

Algorithm $\text{gen}'(1^k)$:

- ┌ $(sk_0, pk_0) := \text{gen}(1^k)$
- └ **return** (sk_0, pk_0)

Algorithm $\text{sgn}'(sk_0, m)$:

- ┌ $i := \text{number of calls to } \text{sgn}'$
- ┌ $(sk_i, pk_i) := \text{gen}(1^k)$
- ┌ $\eta_i := \text{sgn}(sk_{i-1}, m_i || pk_i)$
- ┌ memorise $m_i || pk_i || \eta_i$
- └ **return** $(m_j || pk_j || \eta_j)_{1 \leq j \leq i}$

Algorithm $\text{vrf}'(pk_0, m, \sigma)$:

- ┌ unpack $\sigma =: (m_j || pk_j || \eta_j)_{1 \leq j \leq i}$
- ┌ **if** $m \neq m_i$ **then**
- ┌ ┌ **return** false
- ┌ **for** $j = 1 \dots i$ **do**
- ┌ ┌ **if** $\neg \text{vrf}(pk_{j-1}, m_j || pk_j, \eta_j)$ **then**
- ┌ ┌ ┌ **return** false
- └ **return** true