

Scheduling in a Real-time Network-on-Chip

Period minimization using metaheuristics

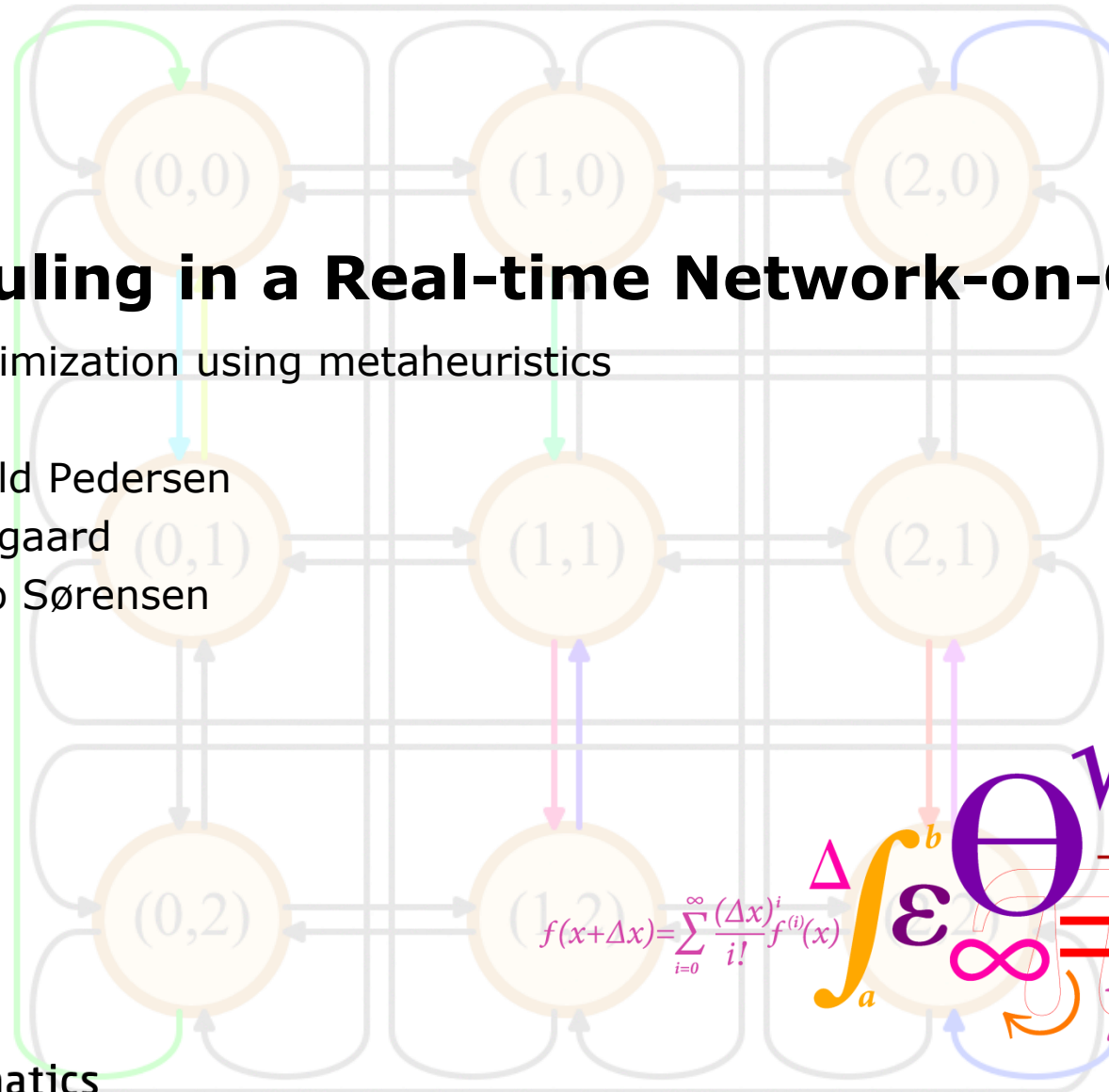
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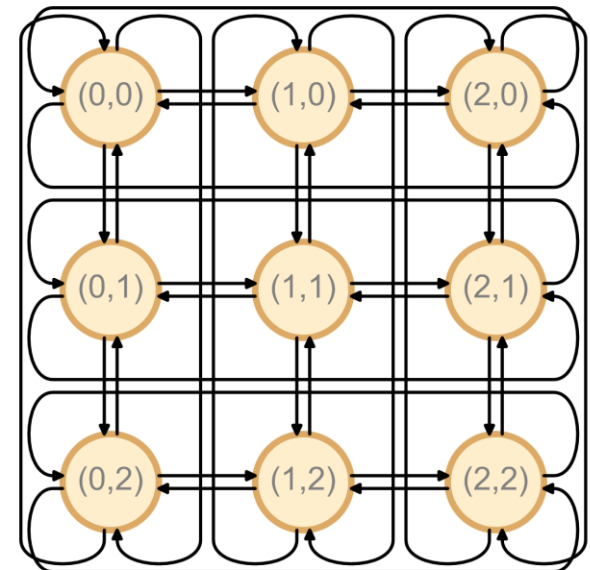
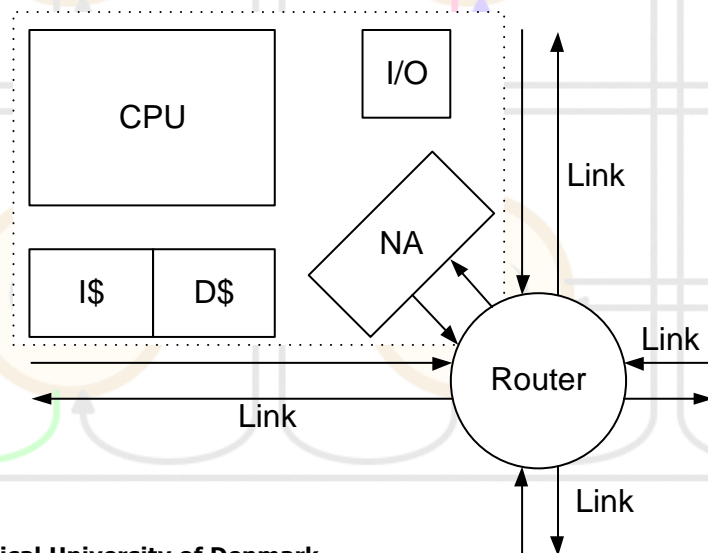
$$f(x+\Delta x) = \sum_{i=0}^{\infty} \frac{(\Delta x)^i}{i!} f^{(i)}(x)$$

$$\int_a^b \epsilon \Theta^{\sqrt{17}} + \Omega \int \delta e^{i\pi} = \{2.7182818284\}$$

$$\infty = \chi^2 \sum! >$$

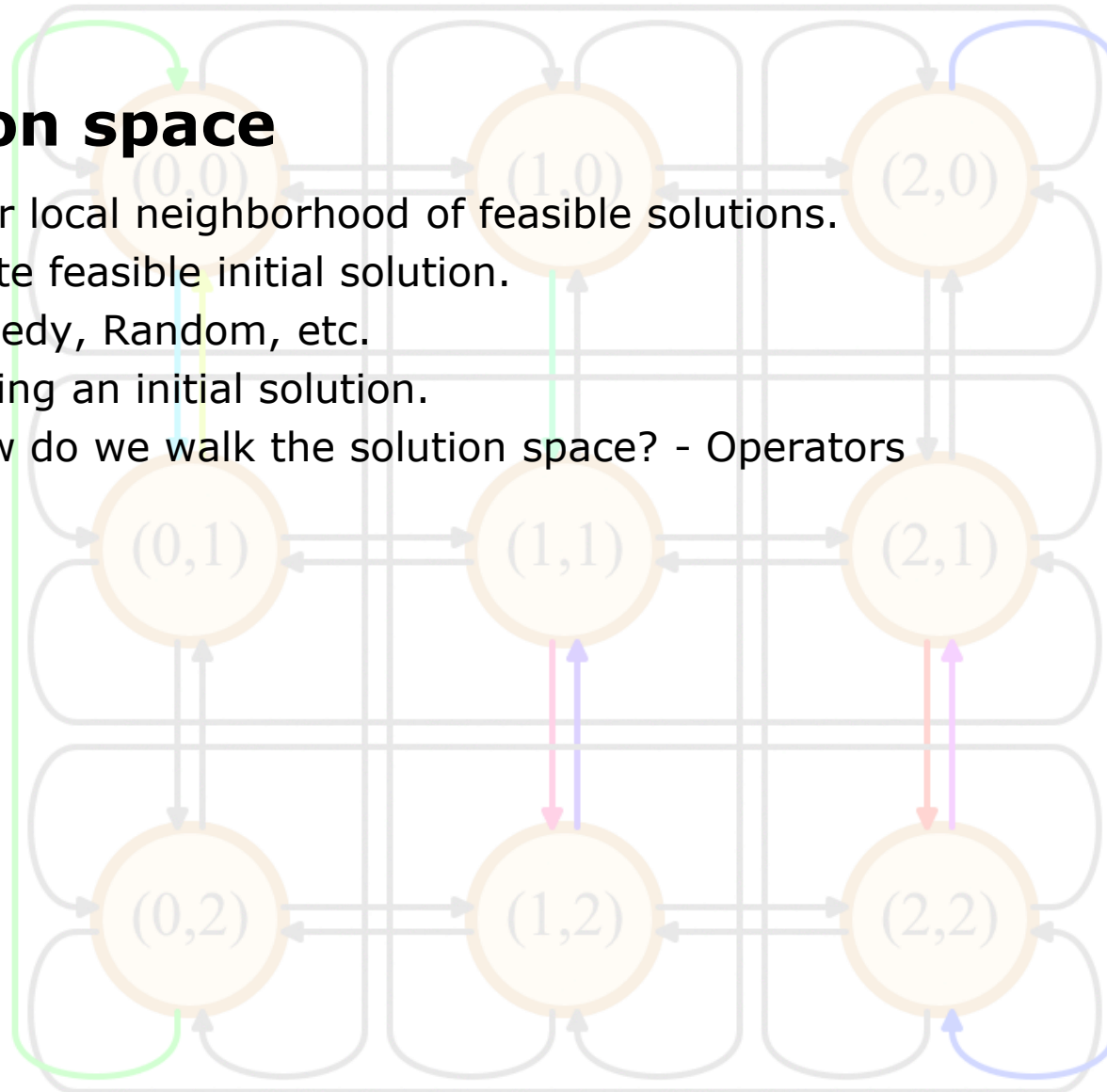
Problem domain

- Real-time Network-on-Chip
- Inter-processor communication
- No buffering
- Application specific
- NP-complete: Integer multi-commodity flow problem
- Minimizing schedule period



Solution space

- No clear local neighborhood of feasible solutions.
- Generate feasible initial solution.
 - Greedy, Random, etc.
- Improving an initial solution.
 - How do we walk the solution space? - Operators



Operators

Destroy and rebuild paths.

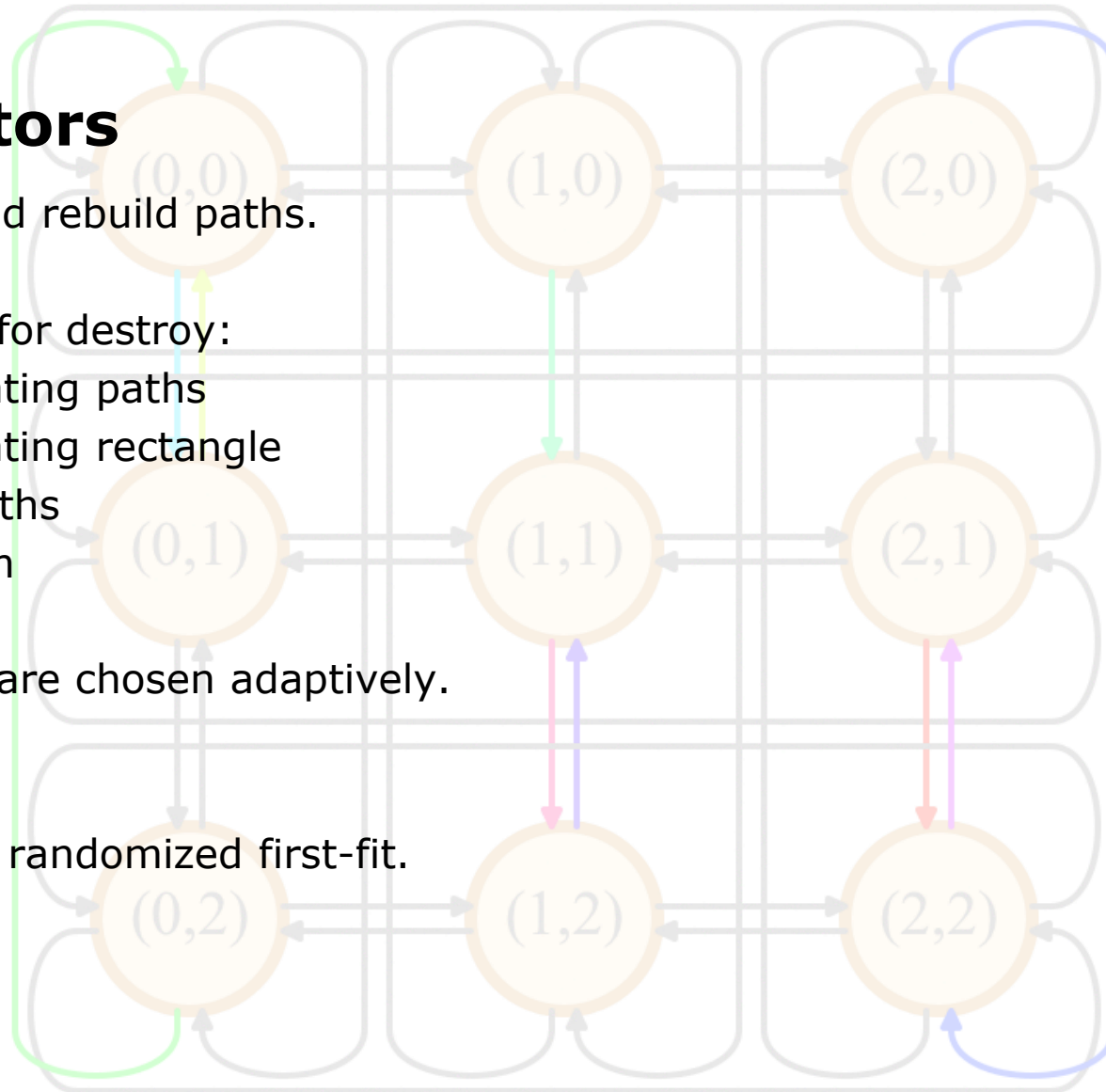
Operators for destroy:

- Dominating paths
- Dominating rectangle
- Late paths
- Random

Operators are chosen adaptively.

Rebuild:

- Greedy randomized first-fit.



Metaheuristics

Greedy randomized adaptive search procedure (GRASP)

```
procedure our_grasp( $\beta$ )
  best = infinite
  while (time left)
    current = initial_solution( $\beta$ )
    if (current shorter than best) then best = current
    {
      operator = choose_operator()
      chosen = operator()
      destroy(chosen)
      repair(chosen)
    }
    if (current shorter than best) then best = current
    punish_reward(operator)
  return best
```

- Local search of GRASP is choose_operator, destroy and repair.
- Random-operator not used.
- Problems with no clear local neighborhood.
- Very large solution spaces.

Metaheuristics

Adaptive Large Neighborhood Search (ALNS)

```
procedure our_alns()  
  best = current = initial_solution()  
  while (time left)  
    operator = choose_operator()  
    chosen = operator()  
    destroy(chosen)  
    repair(chosen)  
    if (current shorter than best) then best = current  
    punish_reward(operator)  
  
  return best
```

- Finds feasible solution easily.
- Destroy and repair gives very large neighborhood.
- Iteratively tries shortening the schedule.

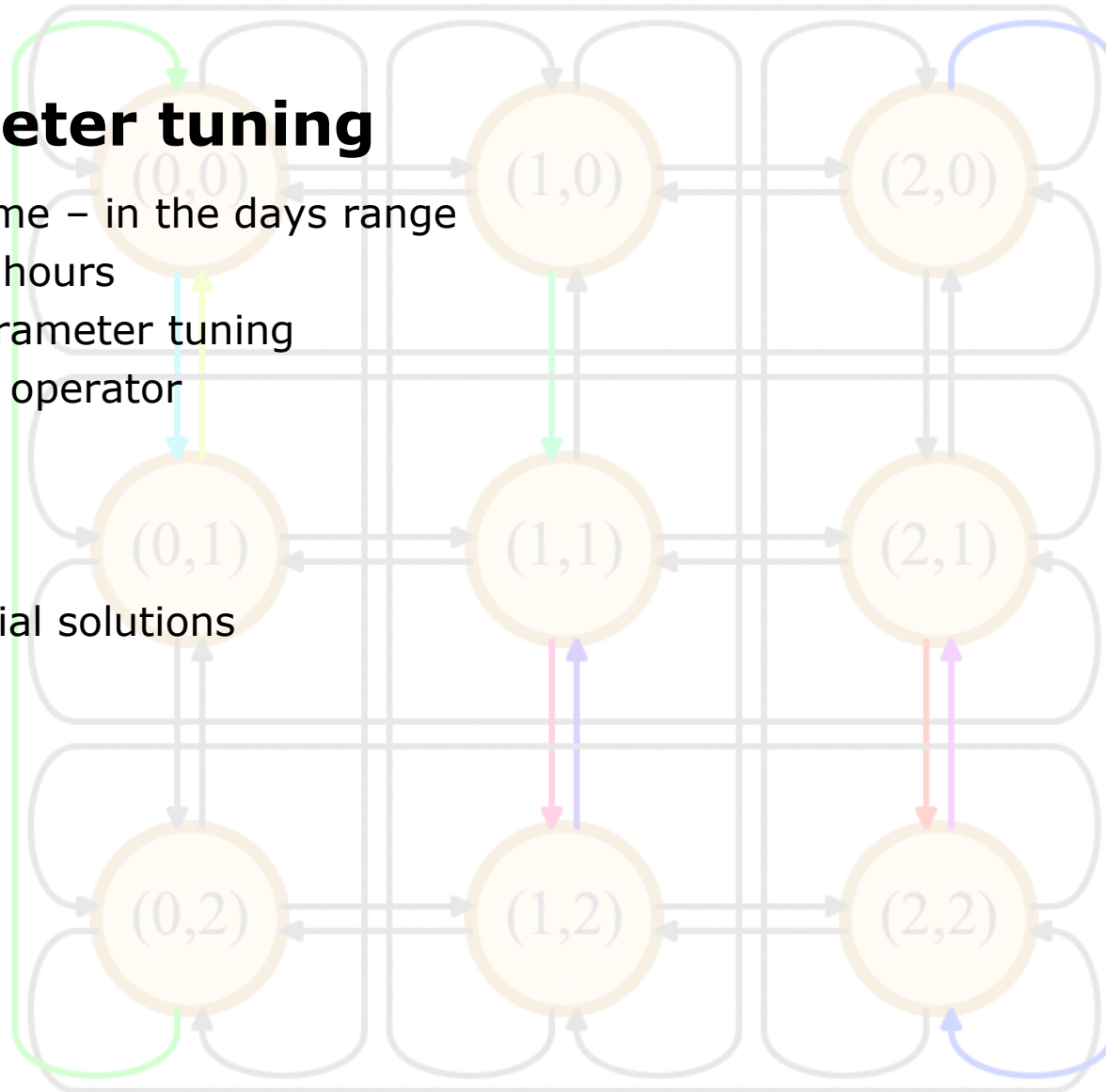
Parameter tuning

Running time – in the days range

Test run 2 hours

Limited parameter tuning

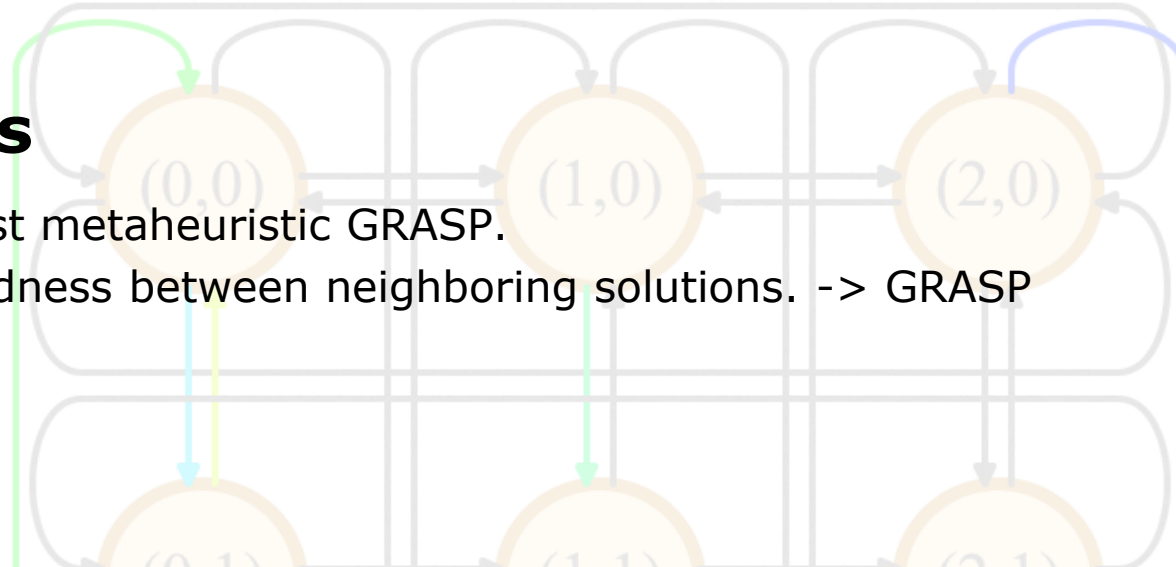
- Choose operator
 - GRASP
 - β
 - ALNS
 - Initial solutions



Results

Overall best metaheuristic GRASP.

Low relatedness between neighboring solutions. -> GRASP

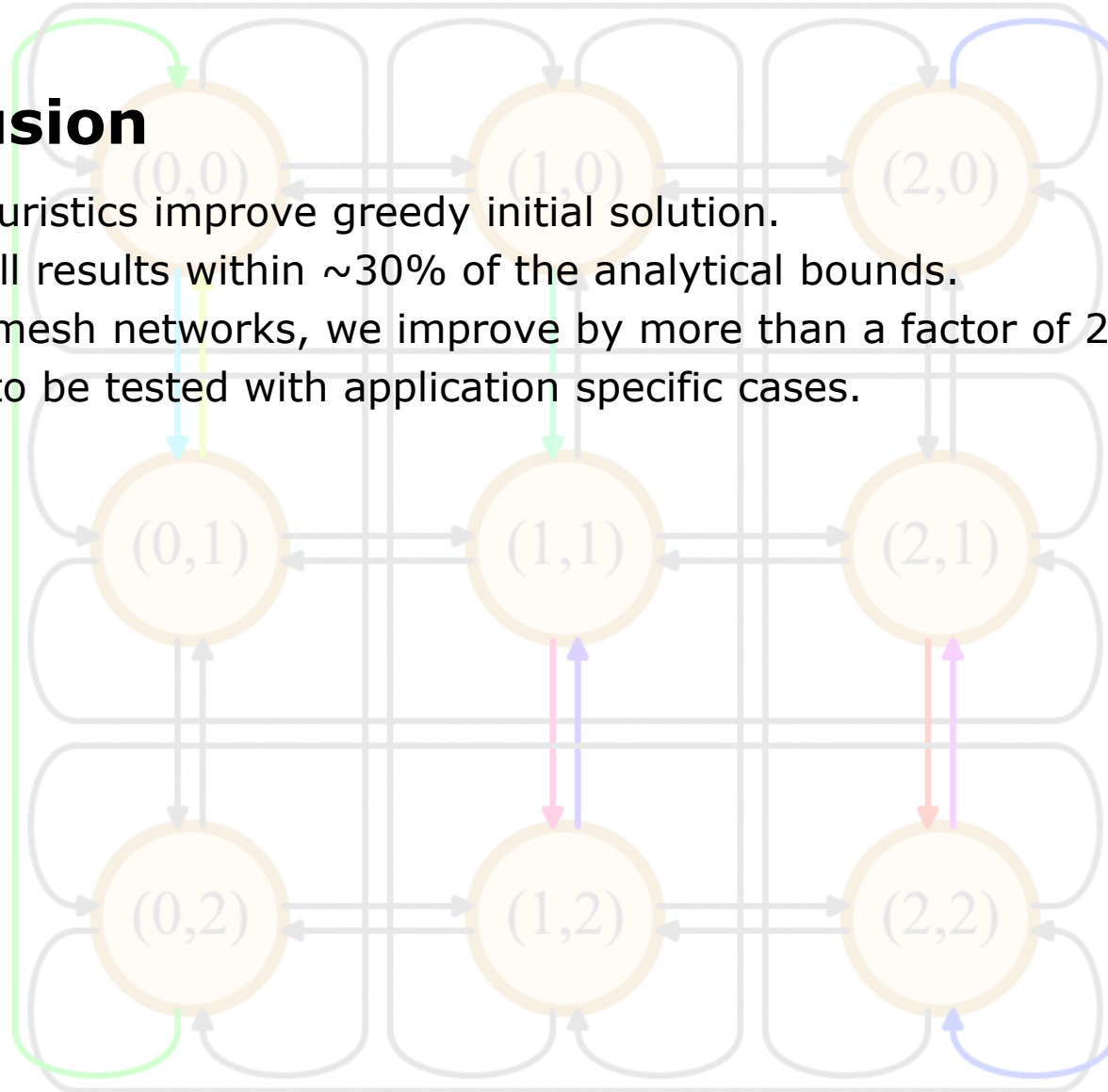


Size	Mesh					Bi-torus				
	Bounds[1]	[2]	GREEDY	ALNS	GRASP	Bounds[1]	[2]	GREEDY	ALNS	GRASP
3×3	8 (10)	28	13	11	11	8 (10)	11	12	10	10
4×4	16 (18)	59	24	21	21	15 (18)	20	21	19	19
5×5	25 (34)	112	41	39	37	24 (28)	28	32	30	30
6×6	54	–	66	65	61	35	–	45	45	43
7×7	66	–	98	97	94	48	–	64	63	61
8×8	128	481	144	144	138	64	88	87	86	85
9×9	135	–	201	201	195	90	–	113	113	113
10×10	250	974	271	271	267	125	158	154	153	151
15×15	600	3467	886	886	899	420	481	471	471	474

Table 4: Results compared to the heuristic results of [2]. Numbers in parenthesis are optimal schedule periods

Conclusion

- Metaheuristics improve greedy initial solution.
- All-to-all results within $\sim 30\%$ of the analytical bounds.
- For all mesh networks, we improve by more than a factor of 2,0.
- Needs to be tested with application specific cases.



Scheduler output

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