```
In [1]: import pandas as pd
        import numpy as np
        import matplotlib.pyplot as plt
        import seaborn as sns
        from sklearn preprocessing import Standard Scaler, Robust Scaler, MinMax Scaler
        from sklearn.model selection import train test split
        from sklearn.feature_selection import SelectKBest, f_classif, mutual_info_cl
        import pickle
        import timeit
        import datetime as dt
        import warnings
        warnings.filterwarnings('ignore')
        # self-defined function
        from func import get FDR
        plt.style.use('seaborn-v0_8-deep')
In [2]: # Load the dataset
        df = pd.read_csv('./data/cleaned.csv', index_col=0)
        print(f"Dataset loaded: {df.shape}")
        df['date'] = pd.to datetime(df['date'])
        df.zip5 = df.zip5.astype(str).str.zfill(5)
        df.ssn = df.ssn.astype(str)
        df.dob = df.dob.astype(str)
        df.homephone = df.homephone.astype(str)
        print(f"\nDataset info:")
        df.info()
       Dataset loaded: (981694, 9)
      Dataset info:
       <class 'pandas.core.frame.DataFrame'>
       Index: 981694 entries, 0 to 981693
       Data columns (total 9 columns):
          Column Non-Null Count Dtype
       ___
          date 981694 non-null datetime64[ns]
       0
                       981694 non-null object
       1 ssn
           firstname 981694 non-null object
          lastname 981694 non-null object address 981694 non-null object
       3
       4
       5
          zip5
                       981694 non-null object
       6
           dob
                       981694 non-null object
       7
           homephone 981694 non-null object
            fraud label 981694 non-null int64
       dtypes: datetime64[ns](1), int64(1), object(7)
       memory usage: 74.9+ MB
```

Dimension Expand

```
In [3]: # Extract time features
    df['year'] = df['date'].dt.year
    df['month'] = df['date'].dt.month
    df['day'] = df['date'].dt.day
    #df['dow'] = df['date'].dt.dayofweek
    df['dow'] = df['date'].dt.day_name()
```

Risk table for day of week

by sigmoid-based smoothing

```
In [4]: train_test = df[df.date < '2016-11-01']</pre>
In [5]: # do statistical smoothing
        c = 4
        nmid = 20
        y avg = train test['fraud label'].mean()
        y_dow = train_test.groupby('dow')['fraud_label'].mean()
        num = train_test.groupby('dow').size()
        y_dow_smooth = y_avg + (y_dow - y_avg)/(1 + np.exp(-(num - nmid)/c))
        df['dow risk'] = df.dow.map(y dow smooth)
In [6]: df[['year', 'month', 'day', 'dow', 'dow_risk', 'fraud_label']].sample(5)
Out[6]:
                 year month day
                                        dow dow_risk fraud_label
        288476 2016
                           4
                               18
                                      Monday
                                                                0
                                              0.013641
         841106 2016
                          11
                                9 Wednesday 0.015339
                                                                0
         712851 2016
                           9
                               22
                                    Thursday
                                               0.015111
                                                                0
         119414 2016
                               14
                                      Sunday 0.013860
                                                                0
         127610 2016
                           2
                               17 Wednesday 0.015339
                                                                0
```

Create entitties

```
In [7]: df['name'] = df.firstname + df.lastname
    df['fulladdress'] = df.address + df.zip5
    df['name_dob'] = df.name + df.dob
    df['name_fulladdress'] = df.name + df.homephone
    df['fulladdress_dob'] = df.fulladdress + df.dob
    df['fulladdress_homephone'] = df.fulladdress + df.homephone
    df['dob_homephone'] = df.dob + df.homephone
    df['dob_homephone_name_dob'] = df.homephone + df.name_dob
In [8]: for field in df.select_dtypes(include=['object', 'category']).columns:
    df['ssn_' + field] = df.ssn + df[field]
```

Velocity + Day since

```
In [ ]: # previous:
        # start = timeit.default_timer()
        # for entity in attributes:
              try: print('Run time for the last entity ----- {}s'.format
              except: print('\n')
              st = timeit.default_timer()
              df l = df1[['record', 'date', entity]]
              df_r = df1[['check_record', 'check_date', entity]]
        #
              temp = pd.merge(df_l, df_r, left_on = entity, right_on = entity)
        #
              temp1 = temp[temp.record > temp.check_record][['record','date','check_
                                                          .groupby('record')[['date'
        #
              mapper = (temp1.date - temp1.check_date).dt.days
        #
              final[entity + ' day since'] = final.record.map(mapper)
        #
              final[entity + '_day_since'].fillna((final.date - pd.to_datetime('2016
              print('\n' + entity + ' day since ---> Done')
        #
              for time in [0,1,3,7,14,30]:
        #
                  temp_1 = temp[(temp.check_date >= (temp.date - dt.timedelta(time))
        #
                                 (temp.record >= temp.check_record)]
                  col name = entity + ' count ' + str(time)
                  mapper2 = temp_1.groupby('record')[entity].count()
                  final[col name] = final.record.map(mapper2)
                  print(entity + '_count_' + str(time) + ' ---> Done')
        # print('Total run time: {}mins'.format((timeit.default timer() - start)/60)
```

```
Run time for the last entity ----- 17.981693499954417s
       ssn day since ---> Done
       ssn_count_0 ---> Done
       ssn_count_1 ---> Done
       ssn_count_3 ---> Done
       ssn count 7 ---> Done
       ssn_count_14 ---> Done
       ssn count 30 ---> Done
       Run time for the last entity ----- 1.1341381249949336s
 In [9]: df1 = df.copy()
         df1['record'] = list(df1.index)
         final = df.copy()
         final['record'] = list(final.index)
         df1['check_date'] = df1.date
         df1['check record'] = df1.record
In [12]: import timeit
         import datetime as dt
         from typing import Dict, List
         import gc
```

on a million-record dataset, the previous code is not efficient, to optimize, can apply:

1. Optimize Data Types

Reduce memory footprint before processing

```
In [ ]: def optimize_dtypes(df: pd.DataFrame) -> pd.DataFrame:
             """Optimize DataFrame data types to reduce memory usage."""
             for col in df.columns:
                 col_type = df[col].dtype
                 if col_type != 'object':
                     c min = df[col].min()
                     c_{max} = df[col].max()
                     if str(col type)[:3] == 'int':
                         if c_min > np.iinfo(np.int8).min and c_max < np.iinfo(np.int</pre>
                              df[col] = df[col].astype(np.int8)
                         elif c_min > np.iinfo(np.int16).min and c_max < np.iinfo(np.</pre>
                              df[col] = df[col].astype(np.int16)
                         elif c_min > np.iinfo(np.int32).min and c_max < np.iinfo(np.</pre>
                              df[col] = df[col].astype(np.int32)
                         if c_min > np.finfo(np.float16).min and c_max < np.finfo(np.</pre>
                              df[col] = df[col].astype(np.float16)
                         elif c_min > np.finfo(np.float32).min and c_max < np.finfo(r</pre>
                              df[col] = df[col].astype(np.float32)
             return df
```

Instead of merging the entire dataset, process in smaller chunks/ pieces 3. Use Iterator-based Merge

For very large datasets, use chunksize parameter in merge operations 4. Garbage collection

Explicitly free memory after each step 5. Avoid duplicating data Process and immediately aggregate

```
In [ ]: def process_entity_chunked(df1: pd.DataFrame, entity: str, final: pd.DataFra
                                  chunk_size: int = 50000) -> pd.DataFrame:
            """Process entity with chunking to reduce memory usage."""
            print(f"\nProcessing {entity}...")
            st = timeit.default_timer()
            # Sort data once for efficiency
            df1_sorted = df1.sort_values('record')
            # Process day since in chunks
            day_since_results = {}
            for start_idx in range(0, len(df1_sorted), chunk_size):
                end_idx = min(start_idx + chunk_size, len(df1_sorted))
                chunk records = df1 sorted.iloc[start idx:end idx]['record'].unique(
                # Get relevant data for this chunk
                chunk data = df1[df1['record'].isin(chunk records) |
                                df1['check_record'].isin(chunk_records)]
                # Self-join on entity
                df_l = chunk_data[['record', 'date', entity]]
                df_r = chunk_data[['check_record', 'check_date', entity]]
                temp = pd.merge(df_l, df_r, on=entity, suffixes=('', '_r'))
                temp = temp[temp.record > temp.check_record]
                if len(temp) > 0:
                    # Calculate days since
                    temp1 = temp[['record', 'date', 'check_date']].groupby('record')
                    days_diff = (temp1['date'] - temp1['check_date']).dt.days
                    for record, days in days_diff.items():
                        day since results[record] = days
                # Clean up
                del temp, df_l, df_r
                gc.collect()
            # Map results
            final[entity + '_day_since'] = final['record'].map(day_since_results)
            final[entity + '_day_since'].fillna(
                (final['date'] - pd.to datetime('2016-01-01')).dt.days,
                inplace=True
            )
```

```
print(f'{entity}_day_since ---> Done')
            # Process counts for different time windows
            for time_window in [0, 1, 3, 7, 14, 30]:
                count results = {}
                for start_idx in range(0, len(df1_sorted), chunk_size):
                    end idx = min(start idx + chunk size, len(df1 sorted))
                    chunk_records = df1_sorted.iloc[start_idx:end_idx]['record'].uni
                    # Get relevant data
                    chunk_data = df1[df1['record'].isin(chunk_records) |
                                    df1['check_record'].isin(chunk_records)]
                    # Self-join
                    df_l = chunk_data[['record', 'date', entity]]
                    df_r = chunk_data[['check_record', 'check_date', entity]]
                    temp = pd.merge(df_l, df_r, on=entity, suffixes=('', '_r'))
                    # Filter by time window
                    temp_filtered = temp[
                        (temp['check_date'] >= (temp['date'] - pd.Timedelta(days=tim
                        (temp['record'] >= temp['check record'])
                    1
                    if len(temp filtered) > 0:
                        counts = temp_filtered.groupby('record')[entity].count()
                        for record, count in counts.items():
                            count results[record] = count
                    # Clean up
                    del temp, temp_filtered, df_l, df_r
                    gc.collect()
                # Map results
                col name = f'{entity} count {time window}'
                final[col_name] = final['record'].map(count_results).fillna(0).astyr
                print(f'{col name} ---> Done')
            print(f'Entity {entity} completed in {(timeit.default_timer() - st):.2f}
            return final
In [ ]: def process all entities(df1: pd.DataFrame, attributes: List[str],
                                final: pd.DataFrame, chunk_size: int = 50000) -> pd.
            """Process all entities with memory optimization."""
            start = timeit.default_timer()
            # Optimize data types first
            print("Optimizing data types...")
            df1 = optimize dtypes(df1)
            # Ensure date columns are datetime
```

```
df1['date'] = pd.to_datetime(df1['date'])
df1['check_date'] = pd.to_datetime(df1['check_date'])

# Process each entity
for entity in attributes:
    final = process_entity_chunked(df1, entity, final, chunk_size)

# Force garbage collection after each entity
    gc.collect()

print(f'\nTotal run time: {(timeit.default_timer() - start)/60:.2f} mins
return final
```

6. SQL-based Approach with DuckDB

For large self-joins, DuckDB is much more memory-efficient

```
In [ ]: def process_with_duckdb(df1: pd.DataFrame, attributes: List[str],
                               final: pd.DataFrame) -> pd.DataFrame:
            """Process using DuckDB for better memory efficiency."""
            import duckdb
            start = timeit.default timer()
            conn = duckdb.connect(':memory:')
            # Register DataFrame
            conn.register('df1', df1)
            conn.register('final', final)
            for entity in attributes:
                st = timeit.default timer()
                # Calculate day_since using SQL
                query day since = f"""
                WITH last records AS (
                    SELECT
                        l.record,
                        MAX(l.date - r.check_date) as days_diff
                    FROM df1 l
                    JOIN df1 r ON l.{entity} = r.{entity}
                    WHERE l.record > r.check record
                    GROUP BY l.record
                SELECT * FROM last records
                day since df = conn.execute(query day since).df()
                # Process each time window
                for time_window in [0, 1, 3, 7, 14, 30]:
                    query_count = f"""
                    SELECT
                        l.record,
```

```
COUNT(*) as count
                     FROM df1 l
                     JOIN df1 r ON l.{entity} = r.{entity}
                     WHERE l.record >= r.check record
                         AND r.check_date >= l.date - INTERVAL '{time_window} days'
                     GROUP BY l.record
                     count df = conn.execute(query count).df()
                     col_name = f'{entity}_count_{time_window}'
                     final = final.merge(count_df, on='record', how='left')
                     final.rename(columns={'count': col name}, inplace=True)
                     final[col name].fillna(0, inplace=True)
                 print(f'Entity {entity} completed in {(timeit.default timer() - st):
             conn.close()
             print(f'\nTotal run time: {(timeit.default_timer() - start)/60:.2f} mins
             return final
In [11]: # final = process_all_entities(df1, attributes, final, chunk_size=25000)
         # or for very large datasets:
         final = process_with_duckdb(df1, attributes, final)
        Entity ssn completed in 2.99s
        FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
        r color='black'))
        Entity firstname completed in 20.43s
        Entity lastname completed in 9.80s
        Entity address completed in 3.10s
        Entity zip5 completed in 5.73s
        FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
        r color='black'))
        Entity dob completed in 90.28s
        FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
        r_color='black'))
```

```
FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
r color='black'))
Entity homephone completed in 37.07s
FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
r color='black'))
FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
r_color='black'))
FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
r color='black'))
FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
r_color='black'))
FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
r color='black'))
FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
r color='black'))
FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
r_color='black'))
Entity dow completed in 816.35s
Entity name completed in 4.04s
Entity fulladdress completed in 3.89s
Entity name dob completed in 4.41s
Entity name fulladdress completed in 4.70s
Entity name_homephone completed in 4.99s
Entity fulladdress dob completed in 6.13s
Entity fulladdress homephone completed in 5.93s
FloatProgress(value=0.0, layout=Layout(width='auto'), style=ProgressStyle(ba
r color='black'))
```

```
Entity dob homephone completed in 16.99s
Entity homephone name dob completed in 6.64s
Entity ssn ssn completed in 8.29s
Entity ssn firstname completed in 7.64s
Entity ssn_lastname completed in 8.50s
Entity ssn address completed in 9.57s
Entity ssn zip5 completed in 10.26s
Entity ssn dob completed in 9.22s
Entity ssn homephone completed in 10.83s
Entity ssn dow completed in 11.14s
Entity ssn_name completed in 12.22s
Entity ssn fulladdress completed in 13.70s
Entity ssn name dob completed in 14.42s
Entity ssn name fulladdress completed in 15.43s
Entity ssn name homephone completed in 15.14s
Entity ssn fulladdress dob completed in 15.07s
Entity ssn_fulladdress_homephone completed in 15.22s
Entity ssn_dob_homephone completed in 15.73s
Entity ssn homephone name dob completed in 17.49s
```

Total run time: 20.89 mins

Relative Velocity

- calculate rate ratios or normalized counts for different time windows
- count_in_X_days / (count_in_Y_days / Y)
- which gives us: How many times higher is X's count compared to the average daily count over the last Y days
- is commonly used in Fraud detection where sudden spikes in activity (high ratio) happened

DOB and Age

Keep desired variables

```
In [22]: # only keep the numerical variables
    final_cut = final.copy()
    for field in final_cut.select_dtypes(include=['object', 'category']).columns
        final_cut.drop(field, inplace=True, axis=1)
In [28]: final_cut.drop(['date','record'], axis=1, inplace = True)
In [29]: final_cut.columns.to_list()
```

```
Out[29]:
          ['fraud_label',
           'year',
           'month',
           'day',
           'dow_risk',
           'ssn_count_0',
           'ssn_count_1',
           'ssn_count_3',
           'ssn_count_7',
           'ssn_count_14',
           'ssn_count_30',
           'firstname_count_0',
           'firstname_count_1',
           'firstname_count_3',
           'firstname_count_7',
           'firstname_count_14'
           'firstname_count_30',
           'lastname_count_0',
           'lastname count 1',
           'lastname_count_3',
           'lastname_count_7',
           'lastname_count_14',
           'lastname_count_30',
           'address_count_0',
           'address count 1',
           'address_count_3',
           'address_count_7',
           'address_count_14',
           'address_count_30',
           'zip5_count_0',
           'zip5_count_1',
           'zip5_count_3',
           'zip5_count_7',
           'zip5_count_14',
           'zip5_count_30',
           'dob_count_0',
           'dob_count_1',
           'dob_count_3',
           'dob_count_7',
           'dob_count_14',
           'dob_count_30',
           'homephone_count_0',
           'homephone_count_1',
           'homephone_count_3',
           'homephone_count_7',
           'homephone_count_14',
           'homephone_count_30',
           'dow_count_0',
           'dow_count_1',
           'dow_count_3',
           'dow_count_7',
           'dow_count_14',
           'dow_count_30',
           'name_count_0',
           'name_count_1',
           'name_count_3',
```

```
'name_count_7',
'name_count_14',
'name count 30',
'fulladdress_count_0',
'fulladdress_count_1',
'fulladdress count 3',
'fulladdress_count_7',
'fulladdress count 14',
'fulladdress count 30',
'name dob count 0',
'name_dob_count_1',
'name dob count 3',
'name dob count 7',
'name dob count 14',
'name dob count 30',
'name_fulladdress_count_0',
'name_fulladdress_count_1',
'name_fulladdress_count_3'
'name fulladdress count 7',
'name_fulladdress_count_14'
'name_fulladdress_count_30',
'name_homephone_count_0',
'name_homephone_count_1',
'name_homephone_count_3',
'name_homephone_count_7',
'name homephone count 14',
'name_homephone_count_30',
'fulladdress dob count 0',
'fulladdress_dob_count_1',
'fulladdress_dob_count_3',
'fulladdress_dob_count_7',
'fulladdress dob count 14'
'fulladdress_dob_count_30',
'fulladdress homephone count 0',
'fulladdress_homephone_count_1',
'fulladdress_homephone_count_3',
'fulladdress homephone count 7'
'fulladdress homephone count 14',
'fulladdress_homephone_count_30',
'dob_homephone_count_0',
'dob_homephone_count_1',
'dob_homephone_count_3',
'dob_homephone_count_7',
'dob homephone count 14',
'dob_homephone_count_30',
'homephone_name_dob_count_0',
'homephone_name_dob_count_1'
'homephone_name_dob_count_3',
'homephone_name_dob_count_7'
'homephone name dob count 14',
'homephone_name_dob_count_30',
'ssn_ssn_count_0',
'ssn ssn count 1',
'ssn_ssn_count_3',
'ssn_ssn_count_7',
'ssn ssn count 14',
```

```
'ssn_ssn_count_30',
'ssn_firstname_count_0',
'ssn firstname count 1'
'ssn_firstname_count_3',
'ssn_firstname_count_7',
'ssn_firstname_count_14',
'ssn_firstname_count_30',
'ssn lastname count 0',
'ssn lastname count 1',
'ssn_lastname_count_3',
'ssn_lastname_count_7'
'ssn lastname count 14',
'ssn lastname count 30',
'ssn address count 0',
'ssn address count 1',
'ssn address count 3',
'ssn_address_count_7',
'ssn_address_count_14',
'ssn address count 30',
'ssn_zip5_count_0',
'ssn_zip5_count_1',
'ssn zip5 count 3',
'ssn_zip5_count_7',
'ssn_zip5_count_14',
'ssn_zip5_count_30',
'ssn dob count 0',
'ssn_dob_count_1',
'ssn dob count 3',
'ssn_dob_count_7',
'ssn_dob_count_14',
'ssn dob count 30',
'ssn homephone count 0',
'ssn_homephone_count_1',
'ssn homephone count 3',
'ssn_homephone_count_7',
'ssn_homephone_count_14',
'ssn homephone count 30',
'ssn dow count 0',
'ssn_dow_count_1',
'ssn_dow_count_3',
'ssn dow count 7',
'ssn_dow_count_14',
'ssn_dow_count_30',
'ssn_name_count_0',
'ssn_name_count_1',
'ssn_name_count_3',
'ssn name count 7',
'ssn_name_count_14',
'ssn_name_count_30',
'ssn fulladdress count 0',
'ssn_fulladdress_count_1',
'ssn_fulladdress_count_3',
'ssn fulladdress count 7',
'ssn fulladdress count 14'
'ssn_fulladdress_count_30',
'ssn name dob count 0',
```

```
'ssn name dob count 1',
'ssn_name_dob_count_3',
'ssn name dob count 7'
'ssn_name_dob_count_14',
'ssn_name_dob_count_30',
'ssn name fulladdress count 0',
'ssn_name_fulladdress_count_1',
'ssn name fulladdress count 3',
'ssn name fulladdress count 7',
'ssn_name_fulladdress_count_14',
'ssn_name_fulladdress_count_30',
'ssn name homephone count 0',
'ssn name homephone count 1',
'ssn name homephone count 3',
'ssn name homephone count 7'
'ssn name homephone count 14',
'ssn_name_homephone_count_30',
'ssn_fulladdress_dob_count_0'
'ssn fulladdress dob count 1',
'ssn_fulladdress_dob_count_3',
'ssn_fulladdress_dob_count_7'
'ssn fulladdress dob count 14',
'ssn_fulladdress_dob_count_30',
'ssn_fulladdress_homephone_count_0',
'ssn fulladdress homephone count 1',
'ssn fulladdress homephone count 3',
'ssn_fulladdress_homephone_count_7',
'ssn fulladdress homephone count 14'
'ssn_fulladdress_homephone_count_30',
'ssn_dob_homephone_count_0',
'ssn dob homephone count 1',
'ssn dob homephone count 3',
'ssn_dob_homephone_count_7',
'ssn dob homephone count 14',
'ssn_dob_homephone_count_30',
'ssn_homephone_name_dob_count_0',
'ssn homephone name dob count 1',
'ssn homephone name dob count 3',
'ssn_homephone_name_dob_count_7',
'ssn_homephone_name_dob_count_14'
'ssn homephone name dob count 30',
'ssn_count_0_by_3',
'ssn_count_0_by_7',
'ssn count 0 by 14',
'ssn_count_0_by_30',
'ssn_count_1_by_3',
'ssn count 1 by 7',
'ssn_count_1_by_14',
'ssn_count_1_by_30',
'firstname count 0 by 3',
'firstname_count_0_by_7'
'firstname_count_0_by_14'
'firstname count 0 by 30',
'firstname_count_1_by_3',
'firstname_count_1_by_7'
'firstname count 1 by 14',
```

```
'firstname_count_1_by_30',
'lastname_count_0_by_3',
'lastname count 0 by 7'
'lastname count 0 by 14',
'lastname_count_0_by_30',
'lastname_count_1_by_3',
'lastname_count_1_by_7',
'lastname_count_1_by_14',
'lastname count 1 by 30',
'address_count_0_by_3',
'address_count_0_by_7'
'address count 0 by 14',
'address_count_0_by_30',
'address_count_1_by_3',
'address count 1 by 7',
'address_count_1_by_14'
'address_count_1_by_30',
'zip5_count_0_by_3',
'zip5 count 0 by 7',
'zip5_count_0_by_14',
'zip5_count_0_by_30',
'zip5 count 1 by 3',
'zip5_count_1_by_7'
'zip5_count_1_by_14',
'zip5_count_1_by_30',
'dob count 0 by 3',
'dob_count_0_by_7',
'dob count 0 by 14'
'dob_count_0_by_30',
'dob_count_1_by_3',
'dob count 1 by 7',
'dob count 1 by 14',
'dob_count_1_by_30',
'homephone count 0 by 3',
'homephone_count_0_by_7',
'homephone_count_0_by_14',
'homephone count 0 by 30',
'homephone count 1 by 3',
'homephone_count_1_by_7',
'homephone_count_1_by_14',
'homephone_count_1_by_30',
'dow_count_0_by_3',
'dow_count_0_by_7',
'dow count 0 by 14',
'dow_count_0_by_30',
'dow_count_1_by_3',
'dow count 1 by 7',
'dow_count_1_by_14',
'dow_count_1_by_30',
'name count 0 by 3',
'name_count_0_by_7',
'name_count_0_by_14'
'name count 0 by 30',
'name_count_1_by_3',
'name_count_1_by_7',
'name count 1 by 14',
```

```
'name_count_1_by_30',
'fulladdress_count_0_by_3',
'fulladdress count 0 by 7',
'fulladdress_count_0_by_14',
'fulladdress_count_0_by_30',
'fulladdress_count_1_by_3',
'fulladdress_count_1_by_7',
'fulladdress_count_1_by_14'
'fulladdress count 1 by 30',
'name_dob_count_0_by_3',
'name_dob_count_0_by_7'
'name dob count 0 by 14',
'name_dob_count_0_by_30',
'name dob count 1 by 3',
'name dob count 1 by 7'
'name dob count 1 by 14',
'name_dob_count_1_by_30',
'name_fulladdress_count_0_by_3',
'name fulladdress count 0 by 7',
'name_fulladdress_count_0_by_14',
'name_fulladdress_count_0_by_30',
'name fulladdress count 1 by 3',
'name_fulladdress_count_1_by_7'
'name_fulladdress_count_1_by_14',
'name fulladdress count 1 by 30',
'name homephone count 0 by 3',
'name_homephone_count_0_by_7'
'name homephone count 0 by 14'
'name_homephone_count_0_by_30',
'name_homephone_count_1_by_3',
'name homephone count 1 by 7',
'name homephone count 1 by 14'
'name_homephone_count_1_by_30',
'fulladdress dob count 0 by 3',
'fulladdress_dob_count_0_by_7'
'fulladdress_dob_count_0_by_14',
'fulladdress dob count 0 by 30',
'fulladdress dob count 1 by 3',
'fulladdress_dob_count_1_by_7'
'fulladdress_dob_count_1_by_14',
'fulladdress_dob_count_1_by_30',
'fulladdress_homephone_count_0_by_3',
'fulladdress_homephone_count_0_by_7',
'fulladdress homephone count 0 by 14'
'fulladdress_homephone_count_0_by_30',
'fulladdress_homephone_count_1_by_3',
'fulladdress_homephone_count_1_by_7'
'fulladdress_homephone_count_1_by_14',
'fulladdress_homephone_count_1_by_30',
'dob homephone count 0 by 3',
'dob_homephone_count_0_by_7'
'dob_homephone_count_0_by_14'
'dob homephone count 0 by 30',
'dob_homephone_count_1_by_3',
'dob_homephone_count_1_by_7'
'dob homephone count 1 by 14',
```

```
'dob_homephone_count_1_by_30',
'homephone_name_dob_count_0_by_3',
'homephone name dob count 0 by 7',
'homephone_name_dob_count_0_by_14',
'homephone_name_dob_count_0_by_30',
'homephone_name_dob_count_1_by_3',
'homephone name dob count 1 by 7',
'homephone_name_dob_count_1_by_14'
'homephone name dob count 1 by 30',
'ssn_ssn_count_0_by_3',
'ssn_ssn_count_0_by_7'
'ssn ssn count 0 by 14',
'ssn ssn count 0 by 30',
'ssn ssn count 1 by 3',
'ssn ssn count 1 by 7'
'ssn ssn count 1 by 14',
'ssn_ssn_count_1_by_30',
'ssn_firstname_count_0_by_3',
'ssn firstname count 0 by 7',
'ssn firstname count 0 by 14',
'ssn_firstname_count_0_by_30',
'ssn firstname count 1 by 3',
'ssn_firstname_count_1_by_7'
'ssn_firstname_count_1_by_14',
'ssn firstname count 1 by 30',
'ssn lastname count 0 by 3',
'ssn_lastname_count_0_by_7'
'ssn lastname count 0 by 14'
'ssn_lastname_count_0_by_30',
'ssn_lastname_count_1_by_3',
'ssn lastname count 1 by 7',
'ssn lastname count 1 by 14',
'ssn_lastname_count_1_by_30',
'ssn address count 0 by 3',
'ssn_address_count_0_by_7'
'ssn_address_count_0_by_14',
'ssn address count 0 by 30',
'ssn address count 1 by 3',
'ssn_address_count_1_by_7',
'ssn_address_count_1_by_14'
'ssn address count 1 by 30',
'ssn_zip5_count_0_by_3',
'ssn_zip5_count_0_by_7',
'ssn zip5 count 0 by 14',
'ssn_zip5_count_0_by_30',
'ssn_zip5_count_1_by_3',
'ssn zip5 count 1 by 7',
'ssn zip5 count 1 by 14',
'ssn_zip5_count_1_by_30',
'ssn dob count 0 by 3',
'ssn dob count 0 by 7'
'ssn_dob_count_0_by_14'
'ssn dob count 0 by 30',
'ssn_dob_count_1_by_3',
'ssn_dob_count_1_by_7',
'ssn dob count 1 by 14',
```

```
'ssn_dob_count_1_by_30',
'ssn homephone count 0 by 3',
'ssn homephone count 0 by 7',
'ssn homephone count 0 by 14',
'ssn_homephone_count_0_by_30',
'ssn homephone count 1 by 3',
'ssn homephone count 1 by 7'
'ssn homephone count 1 by 14'
'ssn homephone count 1 by 30',
'ssn_dow_count_0_by_3',
'ssn_dow_count_0_by_7'
'ssn dow count 0 by 14',
'ssn dow count 0 by 30',
'ssn dow count 1 by 3',
'ssn dow count 1 by 7'
'ssn dow count 1 by 14'
'ssn_dow_count_1_by_30',
'ssn_name_count_0_by_3'
'ssn name count 0 by 7',
'ssn name count 0 by 14',
'ssn_name_count_0_by_30',
'ssn name count 1 by 3',
'ssn_name_count_1_by_7',
'ssn name count 1 by 14',
'ssn name count 1 by 30',
'ssn fulladdress count 0 by 3',
'ssn fulladdress count 0 by 7'
'ssn fulladdress count 0 by 14'
'ssn_fulladdress_count_0_by_30',
'ssn_fulladdress_count_1_by_3',
'ssn fulladdress count 1 by 7'
'ssn fulladdress count 1 by 14'
'ssn_fulladdress_count_1_by_30',
'ssn_name_dob_count_0_by_3',
'ssn name dob count 0 by 7'
'ssn_name_dob_count_0_by_14',
'ssn name dob count 0 by 30',
'ssn name dob count 1 by 3',
'ssn_name_dob_count_1_by_7'
'ssn_name_dob_count_1_by_14',
'ssn name dob count 1 by 30',
'ssn name fulladdress count 0 by 3',
'ssn_name_fulladdress_count_0_by_7',
'ssn name fulladdress count 0 by 14'
'ssn_name_fulladdress_count_0_by_30',
'ssn_name_fulladdress_count_1_by_3',
'ssn name fulladdress count 1 by 7'
'ssn name fulladdress count 1 by 14',
'ssn_name_fulladdress_count_1_by_30',
'ssn name homephone count 0 by 3',
'ssn name homephone count 0 by 7'
'ssn_name_homephone_count_0_by_14'
'ssn name homephone count 0 by 30',
'ssn_name_homephone_count_1_by_3',
'ssn name homephone count 1 by 7',
'ssn name homephone count 1 by 14',
```

```
'ssn name homephone count 1 by 30',
           'ssn_fulladdress_dob_count_0_by_3',
           'ssn fulladdress dob count 0 by 7',
           'ssn fulladdress dob count 0 by 14',
           'ssn_fulladdress_dob_count_0_by_30',
           'ssn fulladdress dob count 1 by 3',
           'ssn fulladdress dob count 1 by 7',
           'ssn fulladdress dob count 1 by 14'
           'ssn fulladdress dob count 1 by 30',
           'ssn fulladdress homephone count 0 by 3',
           'ssn_fulladdress_homephone_count_0_by_7',
           'ssn fulladdress homephone count 0 by 14',
           'ssn fulladdress homephone count 0 by 30',
           'ssn fulladdress homephone count 1 by 3',
           'ssn fulladdress homephone count 1 by 7'
           'ssn fulladdress homephone count 1 by 14'
           'ssn_fulladdress_homephone_count_1_by_30',
           'ssn_dob_homephone_count_0_by_3',
           'ssn dob homephone count 0 by 7',
           'ssn dob homephone count 0 by 14',
           'ssn_dob_homephone_count_0_by_30',
           'ssn dob homephone count 1 by 3',
           'ssn_dob_homephone_count_1_by_7',
           'ssn_dob_homephone_count_1_by_14',
           'ssn dob homephone count 1 by 30',
           'ssn homephone name dob count 0 by 3',
           'ssn_homephone_name_dob_count_0_by_7',
           'ssn homephone name dob count 0 by 14'
           'ssn_homephone_name_dob_count_0_by_30',
           'ssn_homephone_name_dob_count_1_by_3',
           'ssn homephone name dob count 1 by 7',
           'ssn homephone name dob count 1 by 14'
           'ssn_homephone_name_dob_count_1_by_30',
           'birth year',
           'birth month',
           'birth_day',
           'age']
In [30]:
         final_cut.shape
Out[30]: (981694, 485)
         final_cut.sample(5)
In [32]:
```

Out[32]:		fraud_label	year	month	day	dow_risk	ssn_count_0	ssn_count_1	ssn_co
	663247	0	2016	9	4	0.013860	1	1	
	663901	0	2016	9	4	0.013860	1	1	
	433918	0	2016	6	10	0.014702	1	1	
	386577	0	2016	5	24	0.014220	1	1	
	863720	0	2016	11	18	0.014702	1	1	

5 rows × 485 columns

```
In [33]: final_cut.to_csv('./data/vars 485.csv')
```

Feature Selection

```
In [2]: final_cut = pd.read_csv('./data/vars 485.csv', index_col=0)
    data = final_cut.loc[(final_cut.index <= 790000)&(final_cut.index >= 35755)]
    data['RANDOM'] = np.random.ranf(len(data))
    del final_cut
```

Filter

```
In [3]: from scipy.stats import ks_2samp
from sklearn.feature_selection import SelectKBest
```

The **ks_2samp()** function computes the Kolmogorov–Smirnov (KS) statistic, which measures the maximum distance between the cumulative distribution functions (CDFs) of two groups (fraud vs. non-fraud) for a given feature

KS value ranges from 0 to 1.

Higher KS means better separation → the feature is more discriminatory

 To measure how well a feature distinguishes between frauds (fraud_label = 1) and non-frauds (fraud_label = 0)

```
filter_df.columns = ['feature', 'KS']
filter_df.sort_values(by=['KS'], ascending = False, inplace = True)
filter_df.head(10)
```

```
Out[4]:
                          feature
                                      KS
         27
                  address_count_30 0.329452
                fulladdress_count_30 0.328546
        63
        26
                   fulladdress_count_14 0.318109
        62
        25
                   address_count_7 0.297637
         61
                 fulladdress_count_7 0.297425
       235
              address_count_0_by_30 0.287879
       283 fulladdress_count_0_by_30 0.287071
       234
              282 fulladdress_count_0_by_14 0.276820
```

```
In [5]: del goods, bads
```

Fraud Detection Rate (FDR): Take the top 3% and bottom 3% values of each feature. Compute the fraud rate (i.e., proportion of frauds) in both subsets. then keep the maximum FDR between the two tails.

- Higher FDR means fraud cases are concentrated in the extreme values of the feature. Indicates the feature is useful for detecting fraud in high- or low-end values.
- Measures how concentrated the frauds are at the extremes of each feature.

```
Out[8]: ['fulladdress count 30',
          'address_count_14',
          'fulladdress_count_14',
          'address_count_7',
          'fulladdress_count_7',
          'address_count_0_by_14',
          'fulladdress_count_0_by_14',
          'address_count_3',
          'fulladdress_count_3',
          'fulladdress_count_0_by_30',
          'address_count_0_by_30',
          'address_count_0_by_7',
          'fulladdress_count_0_by_7',
          'address_count_1',
          'fulladdress_count_1',
          'ssn_dob_count_30',
          'ssn_count_30',
          'ssn_ssn_count_30',
          'ssn firstname count 30',
          'ssn_lastname_count_30',
          'fulladdress_homephone_count_30',
          'ssn_name_dob_count_30',
          'name_dob_count_30',
          'ssn_name_count_30',
          'fulladdress count 0 by 3',
          'address_count_0_by_3',
          'fulladdress_homephone_count_14',
          'ssn_ssn_count_14',
          'ssn_count_14',
          'ssn_dob_count_14',
          'ssn_firstname_count_14',
          'zip5_count_1',
          'name_count_30',
          'ssn_lastname_count_14',
          'zip5_count_3',
          'name_dob_count_14',
          'ssn_name_count_14',
          'ssn_name_dob_count_14',
          'ssn_dob_count_0_by_30',
          'ssn_name_dob_count_0_by_30',
          'address_count_1_by_14',
          'fulladdress_count_1_by_14',
          'fulladdress_homephone_count_7',
          'ssn_count_0_by_14',
          'ssn_ssn_count_0_by_14',
          'fulladdress_homephone_count_0_by_30',
          'ssn_dob_count_0_by_14',
          'ssn ssn count 0 by 30',
          'name_count_14',
          'ssn_count_0_by_30',
          'ssn_firstname_count_0_by_30',
          'ssn_firstname_count_0_by_14',
          'ssn_count_7',
          'ssn ssn count 7',
          'ssn_lastname_count_0_by_30',
          'ssn_name_count_0_by_30',
```

```
'name_dob_count_0_by_14',
'name_dob_count_7',
'ssn_dob_count_7',
'ssn_lastname_count_0_by_14',
'ssn_firstname_count_7',
'name_dob_count_0_by_30',
'ssn_name_dob_count_0_by_14',
'ssn_lastname_count_7',
'ssn_name_count_0_by_14',
'fulladdress_homephone_count_0_by_14',
'ssn_name_count_7',
'ssn_name_count_7',
'ssn_name_dob_count_7',
'zip5_count_7']
```

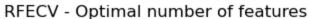
Wrapper

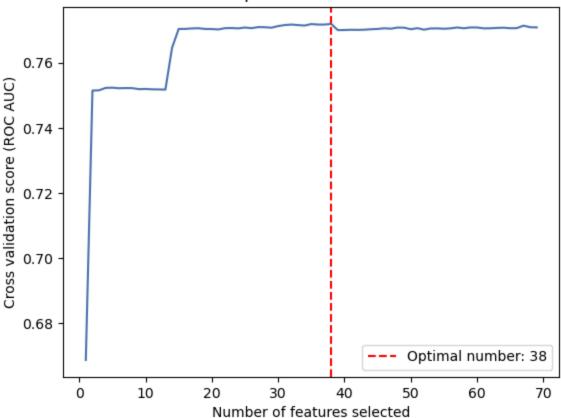
```
In [9]: newX = data.drop(['fraud_label'],axis=1).loc[:,cols_keep]
y = data.fraud_label
del data
```

```
In [10]: from sklearn.pipeline import Pipeline
         from sklearn.preprocessing import StandardScaler
         from sklearn.linear_model import LogisticRegression
         from sklearn.feature_selection import RFECV
         # Create the pipeline to avoid data leakage
         # first standardized, then build logistic regression model
         pipeline = Pipeline([
             ('scaler', StandardScaler()),
             ('logreg', LogisticRegression(max_iter=1000))
         ])
         # Define a custom importance getter function
         def get_coef(estimator):
             return abs(estimator.named steps['logreg'].coef [0])
         # Use the custom importance getter in RFECV
         rfecv = RFECV(
             estimator=pipeline,
             step=1,
             cv=3,
             scoring='roc_auc',
             verbose=3,
             n jobs=-1,
             importance_getter=get_coef
         rfecv.fit(newX, y)
```

```
Fitting estimator with 69 features.
        Fitting estimator with 68 features.
        Fitting estimator with 67 features.
        Fitting estimator with 66 features.
        Fitting estimator with 65 features.
        Fitting estimator with 64 features.
        Fitting estimator with 63 features.
        Fitting estimator with 62 features.
        Fitting estimator with 61 features.
        Fitting estimator with 60 features.
        Fitting estimator with 59 features.
        Fitting estimator with 58 features.
        Fitting estimator with 57 features.
        Fitting estimator with 56 features.
        Fitting estimator with 55 features.
        Fitting estimator with 54 features.
        Fitting estimator with 53 features.
        Fitting estimator with 52 features.
        Fitting estimator with 51 features.
        Fitting estimator with 50 features.
        Fitting estimator with 49 features.
        Fitting estimator with 48 features.
        Fitting estimator with 47 features.
        Fitting estimator with 46 features.
        Fitting estimator with 45 features.
        Fitting estimator with 44 features.
        Fitting estimator with 43 features.
        Fitting estimator with 42 features.
        Fitting estimator with 41 features.
        Fitting estimator with 40 features.
        Fitting estimator with 39 features.
Out[10]: •
                       RFECV
                 estimator: Pipeline
                  StandardScaler
              ▶ LogisticRegression
```

```
plt.savefig('./plots/RFECV.png', dpi=300, bbox_inches='tight')
plt.show()
```





```
In [12]: selected_feature_names = list(newX.columns[rfecv.support_])
    print(f"{rfecv.n_features_} selected feature names: {selected_feature_names}

# Show all features with their rankings
    feature_ranking_df = pd.DataFrame({
        'feature': newX.columns,
        'ranking': rfecv.ranking_
}).sort_values('ranking')
    print("\nFeature rankings:")
    with pd.option_context('display.max_rows', None):
        print(feature_ranking_df)
```

38 selected feature names: ['fulladdress_count_30', 'address_count_14', 'ful laddress_count_14', 'address_count_7', 'fulladdress_count_7', 'fulladdress_count_0_by_7', 'address_count_1', 'fulladdress_count_1', 'ssn_dob_count_30', 'ssn_count_30', 'ssn_ssn_count_30', 'ssn_firstname_count_30', 'ssn_lastname_count_30', 'fulladdress_homephone_count_30', 'ssn_name_dob_count_30', 'name_dob_count_30', 'ssn_ssn_count_14', 'ssn_count_14', 'ssn_lastname_count_14', 'ssn_firstname_count_14', 'zip5_count_1', 'ssn_lastname_count_14', 'zip5_count_3', 'name_dob_count_14', 'ssn_name_count_14', 'ssn_name_dob_count_14', 'ssn_name_count_14', 'fulladdress_homephone_count_7', 'fulladdress_homephone_count_0_by_30', 'ssn_firstname_count_0_by_30', 'ssn_ssn_count_0_by_30', 'ssn_ssn_count_0_by_30', 'name_dob_count_0_by_30', 'ssn_name_count_0_by_30', 'name_dob_count_0_by_30']

Feature rankings:

геа	ture rankings:	
	feature	ranking
0	fulladdress_count_30	1
28	ssn_count_14	1
29	ssn_dob_count_14	1
30	ssn_firstname_count_14	1
31	zip5_count_1	1
33	ssn_lastname_count_14	1
35	name_dob_count_14	1
36	ssn_name_count_14	1
37	ssn_name_dob_count_14	1
39	ssn_name_dob_count_0_by_30	1
41	fulladdress_count_1_by_14	1
42	fulladdress_homephone_count_7	1
45	fulladdress_homephone_count_0_by_30	1
46	ssn_dob_count_0_by_14	1
47	ssn_ssn_count_0_by_30	1
51	ssn_firstname_count_0_by_14	1
53	ssn_ssn_count_7	1
54	ssn_lastname_count_0_by_30	1
55	ssn_name_count_0_by_30	1
61	name_dob_count_0_by_30	1
27	ssn_ssn_count_14	1
23	ssn_name_count_30	1
34	zip5_count_3	1
21	ssn_name_dob_count_30	1
1	address_count_14	1
2	fulladdress_count_14	1
3	address_count_7	1
20	fulladdress_homephone_count_30	1
19	ssn_lastname_count_30	1
18	ssn_firstname_count_30	1
17	ssn_ssn_count_30	1
16	ssn_count_30	1
4	fulladdress_count_7	1
15	ssn dob count 30	1
22	name_dob_count_30	1
14	fulladdress_count_1	1
13	address_count_1	1
12	fulladdress_count_0_by_7	1
68	zip5_count_7	2
49	ssn_count_0_by_30	3
	22222_07_00	

```
43
                               ssn_count_0_by_14
                                                         4
                                                         5
        10
                           address_count_0_by_30
        50
                     ssn firstname count 0 by 30
                                                         6
                  fulladdress_homephone_count_14
                                                         7
        26
        44
                           ssn_ssn_count_0_by_14
                                                         8
        40
                           address_count_1_by_14
                                                         9
        59
                      ssn_lastname_count_0_by_14
                                                        10
        5
                           address_count_0_by_14
                                                        11
        6
                       fulladdress count 0 by 14
                                                        12
        24
                        fulladdress_count_0_by_3
                                                        13
        7
                                 address_count_3
                                                        14
        48
                                                        15
                                   name_count_14
        32
                                   name_count_30
                                                        16
        52
                                                        17
                                     ssn_count_7
        58
                                 ssn dob count 7
                                                        18
        38
                           ssn_dob_count_0_by_30
                                                        19
        64
                          ssn_name_count_0_by_14
                                                        20
        8
                             fulladdress_count_3
                                                        21
        11
                            address_count_0_by_7
                                                        22
        25
                            address_count_0_by_3
                                                        23
        9
                       fulladdress_count_0_by_30
                                                        24
        56
                          name_dob_count_0_by_14
                                                        25
            fulladdress_homephone_count_0_by_14
        65
                                                        26
        60
                           ssn_firstname_count_7
                                                        27
        63
                            ssn_lastname_count_7
                                                        28
        62
                      ssn_name_dob_count_0_by_14
                                                        29
        57
                                name_dob_count_7
                                                        30
        67
                            ssn name dob count 7
                                                        31
        66
                                ssn_name_count_7
                                                        32
In [13]: del newX, y
In [14]: final_cut = pd.read_csv('./data/vars 485.csv', index_col=0)
         final_cut = final_cut[selected_feature_names + ['fraud_label']]
         final_cut.to_csv('./data/selected.csv')
```

Standardization

```
In [2]: #final_cut = pd.read_csv('./data/vars 485.csv', index_col=0)
In [15]: label = final_cut.fraud_label
label.shape
Out[15]: (981694,)
In [16]: only_feature = final_cut.drop(['fraud_label'], axis=1)
    print('features shape: ', only_feature.shape)
    std = only_feature.mean()
    z_scaled = (only_feature - mean)/std
    del final_cut
    # Prevent extreme values after z-scaled
```

```
z_scaled = z_scaled.clip(lower=-1000, upper=1000)
z_scaled.describe()
```

features shape: (981694, 38)

Out[16]:

		fulladdress_count_30	address_count_14	fulladdress_count_14	address_count_
	count	9.816940e+05	9.816940e+05	9.816940e+05	9.816940e+C
	mean	-1.779950e-16	1.749262e-16	-1.817588e-16	4.771240e - ′
	std	1.000000e+00	1.000000e+00	1.000000e+00	1.000000e+C
	min	-1.014801e-01	-8.811756e-02	-7.861317e-02	-7.224399e-C
	25%	-1.014801e-01	-8.811756e-02	-7.861317e-02	-7.224399e-C
	50%	-1.014801e-01	-8.811756e-02	-7.861317e-02	-7.224399e-C
	75%	-1.014801e-01	-8.811756e-02	-7.861317e-02	-7.224399e-C
	max	4.534025e+01	4.648183e+01	4.733666e+01	4.903885e+(

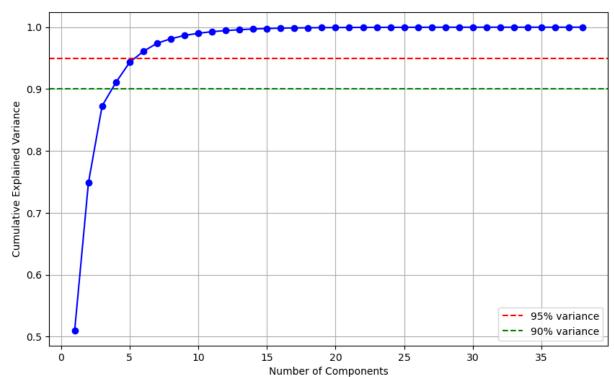
8 rows × 38 columns

```
In [17]: z_scaled['fraud_label']=label
z_scaled.to_csv('./data/z_scaled.csv')
```

Feature Reduction

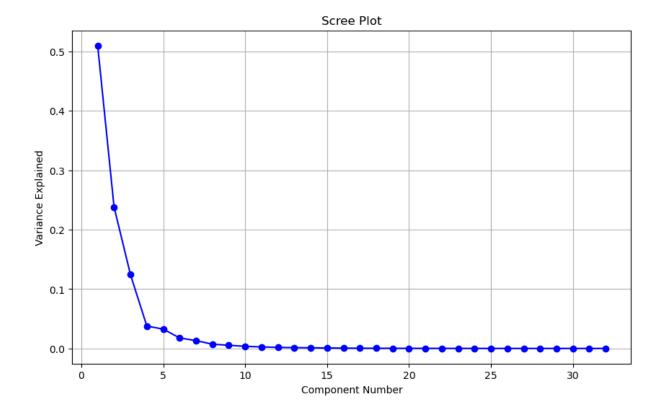
```
In [18]: from sklearn.decomposition import PCA
         X = z_scaled.drop(['fraud_label'], axis=1)
         y = z scaled.fraud label
         # Fit PCA with all components
         pca = PCA()
         pca.fit(X)
         # Calculate cumulative variance explained
         cumsum_var = np.cumsum(pca.explained_variance_ratio_)
         # Plot the results
         plt.figure(figsize=(10, 6))
         plt.plot(range(1, len(cumsum_var) + 1), cumsum_var, 'bo-')
         plt.xlabel('Number of Components')
         plt.ylabel('Cumulative Explained Variance')
         plt.axhline(y=0.95, color='r', linestyle='--', label='95% variance')
         plt.axhline(y=0.90, color='g', linestyle='--', label='90% variance')
         plt.legend()
         plt.grid(True)
         plt.show()
         # Find number of components for desired variance
         n_components_95 = round(np.argmax(cumsum_var >= 0.95))
```

```
n_components_90 = round(np.argmax(cumsum_var >= 0.90))
print(f"Components for 95% variance: {n_components_95}")
print(f"Components for 90% variance: {n_components_90}")
```



Components for 95% variance: 5 Components for 90% variance: 3

```
In [19]: # Plot individual variance explained
plt.figure(figsize=(10, 6))
plt.plot(range(1, 33), pca.explained_variance_ratio_[:32], 'bo-')
plt.xlabel('Component Number')
plt.ylabel('Variance Explained')
plt.title('Scree Plot')
plt.grid(True)
plt.show()
```



split statistics to about 80% train, test set (X, y will be divided by train_test_split function) and 20% Out Of Time (OOT)

```
In [20]: total = X.shape[0]
         X = X[0:round(total*0.8)]
         y = y[0:round(total*0.8)]
         X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3)
In [21]: from sklearn.model_selection import cross_val_score
         from sklearn.ensemble import RandomForestClassifier
         from sklearn.pipeline import Pipeline
         # Test different numbers of components
         n_{components\_range} = [3, 5, 7, 10]
         cv_scores = []
         for n in n components range:
             pipeline = Pipeline([
                  ('scaler', StandardScaler()),
                  ('pca', PCA(n_components=n)),
                  ('classifier', RandomForestClassifier(n_estimators=100, random_state
             1)
             scores = cross_val_score(pipeline, X_train, y_train, cv=5, scoring='roc_
             cv_scores.append(scores.mean())
             print(f"n_components={n}, AUC={scores.mean():.4f} (+/- {scores.std():.4f
         # Plot results
         plt.figure(figsize=(10, 6))
         plt.plot(n components range, cv scores, 'bo-')
         plt.xlabel('Number of PCA Components')
```

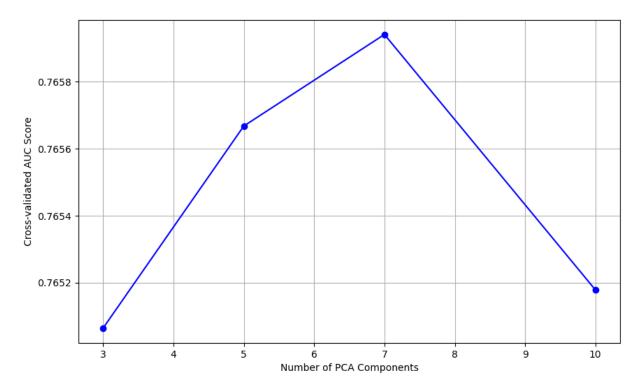
```
plt.ylabel('Cross-validated AUC Score')
plt.grid(True)
plt.show()
```

```
n_{components=3}, AUC=0.7651 (+/- 0.0043)
Fitting estimator with 69 features.
Fitting estimator with 68 features.
Fitting estimator with 67 features.
Fitting estimator with 66 features.
Fitting estimator with 65 features.
Fitting estimator with 64 features.
Fitting estimator with 63 features.
Fitting estimator with 62 features.
Fitting estimator with 61 features.
Fitting estimator with 60 features.
Fitting estimator with 59 features.
Fitting estimator with 58 features.
Fitting estimator with 57 features.
Fitting estimator with 56 features.
Fitting estimator with 55 features.
Fitting estimator with 54 features.
Fitting estimator with 53 features.
Fitting estimator with 52 features.
Fitting estimator with 51 features.
Fitting estimator with 50 features.
Fitting estimator with 49 features.
Fitting estimator with 48 features.
Fitting estimator with 47 features.
Fitting estimator with 46 features.
Fitting estimator with 45 features.
Fitting estimator with 44 features.
Fitting estimator with 43 features.
Fitting estimator with 42 features.
Fitting estimator with 41 features.
Fitting estimator with 40 features.
Fitting estimator with 39 features.
Fitting estimator with 38 features.
Fitting estimator with 37 features.
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Fitting estimator with 34 features.
Fitting estimator with 33 features.
Fitting estimator with 32 features.
Fitting estimator with 31 features.
Fitting estimator with 30 features.
Fitting estimator with 29 features.
Fitting estimator with 28 features.
Fitting estimator with 27 features.
Fitting estimator with 26 features.
Fitting estimator with 25 features.
Fitting estimator with 24 features.
Fitting estimator with 23 features.
Fitting estimator with 22 features.
Fitting estimator with 21 features.
Fitting estimator with 20 features.
Fitting estimator with 19 features.
Fitting estimator with 18 features.
Fitting estimator with 17 features.
Fitting estimator with 16 features.
Fitting estimator with 15 features.
```

```
Fitting estimator with 14 features.
Fitting estimator with 13 features.
Fitting estimator with 12 features.
Fitting estimator with 11 features.
Fitting estimator with 10 features.
Fitting estimator with 9 features.
Fitting estimator with 8 features.
Fitting estimator with 7 features.
Fitting estimator with 6 features.
Fitting estimator with 5 features.
Fitting estimator with 4 features.
Fitting estimator with 3 features.
Fitting estimator with 2 features.
Fitting estimator with 69 features.
Fitting estimator with 68 features.
Fitting estimator with 67 features.
Fitting estimator with 66 features.
Fitting estimator with 65 features.
Fitting estimator with 64 features.
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Fitting estimator with 34 features.
Fitting estimator with 33 features.
Fitting estimator with 32 features.
Fitting estimator with 31 features.
Fitting estimator with 30 features.
Fitting estimator with 29 features.
Fitting estimator with 28 features.
Fitting estimator with 27 features.
```

```
Fitting estimator with 26 features.
Fitting estimator with 25 features.
Fitting estimator with 24 features.
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Fitting estimator with 6 features.
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Fitting estimator with 40 features.
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```

```
Fitting estimator with 38 features.
Fitting estimator with 37 features.
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Fitting estimator with 15 features.
Fitting estimator with 14 features.
Fitting estimator with 13 features.
Fitting estimator with 12 features.
Fitting estimator with 11 features.
Fitting estimator with 10 features.
Fitting estimator with 9 features.
Fitting estimator with 8 features.
Fitting estimator with 7 features.
Fitting estimator with 6 features.
Fitting estimator with 5 features.
Fitting estimator with 4 features.
Fitting estimator with 3 features.
Fitting estimator with 2 features.
n components=5, AUC=0.7657 (+/- 0.0035)
n_{components=7}, AUC=0.7659 (+/- 0.0042)
n_components=10, AUC=0.7652 (+/- 0.0044)
```



```
In [22]: X = z_scaled.drop(['fraud_label'], axis=1)
y = z_scaled.fraud_label

# Apply PCA with 5 components
pca = PCA(n_components=5)
X_pca = pca.fit_transform(X)
pca_columns = [f'PC{i+1}' for i in range(5)]
df_pca = pd.DataFrame(X_pca, columns=pca_columns)
df_pca['fraud'] = y
df_pca.to_csv('./data/reduced_pca.csv')
```

In []: