$\exists$ CM attack on  $\Sigma$ 

 $\triangleright B.m, B.\sigma$ return  $vrf(pk, B.m, B.\sigma)$  $\land (\forall i \in [l], \ B.m \neq B.m_i)$  ► J.pk►  $J.\sigma_1, \ldots, J.\sigma_l$ sample  $a \in \{0, 1\}^k$ sample  $b \in \{0, 1\}^k \setminus \{a\}$  pk' := J.pk || a || bfor  $i = 1 \ldots l$ :

if  $m_i = a$  then fail
else  $\sigma'_i := \sigma_i || \mathbf{0}$ ► pk'►  $\sigma'_1, \ldots, \sigma'_l$ forge  $(m, \sigma')$ unpack  $\sigma' =: \sigma || \eta$