select m_1, \ldots, m_ℓ $ightharpoonup m_1, \ldots, m_{\ell}$

 $\triangleright pk, \sigma_1, \ldots, \sigma_\ell$ sample $a \in \{0, 1\}^k$ sample $b \in \{0, 1\}^k \setminus \{a\}$ pk' := pk||a||bfor $i = 1 \dots \ell$: if $m_i = a$ then fail else $\sigma_i' := \sigma_i || \mathbf{0}$

 $\triangleright pk'$ $\triangleright \sigma'_1, \ldots, \sigma'_{\ell}$ forge (m, σ')

 $\exists CM \text{ attack on } \Sigma'$

 $\triangleright m, \sigma$ return $vrf(pk, m, \sigma)$

 $ightharpoonup m_1, \ldots, m_\ell$

for $i = 1 \dots \ell$:

 $(sk, pk) := gen(1^k)$

 $\sigma_i := \operatorname{sgn}(sk, m_i)$

 $\land (\forall i \in [\ell], \ m \neq m_i)$

 \blacktriangleright (m, σ')

unpack $\sigma' =: \sigma || \eta$

virtual A

 \exists CM attack on Σ