then printing the contents of sys.argv shows
 # ['Delimiter_Check.py', 'file_to_check.py']
 if len(sys.argv) < 2:</pre>
   # This means the user did not provide the filename to check.
    # Show the correct usage.
    print('Usage: python Delimiter_Check.py file_to_check.py')
 else:
    if delimiter check(sys.argv[1]):
      print('The file contains balanced delimiters.')
    else:
      print('The file contains IMBALANCED DELIMITERS.')
```

```
yye02_DSQ_Test.py.rtf
import unittest
from Deque_Generator import get_deque
from Stack import Stack
from Queue import Queue
class DSQTester(unittest.TestCase):
 def setUp(self):
    self.__deque = get_deque()
    self.__stack = Stack()
    self. queue = Queue()
 # TODO add your test methods here. Like Linked List Test.py,
 # each test should me in a method whose name begins with test
 #testing deque
 def test empty deque string(self):
     self.assertEqual('[]', str(self.__deque)) #an empty deque should be
'[ ]'
 def test push front empty(self):
     self. deque.push front('Data')
     self.assertEqual('[ Data ]', str(self. deque))
 def test push front one(self):
     self.__deque.push_front('Structure')
     self. deque.push front('Data')
     self.assertEqual('[ Data, Structure ]', str(self. deque))
 def test push front two(self):
     self. deque.push front('Structure')
     self.__deque.push_front('Data')
     self.__deque.push_front('Love')
     self.assertEqual('[ Love, Data, Structure ]', str(self. deque))
 def test push back empty(self):
     self. deque.push back('Data')
     self.assertEqual('[ Data ]', str(self. deque))
 def test_push_back_one(self):
     self.__deque.push_back('Data')
     self. deque.push back('Structure')
     self.assertEqual('[ Data, Structure ]', str(self. deque))
 def test push back two(self):
     self. deque.push back('Data')
     self. deque.push back('Structure')
```

```
yye02_DSQ_Test.py.rtf
```

```
self.__deque.push_back('Project')
   self.assertEqual('[ Data, Structure, Project ]', str(self.__deque))
def test front back(self):
   self.__deque.push_front('Data')
   self.__deque.push back('Structure')
   self.assertEqual('[ Data, Structure ]', str(self. deque))
def test back front(self):
   self.__deque.push_back('Data')
   self. deque.push front('Structure')
   self.assertEqual('[ Structure, Data ]', str(self. deque))
def test get empty length(self):
   self.assertEqual(0, len(self. deque))
def test get one length front(self):
   self. deque.push front('Yangchen')
   self.assertEqual(1, len(self. deque))
def test get two length front(self):
   self.__deque.push_front('Yangchen')
   self. deque.push front('Ye')
   self.assertEqual(2, len(self. deque))
def test get one length back(self):
   self. deque.push back('Yangchen')
   self.assertEqual(1, len(self. deque))
def test get two length back(self):
   self.__deque.push_back('Yangchen')
   self.__deque.push_back('Ye')
   self.assertEqual(2, len(self.__deque))
def test get two length front back(self):
   self.__deque.push_front('Yangchen')
   self.__deque.push_back('Ye')
   self.assertEqual(2, len(self. deque))
def test get two length back front(self):
   self.__deque.push back('Ye')
   self. deque.push front('Zhang')
   self.assertEqual(2, len(self.__deque))
def test pop front empty return value(self):
   to return = self. deque.pop front()
```

```
self.assertEqual(None, to return)
def test pop front empty remaining deque(self):
   to_return = self.__deque.pop_front()
   self.assertEqual('[ ]', str(self. deque))
def test pop front empty length(self):
   to return = self.__deque.pop_front()
   self.assertEqual(0, len(self.__deque))
def test pop front leaving empty return value(self):
   self. deque.push_front('Yangchen')
   to_return = self.__deque.pop_front()
   self.assertEqual('Yangchen', to return)
def test_pop_front_leaving_empty_remaining_deque(self):
   self. deque.push back('Data')
   to return = self. deque.pop front()
   self.assertEqual('[ ]', str(self. deque))
def test pop front leaving empty length(self):
   self. deque.push back('Data')
   to_return = self.__deque.pop_front()
   self.assertEqual(0, len(self. deque))
def test pop front leaving one return value(self):
   self. deque.push front('Yangchen')
   self.__deque.push_front('Ye')
   to_return = self.__deque.pop_front()
   self.assertEqual('Ye', to return)
def test_pop_front_leaving_one_remaining_deque(self):
   self. deque.push back('Data')
   self.__deque.push_front('Structure')
   to return = self. deque.pop front()
   self.assertEqual('[ Data ]', str(self.__deque))
def test pop front leaving one length(self):
   self.__deque.push_back('Data')
   self.__deque.push_back('Structure')
   to_return = self.__deque.pop_front()
   self.assertEqual(1, len(self. deque))
def test pop back empty return value(self):
   to return = self. deque.pop back()
   self.assertEqual(None, to return)
```

```
def test pop back empty remaining deque(self):
   to return = self. deque.pop back()
   self.assertEqual('[ ]', str(self. deque))
def test pop back empty length(self):
   to_return = self.__deque.pop_back()
   self.assertEqual(0, len(self. deque))
def test_pop_back_leaving_empty_return_value(self):
   self. deque.push front('Yangchen')
   to return = self.__deque.pop_back()
   self.assertEqual('Yangchen', to return)
def test pop back leaving empty remaining deque(self):
   self.__deque.push_back('Data')
   to return = self. deque.pop back()
   self.assertEqual('[ ]', str(self.__deque))
def test pop back leaving empty length(self):
   self. deque.push back('Data')
   to_return = self.__deque.pop_back()
   self.assertEqual(0, len(self. deque))
def test_pop_back_leaving_one_return_value(self):
   self.__deque.push_front('Yangchen')
   self. deque.push front('Ye')
   to_return = self.__deque.pop_back()
   self.assertEqual('Yangchen', to return)
def test pop back leaving one remaining deque(self):
   self.__deque.push_back('Data')
   self. deque.push front('Structure')
   to_return = self.__deque.pop_back()
   self.assertEqual('[ Structure ]', str(self. deque))
def test pop back leaving one length(self):
   self.__deque.push_back('Data')
   self.__deque.push_back('Structure')
   to_return = self.__deque.pop_back()
   self.assertEqual(1, len(self.__deque))
def test pop front leaving empty push front(self):
   self. deque.push front('Data')
   to return = self. deque.pop front()
   self. deque.push front('Structure')
```

```
self.assertEqual('[ Structure ]', str(self. deque))
def test pop front leaving empty push back(self):
   self. deque.push front('Data')
   to_return = self.__deque.pop_front()
   self. deque.push back('Structure')
   self.assertEqual('[ Structure ]', str(self. deque))
def test pop front leaving one push front(self):
   self.__deque.push_front('Data')
   self.__deque.push_front('Structure')
   to return = self. deque.pop front()
   self.__deque.push_front('Ye')
   self.assertEqual('[ Ye, Data ]', str(self.__deque))
def test_pop_front_leaving_one_push_back(self):
   self.__deque.push_front('Data')
   self. deque.push front('Structure')
   to_return = self.__deque.pop_front()
   self. deque.push back('Ye')
   self.assertEqual('[ Data, Ye ]', str(self. deque))
def test pop back leaving empty push front(self):
   self. deque.push front('Data')
   to_return = self.__deque.pop_back()
   self. deque.push front('Structure')
   self.assertEqual('[ Structure ]', str(self. deque))
def test_pop_back_leaving_empty_push_back(self):
   self. deque.push front('Data')
   to_return = self.__deque.pop_back()
   self. deque.push back('Structure')
   self.assertEqual('[ Structure ]', str(self. deque))
def test pop back leaving one push front(self):
   self.__deque.push_front('Data')
   self.__deque.push_front('Structure')
   to return = self. deque.pop back()
   self. deque.push front('Ye')
   self.assertEqual('[ Ye, Structure ]', str(self.__deque))
def test pop back leaving one push back(self):
   self.__deque.push_front('Data')
   self. deque.push front('Structure')
   to return = self. deque.pop back()
   self. deque.push back('Ye')
```

```
self.assertEqual('[ Structure, Ye ]', str(self. deque))
def test peek front empty return value(self):
   to_return = self.__deque.peek_front()
   self.assertEqual(None, to return)
def test peek front empty remaining deque(self):
   to return = self. deque.peek front()
   self.assertEqual('[ ]', str(self.__deque))
def test peek front empty length(self):
   to return = self. deque.peek front()
   self.assertEqual(0, len(self. deque))
def test peek front one return value(self):
   self.__deque.push_front('Yangchen')
   to return = self. deque.peek front()
   self.assertEqual('Yangchen', to return)
def test peek front one remaining deque(self):
   self. deque.push front('Ye')
   to_return = self.__deque.peek_front()
   self.assertEqual('[ Ye ]', str(self. deque))
def test peek front one length(self):
   self. deque.push front('Ye')
   to return = self. deque.peek front()
   self.assertEqual(1, len(self.__deque))
def test peek front two return value(self):
   self.__deque.push_front('Data')
   self.__deque.push_front('Structure')
   to return = self. deque.peek front()
   self.assertEqual('Structure', to return)
def test_peek_front_two_remaining_deque(self):
   self.__deque.push_front('Data')
   self. deque.push front('Structure')
   to retuen = self. deque.peek front()
   self.assertEqual('[ Structure, Data ]', str(self.__deque))
def test peek front two length(self):
   self.__deque.push_front('Data')
   self. deque.push front('Structure')
   to retuen = self. deque.peek front()
   self.assertEqual(2, len(self. deque))
```

```
def test_peek_back_empty_return_value(self):
   to return = self. deque.peek back()
   self.assertEqual(None, to return)
def test peek back empty remaining deque(self):
   to_return = self.__deque.peek_back()
   self.assertEqual('[ ]', str(self. deque))
def test peek back empty length(self):
   to return = self. deque.peek back()
   self.assertEqual(0, len(self. deque))
def test peek back one return value(self):
   self. deque.push front('Yangchen')
   to_return = self.__deque.peek_back()
   self.assertEqual('Yangchen', to return)
def test peek back one remaining deque(self):
   self. deque.push front('Ye')
   to return = self. deque.peek back()
   self.assertEqual('[ Ye ]', str(self. deque))
def test peek back one length(self):
   self.__deque.push_front('Ye')
   to_return = self.__deque.peek_back()
   self.assertEqual(1, len(self. deque))
def test_peek_back_two_return_value(self):
   self. deque.push front('Data')
   self. deque.push front('Structure')
   to_return = self.__deque.peek_back()
   self.assertEqual('Data', to return)
def test peek back two remaining deque(self):
   self.__deque.push_front('Data')
   self.__deque.push_front('Structure')
   to retuen = self. deque.peek back()
   self.assertEqual('[ Structure, Data ]', str(self. deque))
def test peek back two length(self):
   self.__deque.push_front('Data')
   self.__deque.push_front('Structure')
   to_retuen = self.__deque.peek_back()
   self.assertEqual(2, len(self. deque))
```

```
def test_peek_front_push_front_remaining_deque(self):
   self.__deque.push_front('Ye')
   to_return = self.__deque.peek front()
   self. deque.push front('Yangchen')
   self.assertEqual('[ Yangchen, Ye ]', str(self.__deque))
def test peek front push front length(self):
   self. deque.push front('Ye')
   to_return = self.__deque.peek_front()
   self.__deque.push_front('Yangchen')
   self.assertEqual(2, len(self. deque))
def test peek front push back remaining deque(self):
   self.__deque.push_front('Ye')
   to return = self. deque.peek front()
   self.__deque.push_back('Yangchen')
   self.assertEqual('[ Ye, Yangchen ]', str(self. deque))
def test peek front push back length(self):
   self. deque.push front('Ye')
   to return = self. deque.peek front()
   self. deque.push back('Yangchen')
   self.assertEqual(2, len(self. deque))
def test_peek_back_push_front_remaining_deque(self):
   self. deque.push front('Ye')
   to return = self. deque.peek back()
   self.__deque.push_front('Yangchen')
   self.assertEqual('[ Yangchen, Ye ]', str(self.__deque))
def test peek back push front length(self):
   self.__deque.push_front('Ye')
   to return = self. deque.peek back()
   self.__deque.push_front('Yangchen')
   self.assertEqual(2, len(self.__deque))
def test peek back push back remaining deque(self):
   self. deque.push front('Ye')
   to_return = self.__deque.peek_back()
   self.__deque.push_back('Yangchen')
   self.assertEqual('[ Ye, Yangchen ]', str(self.__deque))
def test peek back push back length(self):
   self. deque.push front('Ye')
   to return = self. deque.peek back()
   self. deque.push back('Yangchen')
```

```
yye02_DSQ_Test.py.rtf
```

```
self.assertEqual(2, len(self. deque))
#testing stack
def test empty stack string(self):
   self.assertEqual('[ ]', str(self.__stack))
def test push empty(self):
   self. stack.push('Data')
   self.assertEqual('[ Data ]', str(self.__stack))
def test push one(self):
   self. stack.push('Data')
   self.__stack.push('Structure')
   self.assertEqual('[ Structure, Data ]', str(self.__stack))
def test empty stack length(self):
   self.assertEqual(0, len(self. stack))
def test one stack length(self):
   self. stack.push('Data')
   self.assertEqual(1, len(self. stack))
def test two stack length(self):
   self. stack.push('Data')
   self.__stack.push('Structure')
   self.assertEqual(2, len(self. stack))
def test_pop_empty_return_value(self):
   to_return = self.__stack.pop()
   self.assertEqual(None, to return)
def test_pop_empty_remaining_stack(self):
   to_return = self. stack.pop()
   self.assertEqual('[ ]', str(self. stack))
def test_pop_empty_length(self):
   to_return = self.__stack.pop()
   self.assertEqual(0, len(self. stack))
def test pop one return value(self):
   self.__stack.push('Yangchen')
   to return = self. stack.pop()
   self.assertEqual('Yangchen', to_return)
def test pop one remaining stack(self):
   self. stack.push('Yangchen')
```

```
to_return = self.__stack.pop()
   self.assertEqual('[ ]', str(self.__stack))
def test pop one length(self):
   self.__stack.push('Yangchen')
   to_return = self.__stack.pop()
   self.assertEqual(0, len(self. stack))
def test_pop_two_return_value(self):
   self.__stack.push('Yangchen')
   self. stack.push('Ye')
   to return = self. stack.pop()
   self.assertEqual('Ye', to_return)
def test pop two remaining stack(self):
   self.__stack.push('Ye')
   self. stack.push('Yangchen')
   to_return = self.__stack.pop()
   self.assertEqual('[ Ye ]', str(self. stack))
def test pop two length(self):
   self.__stack.push('Ye')
   self. stack.push('Yangchen')
   to return = self. stack.pop()
   self.assertEqual(1, len(self.__stack))
def test peek empty return value(self):
   to_return = self.__stack.peek()
   self.assertEqual(None, to return)
def test peek empty remaining stack(self):
   to_return = self.__stack.peek()
   self.assertEqual('[ ]', str(self. stack))
def test peek empty length(self):
   to_return = self.__stack.peek()
   self.assertEqual(0, len(self. stack))
def test_peek_one_return_value(self):
   self.__stack.push('Yangchen')
   to_return = self.__stack.peek()
   self.assertEqual('Yangchen', to return)
def test peek one remaining stack(self):
   self. stack.push('Yangchen')
   to_return = self.__stack.peek()
```

```
yye02_DSQ_Test.py.rtf
```

```
self.assertEqual('[ Yangchen ]', str(self. stack))
def test peek one length(self):
   self. stack.push('Yangchen')
   to_return = self.__stack.peek()
   self.assertEqual(1, len(self. stack))
def test peek two return value(self):
   self.__stack.push('Yangchen')
   self.__stack.push('Ye')
   to return = self. stack.peek()
   self.assertEqual('Ye', to return)
def test peek two remaining stack(self):
   self. stack.push('Ye')
   self.__stack.push('Yangchen')
   to return = self. stack.peek()
   self.assertEqual('[ Yangchen, Ye ]', str(self. stack))
def test peek two length(self):
   self.__stack.push('Ye')
   self.__stack.push('Yangchen')
   to_return = self.__stack.peek()
   self.assertEqual(2, len(self. stack))
#testing queue
def test empty queue string(self):
   self.assertEqual('[ ]', str(self.__queue))
def test enqueue empty(self):
   self. queue.enqueue('Data')
   self.assertEqual('[ Data ]', str(self.__queue))
def test enqueue one(self):
   self.__queue.enqueue('Data')
   self.__queue.enqueue('Structure')
   self.assertEqual('[ Data, Structure ]', str(self. queue))
def test_enqueue_two(self):
   self.__queue.enqueue('Data')
   self.__queue.enqueue('Structure')
   self. queue.enqueue('241')
   self.assertEqual('[ Data, Structure, 241 ]', str(self._ queue))
def test_dequeue_empty_return_value(self):
   to_return = self.__queue.dequeue()
```

```
self.assertEqual(None, to return)
  def test dequeue empty remaining queue(self):
     to_return = self.__queue.dequeue()
     self.assertEqual('[ ]', str(self. queue))
  def test dequeue_empty_length(self):
     to return = self.__queue.dequeue()
     self.assertEqual(0, len(self. queue))
  def test dequeue one return value(self):
     self. queue.enqueue('Yangchen')
     to_return = self.__queue.dequeue()
     self.assertEqual('Yangchen', to return)
  def test dequeue one remaining queue(self):
     self. queue.enqueue('Yangchen')
     to return = self. queue.dequeue()
     self.assertEqual('[ ]', str(self. queue))
  def test dequeue one length(self):
     self. queue.enqueue('Yangchen')
     to_return = self.__queue.dequeue()
     self.assertEqual(0, len(self. queue))
  def test dequeue two return value(self):
     self. queue.enqueue('Yangchen')
     self.__queue.enqueue('Ye')
     to_return = self.__queue.dequeue()
     self.assertEqual('Yangchen', to return)
  def test dequeue two remaining queue(self):
     self. queue.enqueue('Yangchen')
     self.__queue.enqueue('Ye')
     to_return = self.__queue.dequeue()
     self.assertEqual('[ Ye ]', str(self.__queue))
  def test dequeue empty length(self):
     self.__queue.enqueue('Yangchen')
     self.__queue.enqueue('Ye')
     to_return = self.__queue.dequeue()
     self.assertEqual(1, len(self. queue))
if name == ' main ':
  unittest.main()
```

```
import time
from Stack import Stack
def Hanoi rec(n, s, a, d):
 print(n, s, a, d)
 # TODO replace pass with your base and recursive cases.
 if n == 0:
    d.push(s.pop())
 else:
    Hanoi_rec(n-1, s, d, a)
    d.push(s.pop())
    Hanoi_rec(n-1, a, s, d)
  print(n, s, a, d)
 print()
def Hanoi(n):
  source = Stack()
 dest = Stack()
  aux = Stack()
  i = n-1
 while i >= 0:
    source.push(i)
    i = i - 1
 Hanoi rec(n-1, source, aux, dest)
if name == ' main ':
 start = time.clock()
 n = 4
 Hanoi(n)
 end = time.clock()
 print('computed Hanoi(' + str(n) + ') in ' + str(end - start) + '
seconds.')
```

```
class Linked List:
     class Node:
          def init (self, val):
                # declare and initialize the private attributes
                # for objects of the Node class.
                self.element = val
                self.prev = None
                self.next = None
     def init (self):
          # declare and initialize the private attributes
          # for objects of the sentineled Linked List class
           self. header = self. Node(None)
          self.__trailer = self.__Node(None)
           self.__header.next = self.__trailer
           self. trailer.prev = self. header
          self.__size = 0
     def len (self):
          # return the number of value-containing nodes in
          # this list.
          return self. size
     def locate(self, index):
          #to find and return the node at the index position
          if index <= self.__size // 2:</pre>
                current node = self. header.next
                for k in range(index):
                     current node = current node.next
                return current node
          else:
                current_node = self.__trailer.prev
                for k in range(self. size - 1 - index, 0, -1):
                     current node = current node.prev
                return current node
     def append element(self, val):
          # increase the size of the list by one, and add a
          # node containing val at the new tail position. this
          # is the only way to add items at the tail position.
          new_node = self.__Node(val)
          new_node.prev = self.__trailer.prev
          new node.next = self. trailer
           self. trailer.prev.next = new node
```

```
self.__trailer.prev = new_node
           self. size = self. size + 1
     def insert element at(self, val, index):
          # assuming the head position (not the header node)
          # is indexed 0, add a node containing val at the
          # specified index. If the index is not a valid
          # position within the list, raise an IndexError
          # exception. This method cannot be used to add an
          # item at the tail position.
          if index < 0 or index >= self. size:
                raise IndexError
          current_node = self.__locate(index)
          predecessor = current node.prev
          new node = self. Node(val)
          new node.prev = predecessor
          new node.next =current node
          predecessor.next = new node
          current node.prev = new node
           self. size = self. size + 1
     def remove element at(self, index):
          # assuming the head position (not the header node)
          # is indexed 0, remove and return the value stored
          # in the node at the specified index. If the index
          # is invalid, raise an IndexError exception.
          if index < 0 or index >= self. size:
                raise IndexError
          current node = self. locate(index)
          predecessor = current node.prev
           successer = current_node.next
          predecessor.next = successer
          successer.prev = predecessor
          value = current node.element
          current node.element = None; current node.prev = None;
current node.next = None
           self. size = self. size - 1
          return value
     def get element at(self, index):
          # assuming the head position (not the header node)
          # is indexed 0, return the value stored in the node
          # at the specified index, but do not unlink it from
          # the list. If the specified index is invalid, raise
```

```
# an IndexError exception.
     if index < 0 or index >= self. size:
          raise IndexError
     current node = self. locate(index)
     return current node.element
def rotate left(self):
     # rotate the list left one position. Conceptual indices
     # should all decrease by one, except for the head, which
     # should become the tail. For example, if the list is
     # [ 5, 7, 9, -4 ], this method should alter it to
     # [ 7, 9, -4, 5 ]. This method should modify the list in
     # place and must not return a value.
     if self. size == 0:
          return
     else:
          rotated element = self.remove element at(∅)
          self.append element(rotated element)
def str (self):
     # return a string representation of the list's
     # contents. An empty list should appear as [ ].
     # A list with one element should appear as [ 5 ].
     # A list with two elements should appear as [ 5, 7 ].
     # You may assume that the values stored inside of the
     # node objects implement the str () method, so you
     # call str(val object) on them to get their string
     # representations.
     if self. size == 0:
          return '[ ]'
     else:
          result = '[ '
          current_node = self.__header.next
          while current node.next is not self. trailer:
                result = result + str(current node.element) + ', '
                current node = current node.next
          result = result + str(current node.element) + ' ]'
     return result
def iter (self):
     # initialize a new attribute for walking through your list
     # TODO insert your initialization code before the return
     # statement. do not modify the return statement.
     self.__iter_node = self.__header.next
```

```
return self
     def next (self):
          # using the attribute that you initialized in iter (),
          # fetch the next value and return it. If there are no more
          # values to fetch, raise a StopIteration exception.
          if self.__iter_node is self.__trailer:
                raise StopIteration
          else:
                to_return = self.__iter_node.element
                self. iter node = self. iter node.next
                return to return
if name == ' main ':
     # Your test code should go here. Be sure to look at cases
     # when the list is empty, when it has one element, and when
     # it has several elements. Do the indexed methods raise exceptions
     # when given invalid indices? Do they position items
     # correctly when given valid indices? Does the string
     # representation of your list conform to the specified format?
     # Does removing an element function correctly regardless of that
     # element's location? Does a for loop iterate through your list
     # from head to tail? Your writeup should explain why you chose the
     # test cases. Leave all test cases in your code when submitting.
          test list = Linked List()
          print(test list)
          print('test list has ' + str(len(test list)) + ' elements')
          #test append element at() method
          #should all work fine
          print()
          print('testing append')
          test list.append element(3)
          test list.append element(10)
          test list.append element(-9)
          test list.append element(None)
          test list.append element(0)
          test list.append element('CSCI241')
          #a linked list can have '0' and 'None'
          #without intefering with its methods.
          print(test list)
          print('test list has '+ str(len(test list)) + ' elements')
          print()
          #test insert element at() method
          print()
```

```
print('testing insert')
try:
#valid index. should work fine.
     test list.insert element at(3,0)
     test_list.insert_element_at(0,3)
     #linked list can have the same elements in different nodes
     test list.insert element at(23,2)
     test list.insert element at(None, len(test list)-1)
except IndexError:
     print('Error: Invalid Index')
print(test list)
print('test list has '+ str(len(test list)) + ' elements')
empty list = Linked List()
try:
#invalid index. should fail
     empty list.insert element at(35,0)
except IndexError:
     print('Successfully Detected: Invalid Index')
print(empty list)
print('empty list has '+ str(len(empty list)) + ' elements')
try:
#invalid index. should fail.
     test list.insert element at(30,-1)
     #cannot have negative index
except IndexError:
     print('Successfully Detected: Invalid Index')
print(test list)
print('test list has '+ str(len(test list)) + ' elements')
try:
#invalid index. should fail.
     test list.insert element at(24,len(test list))
     #len(linked list) is not a valid index. use append
except IndexError:
     print('Successfully Detected: Invalid Index')
print(test list)
print('test list has '+ str(len(test list)) + ' elements')
print()
#test iterator
print()
print('testing iterator')
for element in test list:
     print(element)
```

```
print()
#test remove element at() method
print()
print('testing remove')
try:
#should all work fine
     print(test list.remove element at(0))
     print(test list.remove element at(3))
     print(test list.remove element at(len(test list)-1))
except IndexError:
     print('Error: Invalid Index')
print(test list)
print('test_list has ' + str(len(test_list)) + ' elements')
try:
#should fail and print '[]', list is empty
     empty list.remove element at(0)
except IndexError:
     print('Successfully Detected: Invalid Index')
print(empty list)
print('emptye list has '+ str(len(empty list)) + ' elements')
try:
#invalid index. should fail
     test list.remove element at(-1)
except IndexError:
     print('Successfully Detected: Invalid Index')
print(test list)
print('test list has ' + str(len(test list)) + ' elements')
try:
#invalid index. should fail
     test list.remove element at(len(test list))
except IndexError:
     print('Successfully Detected: Invalid Index')
print(test list)
print('test list has ' + str(len(test list)) + ' elements')
print()
#test get element at() method
print()
print('testing get_element')
try:
#should all work fine
     for index in range(0,len(test list)):
```

```
print(test list.get element at(index))
           except IndexError:
                print('Error: Invalid Index')
           print(test list)
           print('test list has ' + str(len(test list)) + ' elements')
           #should not change the list
          try:
           #invalid index. should fail. empty list
                print(empty list.get element at(0))
           except IndexError:
                print('Successfully Detected: Invalid Index')
           print(empty list)
           print('empty list has ' + str(len(empty list)) + ' elements')
           try:
           #invalid index. should fail
                print(test list.get element at(-1))
           except IndexError:
                print('Successfully Detected: Invalid Index')
           print(test list)
           print('test_list has ' + str(len(test_list)) + ' elements')
          try:
           #invalid index. should fail
                print(test list.get element at(len(test list)))
           except IndexError:
                print('Successfully Detected: Invalid Index')
           print(test list)
           print('test list has ' + str(len(test list)) + ' elements')
           print()
           #test rotate left() method
           print()
           print('testing rotate')
           #should work fine
           test list.rotate left()
           print(test list)
           print('test_list has ' + str(len(test_list)) + ' elements')
           #should have no effect
           empty list.rotate left()
           print(empty list)
           print('empty list has ' + str(len(empty list)) + '
elements')
```

```
yye02_Linked_List_Deque.py.rtf
from Deque import Deque
from Linked_List import Linked_List
class Linked List Deque(Deque):
 def init (self):
    self. list = Linked List()
 def str (self):
    return str(self.__list)
 def len (self):
    return len(self. list)
 # DO NOT CHANGE ANYTHING ABOVE THIS LINE
 #I use the head position in the linked list as the front and
 #tail position in the list as the back.
 def push front(self, val):
    if len(self. list) == 0:
      self. list.append element(val)
      self. list.insert element at(val,∅)
 def pop front(self):
    if len(self. list) == 0:
      return
    return self. list.remove element at(0)
  def peek front(self):
    if len(self.__list) == 0:
      return
    else:
      return self. list.get element at(0)
 def push back(self, val):
    self.__list.append_element(val)
 def pop back(self):
    if len(self.__list) == 0:
      return
    return self. list.remove_element_at(len(self.__list) - 1)
 def peek back(self):
    if len(self.__list) == 0:
```

```
return
else:
    return self.__list.get_element_at(len(self.__list) - 1)
# Unit tests make the main section unneccessary.
#if __name__ == '__main__':
# pass
```

```
yye02_Queue.py.rtf

from Deque_Generator import get_deque

class Queue:

    def __init__(self):
        # TODO replace pass with your implementation.
        self.__dq = get_deque()

    def __str__(self):
        # TODO replace pass with your implementation.
        return str(self.__dq)

    def __len__(self):
        # TODO replace pass with your implementation.
        return len(self.__dq)
```

def enqueue(self, val):

self.__dq.push_back(val)

```
def dequeue(self):
    # TODO replace pass with your implementation.
    return self.__dq.pop_front()

# Unit tests make the main section unneccessary.
#if __name__ == '__main__':
# pass
```

TODO replace pass with your implementation.

```
from Deque_Generator import get_deque
class Stack:
 def __init__(self):
    # TODO replace pass with your implementation.
    self.__dq = get_deque()
  def str (self):
    # TODO replace pass with your implementation.
    return str(self. dq)
 def __len__(self):
    # TODO replace pass with your implementation.
    return len(self. dq)
 def push(self, val):
    # TODO replace pass with your implementation.
    self. dq.push front(val)
 def pop(self):
    # TODO replace pass with your implementation.
    return self.__dq.pop_front()
  def peek(self):
    # TODO replace pass with your implementation.
    return self.__dq.peek_front()
# Unit tests make the main section unneccessary.
#if __name__ == '__main__':
# pass
```

```
test add at negative index ignore ( main .Linked List Tester) ... ok
test add at one past index ignore ( main .Linked List Tester) ...
test add at zero index empty ignore ( main .Linked List Tester) ...
test add head empty ( main .Linked List Tester) ...
test_add_head_with_one ( main .Linked List Tester) ...
test add head with two ( main .Linked List Tester) ...
test add middle with two ( main .Linked List Tester) ...
test add second of four ( main .Linked List Tester) ...
test add tail with one ( main .Linked List Tester) ...
test add tail with two ( main .Linked List Tester) ...
test add third of four ( main .Linked List Tester) ...
test empty iterator ( main .Linked List Tester) ...
test_empty_list_string (__main__.Linked_List_Tester) ...
test get at negative index ignore ( main .Linked List Tester) ...
test get at one past index ignore ( main .Linked List Tester) ...
test get at zero index empty ignore ( main .Linked List Tester) ...
test get empty length ( main .Linked List Tester) ...
test get head with one element ( main .Linked List Tester) ...
test get head with one element length ( main .Linked List Tester) ...
test get head with one element remaining ( main .Linked List Tester)
. . .
ok
test get middle with three elements ( main .Linked List Tester) ...
test get middle with three elements length ( main .Linked List Tester)
ok
test get middle with three elements remaining
( main .Linked List Tester)
ok
test get one length ( main .Linked List Tester) ...
ok
test get tail with two elements ( main .Linked List Tester) ...
test get tail with two elements length ( main .Linked List Tester) ...
ok
```

```
test get tail with two elements remaining ( main .Linked List Tester)
. . .
οk
test get three length insert ( main .Linked List Tester) ...
test get two length append ( main .Linked List Tester) ...
test get two length insert ( main .Linked List Tester) ...
test multiple iterator ( main .Linked List Tester) ...
test one iterator ( main .Linked List Tester) ...
test removeHeadLeavingOneLength ( main .Linked List Tester) ...
test remove at negative index ignore ( main .Linked List Tester) ...
test_remove_at_one_past_index_ignore (__main__.Linked_List_Tester) ...
test remove at zero index empty ignore ( main .Linked List Tester) ...
test remove head leaving one remaining list ( main .Linked List Tester)
ok
test remove head leaving one returned value ( main .Linked List Tester)
ok
test remove head leaving zero length ( main .Linked List Tester) ...
test remove head leaving zero remaining list
( main .Linked List Tester) ...
ok
test remove head leaving zero returned value
( main .Linked List Tester) ...
test_remove_middle_leaving_two length ( main .Linked List Tester) ...
test remove middle leaving two remaining list
( main .Linked List Tester) ...
test remove middle leaving two returned value
( main .Linked List Tester) ...
test remove tail leaving one length ( main .Linked List Tester) ...
test remove tail leaving one remaining list ( main .Linked List Tester)
ok
test remove tail leaving one returned value ( main .Linked List Tester)
test rotate left empty ( main .Linked List Tester) ...
test rotate left with one ( main .Linked List Tester) ...
```

```
ok
test_rotate_left_with_three (__main__.Linked_List_Tester) ...
ok
test_rotate_left_with_two (__main__.Linked_List_Tester) ...
ok

Ran 51 tests in 0.008s

OK
```

```
test d empty len ( main .DSQTester) ... ok
test d empty str ( main .DSQTester) ...
test d len twobb ( main .DSQTester) ... ok
test d len twobf ( main .DSQTester) ...
test d len twofb ( main .DSQTester) ...
test d len twoff ( main .DSQTester) ...
test d one len ( main .DSQTester) ...
test d one str ( main .DSQTester) ...
test d oneb len ( main .DSQTester) ...
test d oneb str ( main .DSQTester) ...
ok
test d onef len ( main .DSQTester) ...
test d onef str ( main .DSQTester) ...
test d peekb empty len ( main .DSQTester) ...
test d peekb empty return ( main .DSQTester) ...
test d peekb empty str ( main .DSQTester) ...
test d peekb oneb len ( main .DSQTester) ...
test d peekb oneb return ( main .DSQTester) ...
test_d_peekb_oneb str ( main .DSQTester) ...
ok
test d peekb onef return ( main .DSQTester) ...
test d peekb twobb return ( main .DSQTester) ...
test d peekb twobf return ( main .DSQTester) ...
test d peekb twofb return ( main .DSQTester) ...
ok
test d peekb twoff return ( main .DSQTester) ...
test d peekf empty len ( main .DSQTester) ...
test d peekf empty return ( main .DSQTester) ... ok
test_d_peekf_empty_str (__main__.DSQTester) ...
test d peekf oneb len ( main .DSQTester) ...
test d peekf oneb return ( main .DSQTester) ...
test d peekf oneb str ( main .DSQTester) ...
```

```
ok
test d peekf onef len ( main .DSQTester) ...
test d peekf onef return ( main .DSQTester) ...
test d peekf onef str ( main .DSQTester) ...
test d peekf twobb return ( main .DSQTester) ...
test d peekf twobf return ( main .DSQTester) ...
ok
test d peekf twofb return ( main .DSQTester) ...
test d peekf twoff return ( main .DSQTester) ...
test d popb empty len ( main .DSQTester) ...
ok
test d popb empty return ( main .DSQTester) ...
test d popb empty str ( main .DSQTester) ...
test d popb oneb len ( main .DSQTester) ...
test d popb oneb return ( main .DSQTester) ...
ok
test d popb oneb str ( main .DSQTester) ...
ok
test d popb onef len ( main .DSQTester) ...
test d popb onef return ( main .DSQTester) ...
test d popb onef str ( main .DSQTester) ...
test d popb twobb return ( main .DSQTester) ...
test d popb twobf return ( main .DSQTester) ...
test d popb twofb return ( main .DSQTester) ...
test d popb twoff return ( main .DSQTester) ...
test d popf empty len ( main .DSQTester) ...
test_d_popf_empty_return (__main__.DSQTester) ...
test d popf empty str ( main .DSQTester) ...
test d popf oneb len ( main .DSQTester) ...
test d popf oneb return ( main .DSQTester) ...
test d popf oneb str ( main .DSQTester) ...
test d popf onef len ( main .DSQTester) ...
```

```
ok
test d popf onef return ( main .DSQTester) ...
test d popf onef str ( main .DSQTester) ...
test d popf twobb return ( main .DSQTester) ...
test d popf twobf return ( main .DSQTester) ...
test d popf twofb return ( main .DSQTester) ...
ok
test d popf twoff return ( main .DSQTester) ...
test d str twobb ( main .DSQTester) ...
test d str twobf ( main .DSQTester) ...
test d str twofb ( main .DSQTester) ...
test d str twoff ( main .DSQTester) ...
test q dequeue1 two len ( main .DSQTester) ...
test q dequeuel two return ( main .DSQTester) ...
test q dequeuel two str ( main .DSQTester) ...
ok
test q dequeue2 two len ( main .DSQTester) ...
test q dequeue2 two return ( main .DSQTester) ...
test q dequeue2 two str ( main .DSQTester) ...
test q dequeue3 two len ( main .DSQTester) ...
test q dequeue3 two return ( main .DSQTester) ...
test q dequeue3 two str ( main .DSQTester) ...
test q dequeue empty len ( main .DSQTester) ... ok
test q dequeue empty return ( main .DSQTester) ...
test q dequeue empty str ( main .DSQTester) ...
test_q_dequeue_one len ( main .DSQTester) ...
test q dequeue one return ( main .DSQTester) ...
test_q_dequeue_one_str ( main .DSQTester) ...
ok
test q three return ( main .DSQTester) ...
test q two len ( main .DSQTester) ...
ok
```

```
test q two str ( main .DSQTester) ...
ok
test s peek empty len ( main .DSQTester) ...
test s peek empty return ( main .DSQTester) ... ok
test_s_peek_empty_str (__main .DSQTester) ...
test s peek one len ( main .DSQTester) ...
test s peek one return ( main .DSQTester) ...
ok
test s peek one str ( main .DSQTester) ...
test s peek two len ( main .DSQTester) ...
test s peek two return ( main .DSQTester) ...
ok
test_s_peek_two_str (__main__.DSQTester) ...
ok
test s pop1 two len ( main .DSQTester) ...
test s pop1 two return ( main .DSQTester) ...
test_s_pop1_two_str (__main__.DSQTester) ...
ok
test s pop2 two len ( main .DSQTester) ...
ok
test s pop2 two return ( main .DSQTester) ...
test s pop2 two str ( main .DSQTester) ...
test s pop3 two len ( main .DSQTester) ...
test s pop3 two return ( main .DSQTester) ...
test s pop3 two str ( main .DSQTester) ...
test s pop empty len ( main .DSQTester) ...
test s pop empty return ( main .DSQTester) ...
ok
test s pop empty str ( main .DSQTester) ...
test s pop one len ( main .DSQTester) ...
test s pop one return ( main .DSQTester) ...
test s pop one str ( main .DSQTester) ...
test s three return ( main .DSQTester) ...
test s two len ( main .DSQTester) ...
test s two str ( main .DSQTester) ...
```

```
ok
test z Hanoi ( main .DSQTester) ...
Ran 112 tests in 0.009s
OK
3 [ 0, 1, 2, 3 ] [ ] [ ]
2 [ 0, 1, 2, 3 ] [ ] [ ]
1 [ 0, 1, 2, 3 ] [ ] [ ]
0 [ 0, 1, 2, 3 ] [ ] [ ]
0 [ 1, 2, 3 ] [ ] [ 0 ]
0 [ 0 ] [ 2, 3 ] [ 1 ]
0 [ ] [ 2, 3 ] [ 0, 1 ]
1 [ 2, 3 ] [ ] [ 0, 1 ]
1 [ 0, 1 ] [ 3 ] [ 2 ]
0 [ 0, 1 ] [ 2 ] [ 3 ]
0 [ 1 ] [ 2 ] [ 0, 3 ]
0 [ 0, 3 ] [ ] [ 1, 2 ]
0 [ 3 ] [ ] [ 0, 1, 2 ]
1 [ ] [ 3 ] [ 0, 1, 2 ]
2 [ 3 ] [ ] [ 0, 1, 2 ]
2 [ 0, 1, 2 ] [ ] [ 3 ]
1 [ 0, 1, 2 ] [ 3 ] [ ]
0 [ 0, 1, 2 ] [ ] [ 3 ]
0 [ 1, 2 ] [ ] [ 0, 3 ]
0 [ 0, 3 ] [ 2 ] [ 1 ]
0 [ 3 ] [ 2 ] [ 0, 1 ]
1 [ 2 ] [ 3 ] [ 0, 1 ]
1 [ 0, 1 ] [ ] [ 2, 3 ]
0 [ 0, 1 ] [ 2, 3 ] [ ]
0 [ 1 ] [ 2, 3 ] [ 0 ]
0 [ 0 ] [ ] [ 1, 2, 3 ]
0 [ ] [ ] [ 0, 1, 2, 3 ]
1 [ ] [ ] [ 0, 1, 2, 3 ]
2 [ ] [ ] [ 0, 1, 2, 3 ]
3 [ ] [ ] [ 0, 1, 2, 3 ]
```

```
test d empty len ( main .DSQTester) ... ok
test d empty str ( main .DSQTester) ...
test d len twobb ( main .DSQTester) ...
test d len twobf ( main .DSQTester) ...
test d len twofb ( main .DSQTester) ...
test d len twoff ( main .DSQTester) ...
ok
test d one len ( main .DSQTester) ...
test d one str ( main .DSQTester) ...
test d oneb len ( main .DSQTester) ...
ok
test_d_oneb_str (__main__.DSQTester) ...
ok
test d onef len ( main .DSQTester) ...
test d onef str ( main .DSQTester) ...
test_d_peekb_empty_len (__main__.DSQTester) ...
ok
test d peekb empty return ( main .DSQTester) ...
ok
test d peekb empty str ( main .DSQTester) ...
test d peekb oneb len ( main .DSQTester) ...
test d peekb oneb return ( main .DSQTester) ...
test d peekb oneb str ( main .DSQTester) ...
test d peekb onef return ( main .DSQTester) ...
test d peekb twobb return ( main .DSQTester) ...
test d peekb twobf return ( main .DSQTester) ...
ok
test d peekb twofb return ( main .DSQTester) ...
test d peekb twoff return ( main .DSQTester) ...
test d peekf empty len ( main .DSQTester) ...
test d peekf empty return ( main .DSQTester) ...
test d peekf empty str ( main .DSQTester) ...
test d peekf oneb len ( main .DSQTester) ...
test d peekf oneb return ( main .DSQTester) ...
```

```
ok
test d peekf oneb str ( main .DSQTester) ...
test d peekf onef len ( main .DSQTester) ...
test d peekf onef return ( main .DSQTester) ...
test d peekf onef str ( main .DSQTester) ...
test d peekf twobb return ( main .DSQTester) ...
ok
test d peekf twobf return ( main .DSQTester) ...
test d peekf twofb return ( main .DSQTester) ...
test d peekf twoff return ( main .DSQTester) ...
ok
test_d_popb_empty_len (__main__.DSQTester) ...
test d popb empty return ( main .DSQTester) ...
test d popb empty str ( main .DSQTester) ...
test d popb oneb len ( main .DSQTester) ...
ok
test d popb oneb return ( main .DSQTester) ...
ok
test d popb oneb str ( main .DSQTester) ...
test d popb onef len ( main .DSQTester) ...
test d popb onef return ( main .DSQTester) ...
test d popb onef str ( main .DSQTester) ...
test d popb twobb return ( main .DSQTester) ...
test d popb twobf return ( main .DSQTester) ...
test d popb twofb return ( main .DSQTester) ...
test d popb twoff return ( main .DSQTester) ...
test d popf empty len ( main .DSQTester) ...
test d popf empty return ( main .DSQTester) ...
test d popf empty str ( main .DSQTester) ...
test d popf oneb len ( main .DSQTester) ...
test d popf oneb return ( main .DSQTester) ...
test d popf oneb str ( main .DSQTester) ...
```

```
ok
test d popf onef len ( main .DSQTester) ...
test d popf onef return ( main .DSQTester) ...
test d popf onef str ( main .DSQTester) ...
test d popf twobb return ( main .DSQTester) ...
test d popf twobf return ( main .DSQTester) ...
ok
test d popf twofb return ( main .DSQTester) ...
test d popf twoff return ( main .DSQTester) ...
test d str twobb ( main .DSQTester) ...
ok
test d str twobf ( main .DSQTester) ...
test d str twofb ( main .DSQTester) ...
test d str twoff ( main .DSQTester) ...
test_q_dequeue1_two_len (__main__.DSQTester) ...
test q dequeuel two return ( main .DSQTester) ...
ok
test q dequeuel two str ( main .DSQTester) ...
test q dequeue2 two len ( main .DSQTester) ...
test q dequeue2 two return ( main .DSQTester) ...
test q dequeue2 two str ( main .DSQTester) ...
test q dequeue3 two len ( main .DSQTester) ...
test q dequeue3 two return ( main .DSQTester) ...
test q dequeue3 two str ( main .DSQTester) ...
test q dequeue empty len ( main .DSQTester) ...
test q dequeue empty return ( main .DSQTester) ...
test q dequeue empty str ( main .DSQTester) ...
test q dequeue one len ( main .DSQTester) ...
test q dequeue one return ( main .DSQTester) ...
test_q_dequeue_one str ( main .DSQTester) ...
test q three return ( main .DSQTester) ...
```

```
ok
test q two len ( main .DSQTester) ...
test q two str ( main .DSQTester) ...
test s peek empty len ( main .DSQTester) ...
test s peek empty return ( main .DSQTester) ...
ok
test s peek empty str ( main .DSQTester) ...
ok
test s peek one len ( main .DSQTester) ...
test s peek one return ( main .DSQTester) ...
test s peek one str ( main .DSQTester) ...
ok
test s peek two len ( main .DSQTester) ...
ok
test s peek two return ( main .DSQTester) ...
test s peek two str ( main .DSQTester) ...
test s pop1 two len ( main .DSQTester) ...
ok
test s pop1 two return ( main .DSQTester) ...
ok
test s pop1 two str ( main .DSQTester) ...
test s pop2 two len ( main .DSQTester) ...
test s pop2 two return ( main .DSQTester) ...
ok
test s pop2 two str ( main .DSQTester) ...
test s pop3 two len ( main .DSQTester) ...
test s pop3 two return ( main .DSQTester) ...
test s pop3 two str ( main .DSQTester) ...
ok
test s pop empty len ( main .DSQTester) ...
test s pop empty return ( main .DSQTester) ...
test s pop empty str ( main .DSQTester) ...
test s pop one len ( main .DSQTester) ...
ok
test s pop one return ( main .DSQTester) ...
test s pop one str ( main .DSQTester) ...
test s three return ( main .DSQTester) ...
```

```
ok
test s two len ( main .DSQTester) ...
test s two str ( main .DSQTester) ...
test z Hanoi ( main .DSQTester) ...
Ran 112 tests in 0.020s
OK
3 [ 0, 1, 2, 3 ] [ ] [ ]
2 [ 0, 1, 2, 3 ] [ ] [ ]
1 [ 0, 1, 2, 3 ] [ ] [ ]
0 [ 0, 1, 2, 3 ] [ ] [ ]
0 [ 1, 2, 3 ] [ ] [ 0 ]
0 [ 0 ] [ 2, 3 ] [ 1 ]
0 [ ] [ 2, 3 ] [ 0, 1 ]
1 [ 2, 3 ] [ ] [ 0, 1 ]
1 [ 0, 1 ] [ 3 ] [ 2 ]
0 [ 0, 1 ] [ 2 ] [ 3 ]
0 [1][2][0,3]
0 [ 0, 3 ] [ ] [ 1, 2 ]
0 [ 3 ] [ ] [ 0, 1, 2 ]
1 [ ] [ 3 ] [ 0, 1, 2 ]
2 [ 3 ] [ ] [ 0, 1, 2 ]
2 [ 0, 1, 2 ] [ ] [ 3 ]
1 [ 0, 1, 2 ] [ 3 ] [ ]
0 [ 0, 1, 2 ] [ ] [ 3 ]
0 [ 1, 2 ] [ ] [ 0, 3 ]
0 [ 0, 3 ] [ 2 ] [ 1 ]
0 [ 3 ] [ 2 ] [ 0, 1 ]
1 [ 2 ] [ 3 ] [ 0, 1 ]
1 [ 0, 1 ] [ ] [ 2, 3 ]
0 [ 0, 1 ] [ 2, 3 ] [ ]
0 [ 1 ] [ 2, 3 ] [ 0 ]
0 [ 0 ] [ ] [ 1, 2, 3 ]
0 [ ] [ ] [ 0, 1, 2, 3 ]
1 [ ] [ ] [ 0, 1, 2, 3 ]
```

2 [] [] [0, 1, 2, 3]

3 [] [] [0, 1, 2, 3]

yye02_delimiter_results.txt

```
Testing delimiter check for yye02
Actual output preceeds expected output.
{}[]()
The file contains balanced delimiters.
The file contains balanced delimiters.
([good])
{
              foo(
        ba)r}
The file contains balanced delimiters.
(]
The file contains IMBALANCED DELIMITERS.
([[[]]])
The file contains IMBALANCED DELIMITERS.
```

The file contains IMBALANCED DELIMITERS.