

Computational model of the peripheral nervous system: PNPy

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Introduction

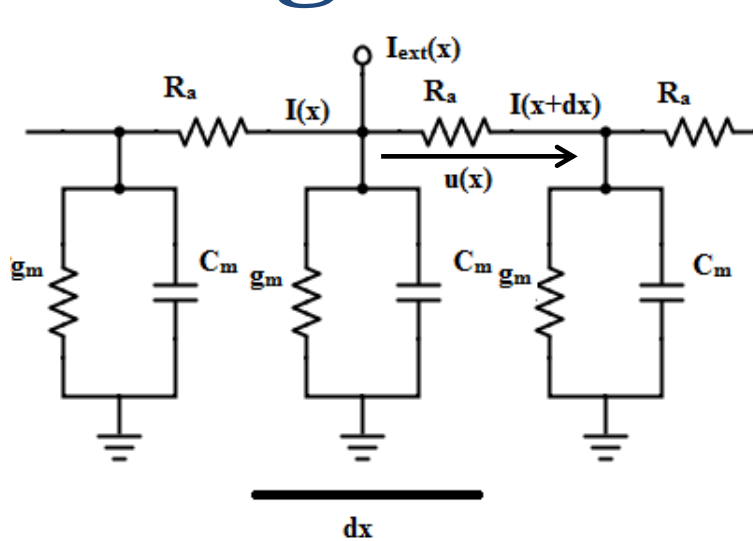
Motivation: Improve understanding of anatomy and neurophysiology of peripheral nerves

Hypothesis: Axons can be modelled by electrical circuits

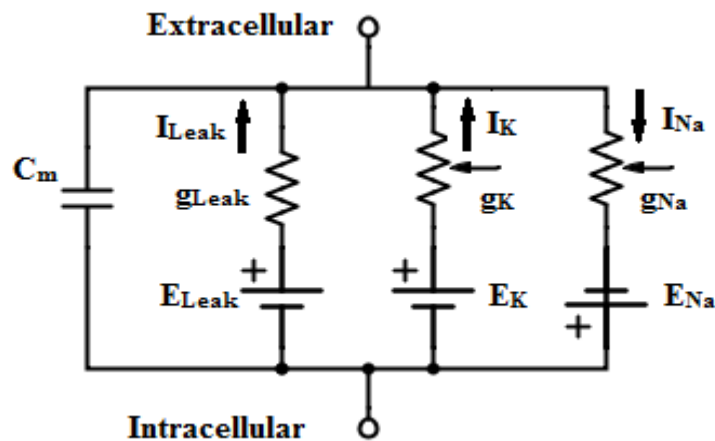
Objective: Produce as an output the type of signals measured by nerve cuff electrodes

Project applications: Vagus nerve stimulation (VNS), bioelectronics medicines

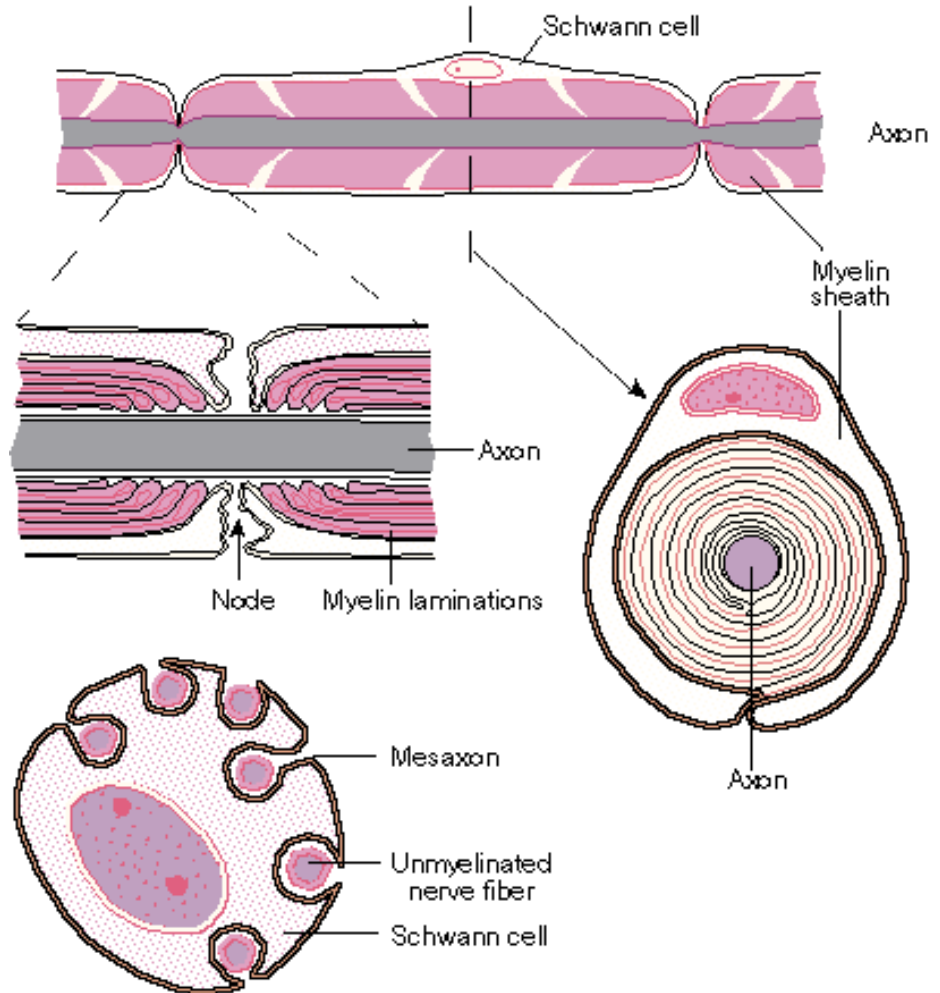
Background



Cable model schematic



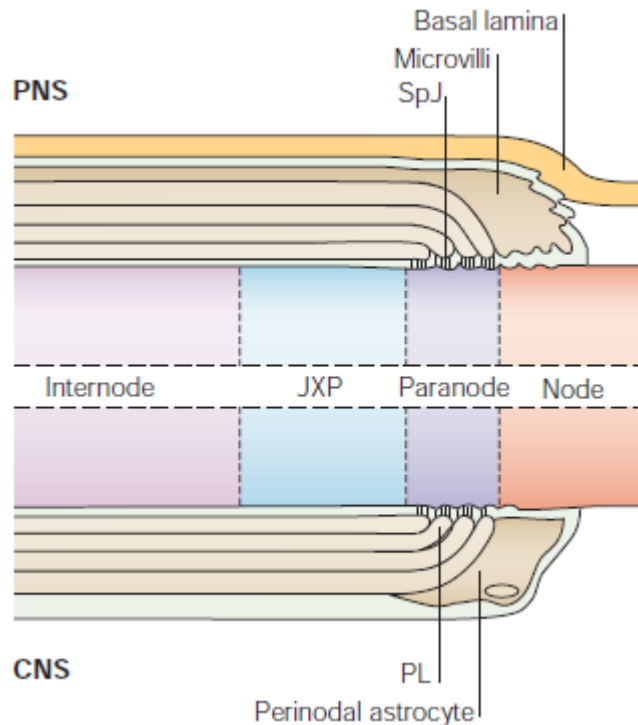
Hodgkin & Huxley model schematic



Credits: Queen Margaret University Edinburgh, Applied Sciences website

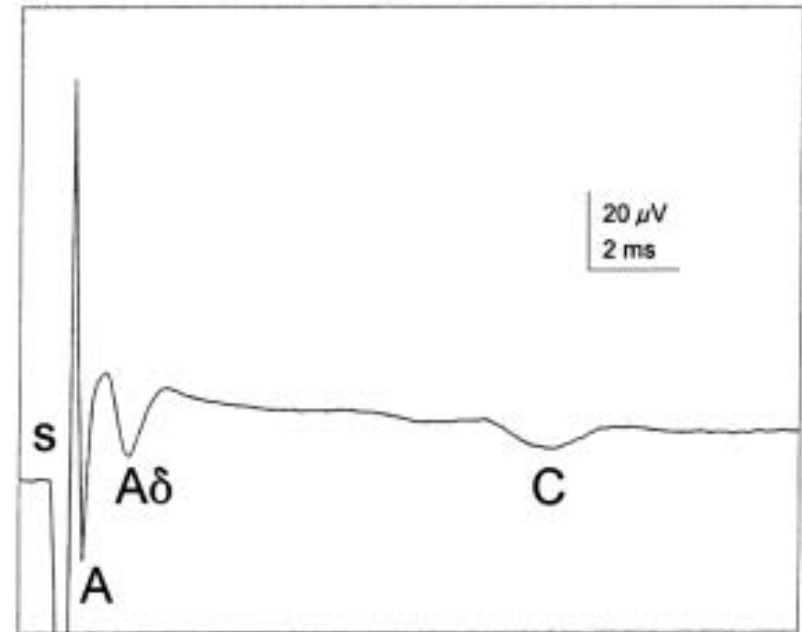
Representation of myelinated and unmyelinated nerve fibres

Background



Credits: S. Poliak and E. Peles, *Nature*, December 2013

Detailed myelinated axon structure around the nodes of Ranvier



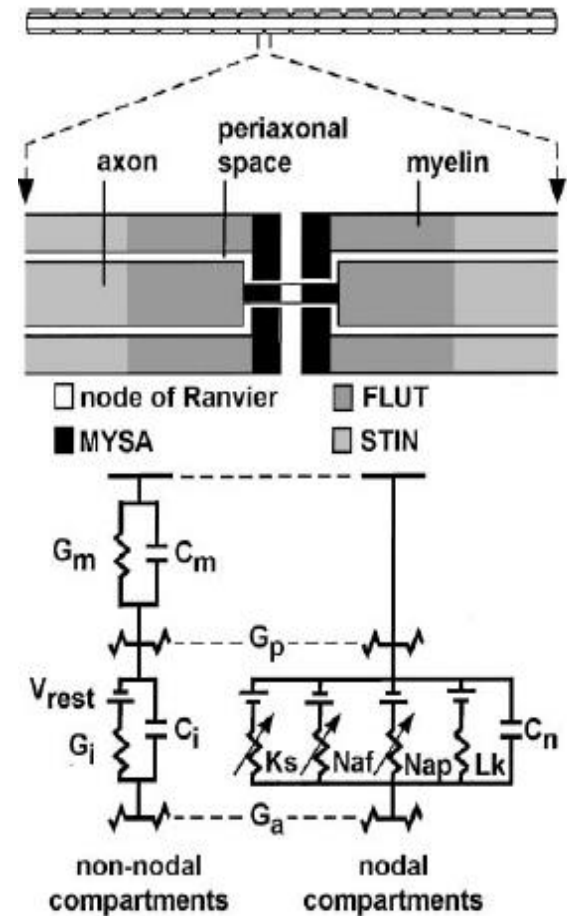
Credits: M. S. Evans et al, *Acta Neurol Scand*, 2004

Example of a compound action potential recorded from the cervical portion of left vagus nerve.

Methods

1. Axons parameters

<i>Unmyelinated axon</i>	<i>Myelinated axon</i>
Distribution of densities & diameters	Distribution of densities & diameters
Axon length (μm)	Number of nodes
Specific axial resistance ($\mu\text{F}/\text{cm}^2$)	



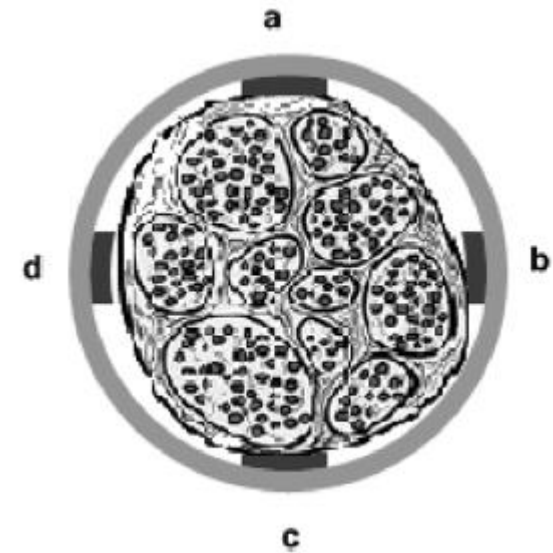
Credits: C. McIntyre et al, J Neurophysiol, 2002

Myelinated axon model used in PNPpy

Methods

2. Electrodes parameters

<i>Stimulating electrode</i>	<i>Recording electrode</i>
Stimulation type	Number contact points
Coordinates	Position along nerve
Frequency and duty cycle	Number of electrodes
Amplitude (nA)	Simulation duration (ms)
Jitter parameters	
Stimulus duration (ms)	



Credits: SC. Ordelman et al 2003

Schematic of a multi-contact electrode cuff around a nerve

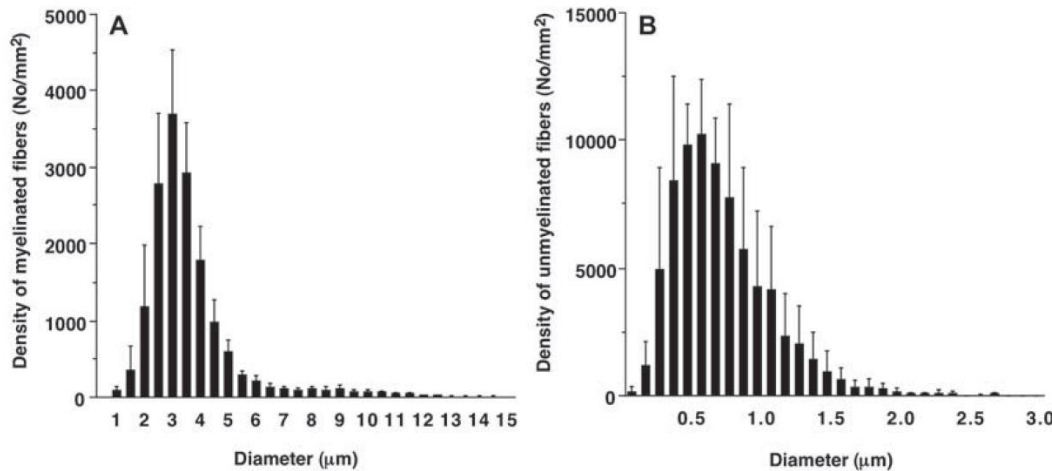
Point source model:

$$V(r, t) = \frac{1}{4\pi\sigma} \sum_{n=1}^N \frac{I_n(t)}{|r - r_n|}$$

Line source model:

$$V(r, t) = \frac{1}{4\pi\sigma} \sum_{n=1}^N I_n(t) \int \frac{dr_n}{|r - r_n|}$$

3. Diameter distributions and bundle parameters



Credits: T. Shimizu et al 2011

Histogram of myelinated and unmyelinated fibre densities of the human vagal visceral branch

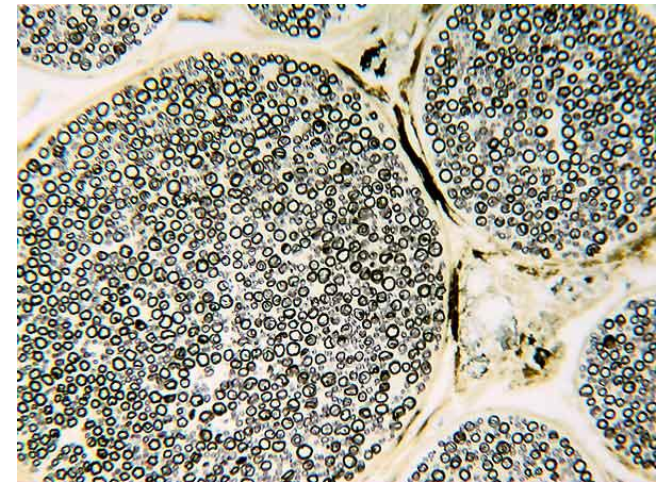
Bundle parameters

Bundle radius

Proportion myelinated axons

Proportion unmyelinated axons

Number of axons



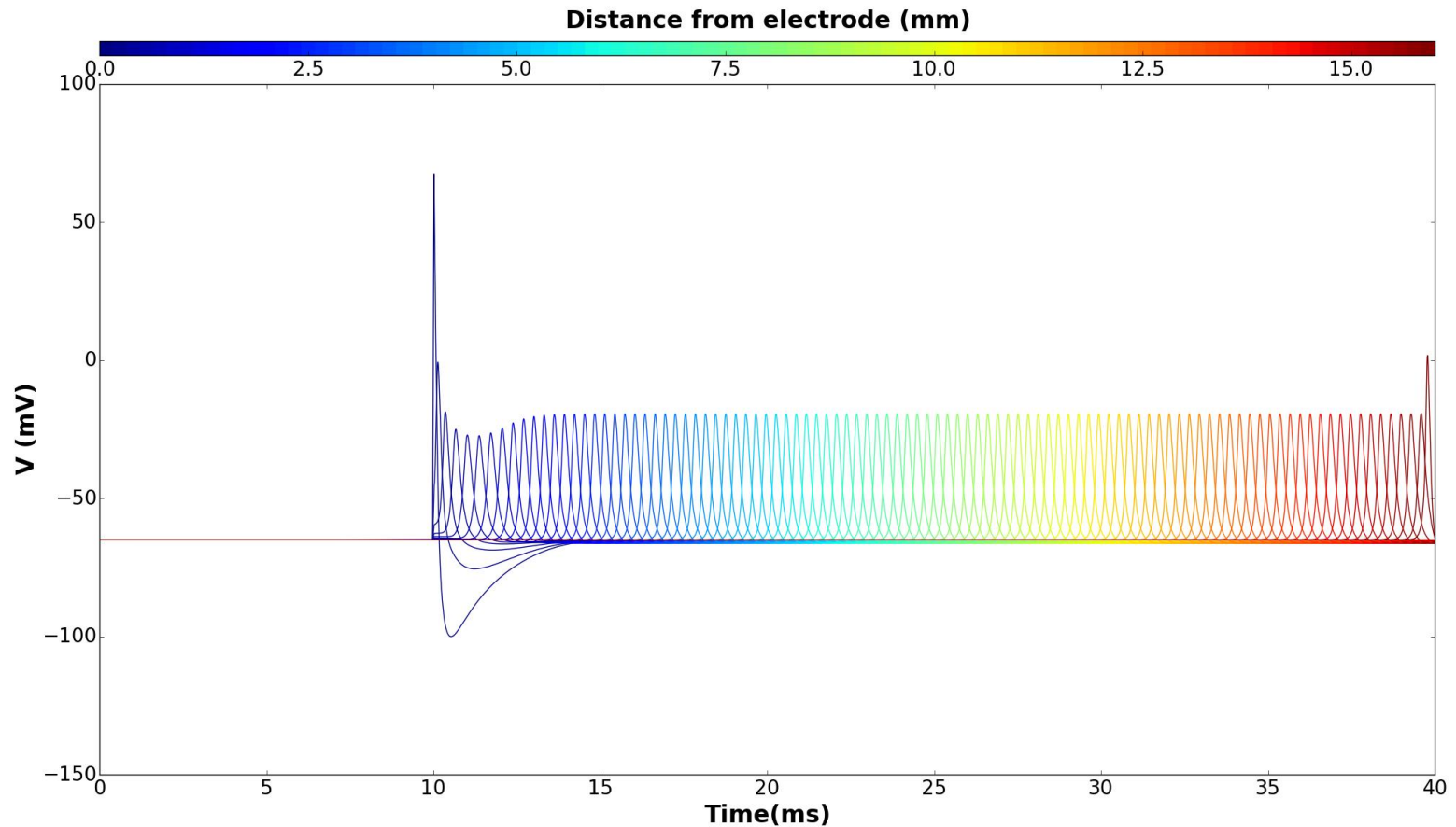
Credits: University of Minnesota, College of Veterinary Medicine website

Transverse section through a canine vagus nerve.

Results

AP propagation along an unmyelinated axon

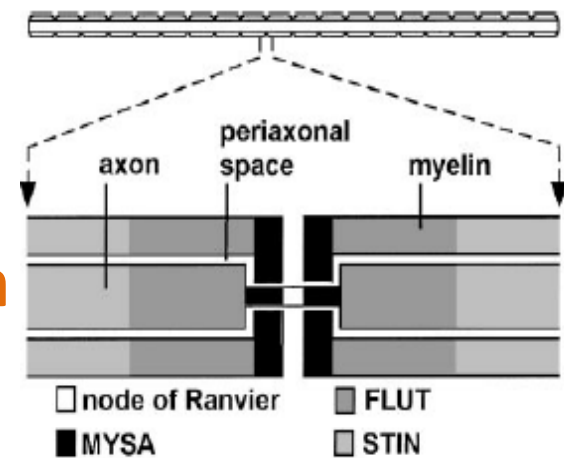
Axon diameter 1,8 cm - Conduction velocity $\approx 0,5$ m/s



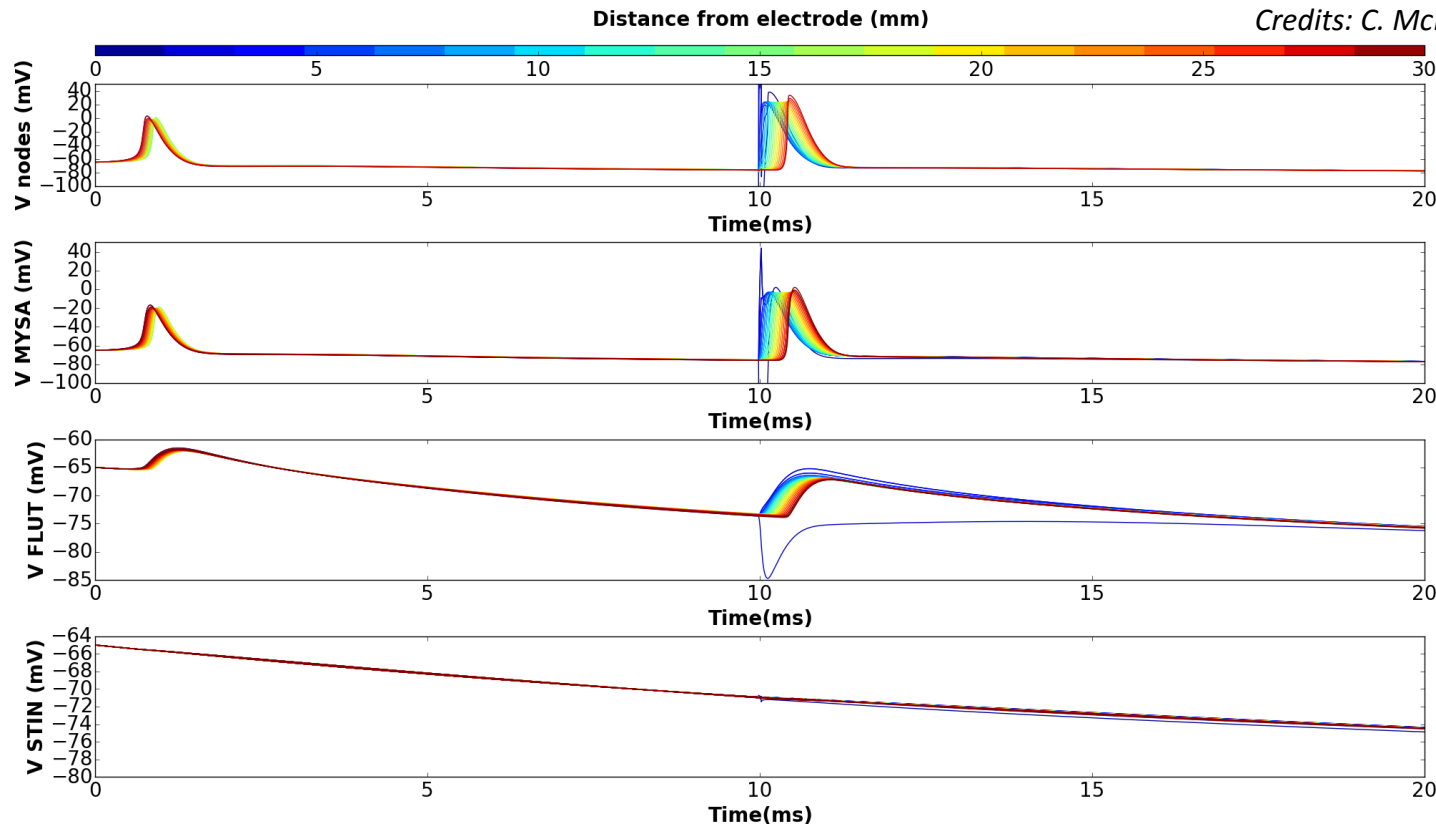
Results

AP propagation along a myelinated axon

Axon diameter = 4,6 μ m - Conduction velocity: ≈ 58 m/s



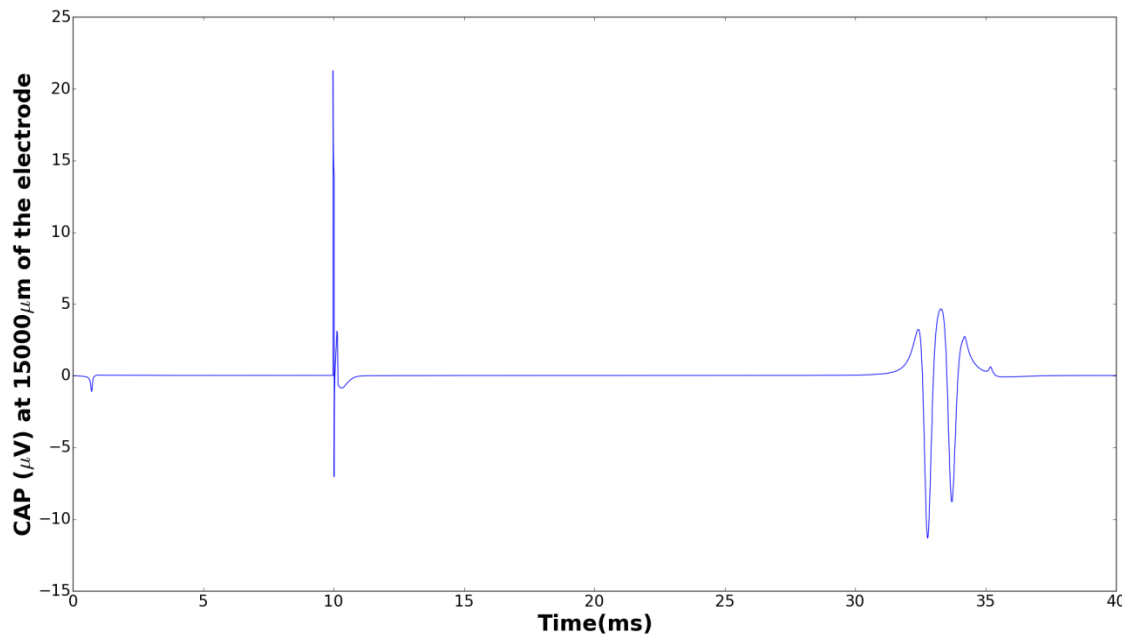
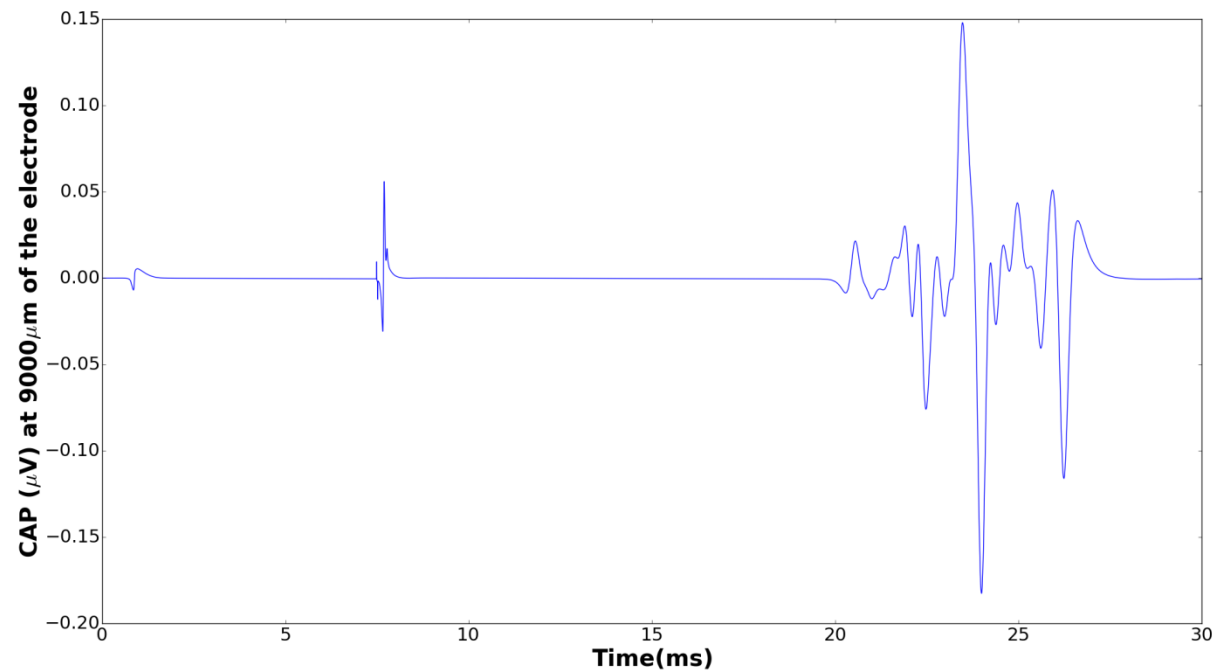
Credits: C. McIntyre et al, J Neurophysiol, 2002



Results

**CAP bipolar
recording 9mm
from stimulus**

**20% of
myelinated axons**

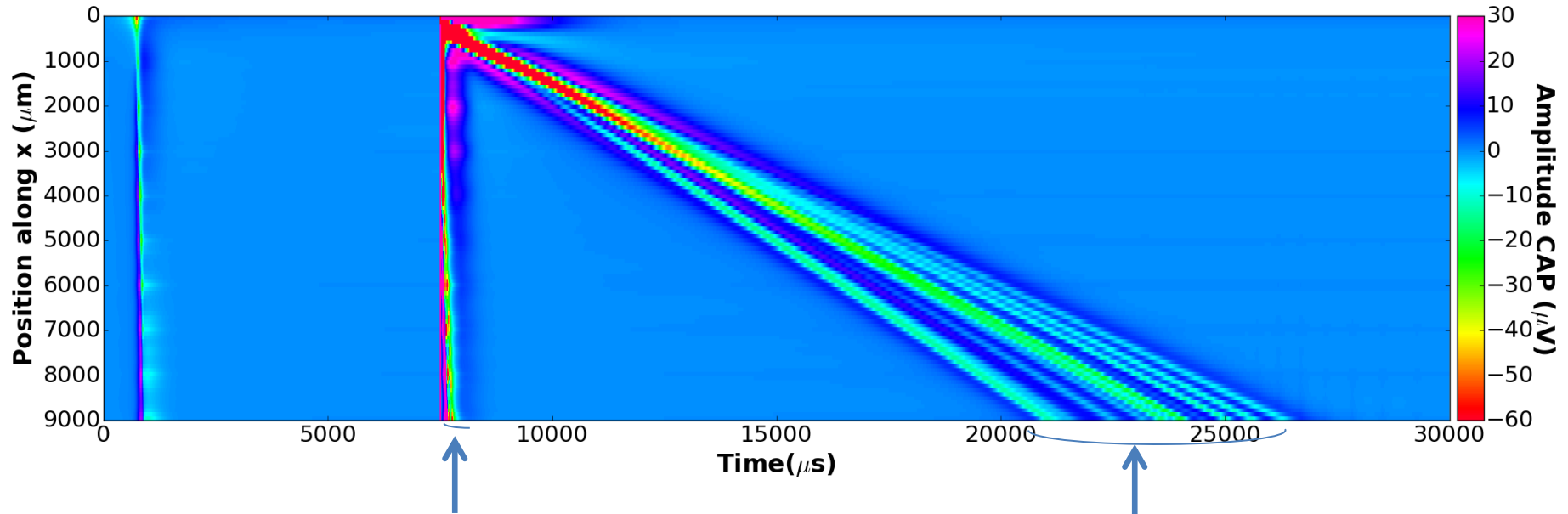


**CAP monopolar
recording 1,5cm
from stimulus**

**17,5% of
myelinated axons**

Results

CAP temporal/spatial propagation

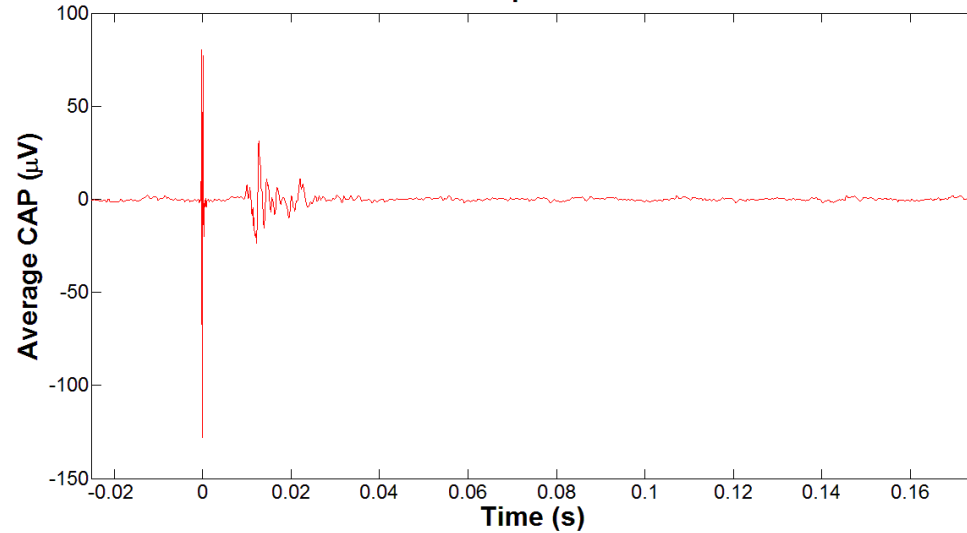


*Distribution myelinated axons
propagating at different
conduction velocities*

*Distribution unmyelinated axons
propagating at different
conduction velocities*

Discussion

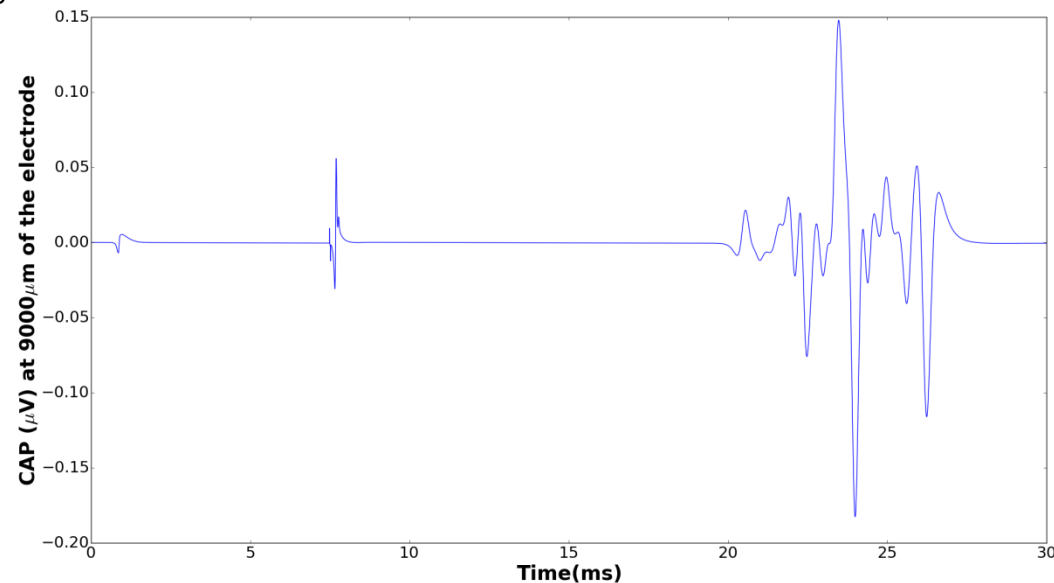
Denoised data from stimulus of pulse width 0.2ms and current 2mA



Credits: A. Eftekhari team, Department of EEE, Imperial College

Cervical vagus nerve recording with bipolar electrode 8cm from the stimulus

Objective: To be able to back derive the composition of the nerve in term of myelinated and unmyelinated fibres from the CAP measurement using PNPpy



References

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Annex

```
unmyelinatedDistribution = {
    'densities': [250, 1250, 5000, 8000, 9800, 10200, 8900, 7600, 5700, 4000, 3900, 23
00, 2000, 1300, 900, 750, 600, 600, 500, 250], # Fibers densities
    'diameters': [ 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1., 1.1,
1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 1.9, 2.], # Diameters for each densities
}

unmyelinatedParameters = {
    'name': "unmyelinated_axon", # Axon name (for NEURON)
    'L': 10500, # Axon length (µm)
    'diam': unmyelinatedDistribution, # Axon diameter distribution (µm)
    'cm' : 1.0, # Specific membrane capacitance (µF/cm²)
    'Ra': 200.0, # Specific axial resistance (Ohm cm)
    'rec_v': False, # Set voltage recorders True or False
}

myelinatedDistribution = {
    'densities': [100, 300, 1150, 2750, 3650, 2850, 1750, 900, 500, 250, 200, 150, 110, 10
0, 110, 100, 105], # Fibres densities
    'diameters': [ 1., 1.5, 2., 2.5, 3., 3.5, 4., 4.5, 5., 5.5, 6., 6.5,
7., 7.5, 8., 8.5, 9.], # Diameters for each densities
}

myelinatedParametersA = {
    'name': "myelinated_axonA", # Axon name (for NEURON)
    'Nnodes': 21, # Number of nodes
    'fiberD': myelinatedDistribution, # Fibre diameter distribution (µm)
    'rec_v': False, # Set voltage recorders True or False
}
```

Annex

```
stimulusParameters = {
    'stim_type': "EXTRA", #Stimulation type either "INTRA" or "EXTRA"
    'stim_coord': [[0,50,0]], # spatial coordinates of the stimulating
    electrodes, example for bipolar case=[[xe0,ye0,ze0], [xe1,ye1,ze1]]
    'amplitude': 2.0, # Pulse amplitude (nA)
    'freq': 0.1, # Frequency of the sin pulse (kHz)
    'duty_cycle': 0.001, # Percentage stimulus is ON for one period
    'stim_dur' : 1e1, # Stimulus duration (ms)
    'jitter_para': [0,0], # Mean and standard deviation of the delay
}

recordingParameters = {
    "number_contact_points": 8, #Number of points on the circle
    constituting the cuff electrode
    'recording_elec_pos': [9000], #Position of the recording electrode
    along axon in um, in "BIPOLAR" case should be given as a couple [x1,x2]
    'number_elects': 100, #number of electrodes along the bundle
    'dur': h.tstop, # Simulation duration (ms)
    'rec_CAP': True, # Boolean stating if CAP is recorded
}

bundleParameters = {
    'radius_bundle': 150.0, # Radius of the bundle in  $\mu\text{m}$ 
    'number_of_axons': 640, # Number of axons in the bundle
    'p_A': 0.2, # Percentage of myelinated fibre type A
    'p_B': 0, # Percentage of myelinated fibre type B
    'p_C': 0.8, # Percentage of unmyelinated fibre type C
    'myelinated_A': myelinatedParametersA, # Parameters for fibre type A
    'myelinated_B': myelinatedParametersB, # Parameters for fibre type B
    'unmyelinated': unmyelinatedParameters, # Parameters for fibre type C
}
```