

**Algorithm  $\text{gen}'(1^k)$ :**

- for**  $i = 1 \dots q$  **do**
- $(sk_i, pk_i) := \text{gen}(1^k)$
- $sk := sk_1 \parallel \dots \parallel sk_q$
- $pk := pk_1 \parallel \dots \parallel pk_q$
- return**  $(sk, pk)$

**Algorithm  $\text{sgn}'(sk, m)$ :**

- unpack  $sk := sk_1 \parallel \dots \parallel sk_q$
- $i :=$  number of calls of  $\text{sgn}'$
- return**  $i \parallel \text{sgn}(sk_i, m)$

**Algorithm  $\text{vrf}'(pk, m, \sigma)$ :**

- unpack  $pk := pk_1 \parallel \dots \parallel pk_q$
- unpack  $\sigma := i \parallel \eta$
- return**  $\text{vrf}(pk_i, m, \eta)$