

Bounding Techniques for Dynamic Partial Order Reduction

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Summary

Aim of Thesis

- Implement Preemption Bounded Search (BPOR) for Nidhugg.

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- Explore the potential of Source-Sets for BPOR.

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- Explore the potential of Source-Sets for BPOR.
- Evaluate the performance of various BPOR implementations.
- Explore alternative approaches to BPOR problem.

Section 1

Background Knowledge

Concurrent Computing and Problems

Concurrent Computing: Concurrent computing is a form of computing in which several computations are executed during overlapping time periods-concurrently-instead of sequentially (one completing before the next starts).

Potential problems include:

- Race Conditions

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Concurrent Computing: Concurrent computing is a form of computing in which several computations are executed during overlapping time periods-concurrently-instead of sequentially (one completing before the next starts).

Potential problems include:

- Race Conditions
- Deadlocks
- Livelocks
- Resource Starvation

Concurrency Errors

To be a Concurrency Error or not to be...

```
void *divider(void* arg){  
    int x = 0;  
    return 42/x;  
}
```

Listing 1: Example of non-concurrency error

```
volatile int x = 1;  
void *divider(){  
    return 42/x;  
}  
  
void *zero(){  
    x = 0;  
}
```

Listing 2: Example of concurrency error

Testing, Model Checking, and Verification

- Testing: For some given inputs check whether the output is correct.
- Verification: Prove formally that the output is correct.
- Model Checking: Explore all the possible states the system can be.

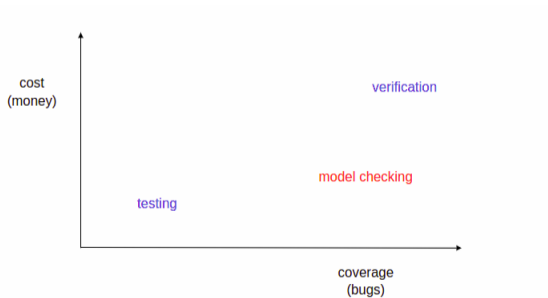


Figure: Comparing Testing, Model Checking and Verification

But What's Our State Space?

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- We need to model our state space!
- An Interleaving represents a scheduling of the concurrent program.
- In order to find an error of a concurrent program, one must examine every possible interleaving BUT leads to STATE EXPLOSION!

Stateless Model Checking and Partial Order Reduction

Partial order reduction aims to reduce the number of interleavings explored by eliminating the exploration of equivalent interleavings.

For example:

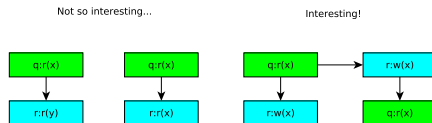


Figure: Examples of Interleavings

Stateless Model Checking and Partial Order Reduction

- Static Partial Order Reduction: Dependencies are tracked before execution.

Stateless Model Checking and Partial Order Reduction

- Static Partial Order Reduction: Dependencies are tracked before execution.
- Dynamic Partial Order Reduction: Dependencies are observed during runtime.

Bounding Techniques for DPOR

- For larger programs DPOR often runs longer than developers are willing to wait.

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- For larger programs DPOR often runs longer than developers are willing to wait.
- Bounded techniques, alleviate state-space explosion by pruning the executions that exceed a bound.
- Preemption Bounded and Delay Bounded exploration.
- Many of the concurrency bugs can be tracked even when the bound limit is set to be small.

General form of DPOR

Explore(\emptyset);

Function *Explore*(E)

let $T = \text{Sufficient_set}(\text{final}(E))$;

for *all* $t \in T$ **do**

 Explore($E.t$) ;

end

Algorithm 1: General form of DPOR

The implemented DPOR form

Explore(\emptyset);

Function *Explore*(*E*)

if *suitable* *p* *exists* **then**

backtrack(*E*) := *p* ;

 add to previous *backtracks* threads due to dependencies revealed by *p*;

while $\exists p \in \textit{backtrack}$ **do**

 | *Explore*(*E.p*) ;

end

end

Algorithm 2: Real DPOR Algorithm

Definition 1 (Sufficient Sets)

A set of transitions is sufficient in a state s if any relevant state reachable via an enabled transition from s is also reachable from s via at least one of the transitions in the sufficient set. A search can thus explore only the transitions in the sufficient set from s because all relevant states still remain reachable. The set containing all enabled threads is trivially sufficient in s , but smaller sufficient sets enable more state space reduction.

Sufficient Sets: Persistent Sets

Definition 2 (Persistent Sets)

Let s be a state, and let $W \subseteq E(s)$ be a set of execution sequences from s . A set T of transitions is a persistent set for W after s if for each prefix w of some sequence in W , which contains no occurrence of a transition in T , we have $E \vdash t \Diamond w$ for each $t \in T$.

Sufficient Sets: Persistent Sets

A simple example:

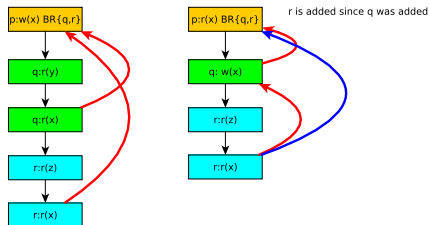


Figure: Construction of persistent sets

Sufficient Sets: Source Sets

Definition 3 (Initials after an execution sequence $E.w$, $I_{[E]}(w)$)

$p \in I_{[E]}(w)$ if and only if there is a sequence w' such that $E.w \simeq E.p.w'$.

Definition 4 (Weak Initials after an execution sequence $E.w$, $WI_{[E]}(w)$)

$p \in WI_{[E]}(w)$ if and only if there are sequences w' and v such that $E.w.v \simeq E.p.w'$.

Sufficient Sets: Source Sets

Definition 5 (Source Sets)

Let E be an execution sequence, and let W be a set of sequences, such that $E.w$ is an execution sequence for each $w \in W$. A set T of processes is a source set for W after E if for each $w \in W$ we have $WI_{[E]}(w) \cap T \neq \emptyset$.

Source Sets

An example:

We don't need to add r since q already belongs to source set.

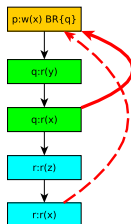


Figure: Construction of Source Sets

Further Optimizations: Sleep Sets

The idea behind Sleep Set Optimization:

- Assume that the search explores transition t from state s , backtracks t , then explores t_0 from s instead. Unless the search explores a transition that is dependent with t , no states are reachable via t_0 that were not already reachable via t from s . Thus, t “sleeps” unless a dependent transition is explored.

Sleep Sets

Sleeps sets in action (Using Persistent Sets):

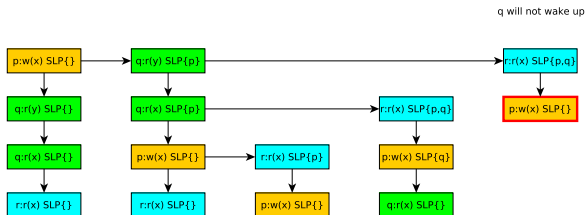


Figure: Example of Sleep Set Optimization

Bounded Dynamic Partial Order Reduction General Form

Given a bound evaluation function B_v and a bound c :

Result: Explore the whole statespace

Explore(\emptyset);

Function *Explore*(E)

$T = \text{Sufficient_set}(\text{final}(E))$

for all $t \in T$ **do**

if $B_v(E.t) \leq c$ **then**

 Explore($E.t$)

end

end

Algorithm 3: Bounded-DPOR

Preemption Bounded Search

Definition 6 (Preemption bound)

$$P_b(\emptyset) = 0$$

$$P_b(E.t) =$$

$$\begin{cases} P_b(E) + 1 & \text{if } t.tid = last(E).tid \text{ and } last(E).tid \in enabled(final(E)) \\ P_b(E) & \text{otherwise} \end{cases}$$

Definition 7 ($ext(s, t)$)

Given a state $s = final(E)$ and a transition $t \in enabled(s)$, $ext(s, t)$ returns the unique sequence of transitions β from s such that

1. $\forall i \in dom(\beta) : \beta_i.tid = t.tid$
2. $t.tid \notin enabled(final(E.\beta))$

Preemption Bounded Persistent Sets

Definition 8 (Preemption Bounded Persistent Set)

A set $T \subseteq \mathcal{T}$ of transitions enabled in a state $s = \text{final}(E)$ is preemption-bound persistent in s iff for all nonempty sequences a of transitions from s in $A_G(P_b, c)$ such that $\forall i \in \text{dom}(a), a_i \notin T$ for all $t \in T$,

1. $Pb(E.t) \leq Pb(E.a_1)$
2. if $Pb(E.t) < Pb(E.a_1)$, then $t \leftrightarrow \text{last}(a)$ and $t \leftrightarrow \text{next}(\text{final}(E.a), \text{last}(a).tid)$
3. if $Pb(E.t) = Pb(E.a_1)$, then $\text{ext}(s, t) \leftrightarrow \text{last}(a)$ and $\text{ext}(s, t) \leftrightarrow \text{next}(\text{final}(E.a), \text{last}(a).tid)$

Preemption Bounded Persistent Sets

Way simplified... :

- Add conservative branches at the beginning of the block.

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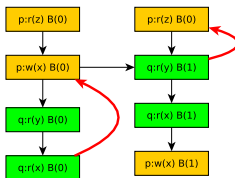


Figure: Example of Blocks and Bound Persistent Sets

Source-DPOR

```

Explore( $\langle \rangle, \emptyset$ );
Function Explore( $E, Sleep$ )
  if  $\exists p \in (enabled(s_{[E]}) \setminus Sleep)$  then
     $backtrack(E) := p$  ;
    while  $\exists p \in (backtrack(E) \setminus Sleep)$  do
      foreach  $e \in dom(E)$  such that  $e \lesssim_{E.p} next_{[E]}(p)$  do
        let  $E' = pre(E, e)$ ;
        let  $u = notdep(e, E).p$ ;
        if  $I_{E'}(u) \cap backtrack(E') = \emptyset$  then
          | add some  $q' \in I_{[E']}(u)$  to  $backtrack(E')$  ;
        end
      end
      let  $Sleep' := \{q \in Sleep \mid E \models p \Diamond q\}$ ;
      Explore( $E.p, Sleep'$ ) ;
      add  $p$  to  $Sleep$  ;
    end
  end

```

Algorithm 4: Source-DPOR Algorithm

DPOR using Clock Vectors (Classic-DPOR)

Function *Explore*(E, C)

```

let  $s := \text{last}(E)$ ;
for all process  $p$  do
  if  $\exists i = \max(\{i \in \text{dom}(E) \mid E_i \text{ is dependent and may be co-enabled with}$ 
     $\text{next}(s, p) \text{ and } i \notin C(p)(\text{proc}(E_i))\})$  then
    if  $p \in \text{enabled}(\text{pre}(E, i))$  then
       $\text{add } p \text{ to } \text{backtrack}(\text{pre}(E, i))$  ;
    else
       $\text{add } \text{enabled}(\text{pre}(E, i)) \text{ to } \text{backtrack}(\text{pre}(E, i))$  ;
    end
  end
end
if  $\exists p \in \text{enabled}(s)$  then
   $\text{backtrack}(s) := p$  ;
  let  $\text{done} = \emptyset$ ;
  while  $\exists p \in (\text{backtrack}(s) \setminus \text{done})$  do
     $\text{add } p \text{ to } \text{done}$  ;
    let  $t = \text{next}(s, p)$ ;
    let  $E' = E.t$ ;
    let  $cu = \max\{C(i) \mid i \in 1..|S| \text{ and } E_i \text{ dependent with } t\}$ ;
    let  $cu2 = cu[p := |E'|]$ ;
    let  $C' = C[p := cu2, |E'| := cu2]$ ;
     $\text{Explore}(E', C')$  ;
  end
end

```

Algorithm 5: DPOR using Clock Vectors (Classic-DPOR)

Source-DPOR vs Classic-DPOR

Similarities:

1. Consist of the same phases i.e., race detection and exploration
2. Both rely on Vector Clocks.

Differences:

1. Classic-DPOR “eager” i.e., adds more dependencies before scheduling.
2. Source-DPOR “lazy” i.e., adds branches after scheduling and thus avoids redundant additions.

Section 2

Implemented Algorithms

Nidhugg-DPOR

```

Explore( $\langle \rangle, \emptyset$ );
Function Explore(E, Sleep)
  if  $\exists p \in (\text{enabled}(s_{[E]}) \setminus \text{Sleep})$  then
    backtrack(E) := p ;
    while  $\exists p \in (\text{backtrack}(\text{E}) \setminus \text{Sleep})$  do
      foreach e  $\in \text{dom}(\text{E})$  such that  $e \lesssim_{E.p} \text{next}_{[E]}(p)$  do
        let  $E' = \text{pre}(E, e)$ ;
        let  $u = \text{notdep}(e, E).p$ ;
        let  $CI = \{i \in I_{E'}(u) \mid i \rightarrow p\}$ ;
        if  $CI \cap \text{backtrack}(E') = \emptyset$  then
          if  $CI \neq \emptyset$  then
            | add some  $q' \in CI$  to  $\text{backtrack}(E')$  ;
          end
          else
            | add some  $q' I_{E'}(u)$  to  $\text{backtrack}(E')$ 
          end
        end
      end
    let  $\text{Sleep}' := \{q \in \text{Sleep} \mid E \models p \diamond q\}$  ;
    Explore(E.p, Sleep') ;
    add p to Sleep ;
  end
end

```

Algorithm 6: Nidhugg-DPOR

Correctness of Nidhugg-DPOR

Case 1: At least one process contains a write command. We know that the two processes will be inverted at some point. Since Nidhugg-DPOR ignores weak initials it will branch both processes. In Source-DPOR only one of the two processes should be branched since they share the same initials. However, in Nidhugg-DPOR this is not true since the CI set does not contain steps from the other process.

When r is added q is not considered since it does not belong to CI
in contrast to I set of Source DPOR

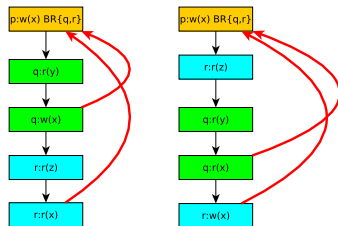


Figure: Construction of persistent sets in Nidhugg when there is a write process

Correctness of Nidhugg-DPOR

Case 2: Both processes are read operations. Since we do not calculate I but CI the first read operation will not be considered as it does not happen before the second read operation and as result both processes will be added to *backtrack*. We notice that by calculating the CI set when the race between p and r is detected q process will be ignored and, thus, r will be added as a branch.

When r is added q is not considered since it does not belong to CI
in contrast to I set of Source DPOR

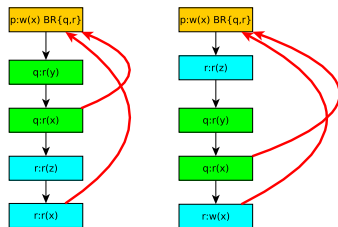


Figure: Construction of persistent sets in Nidhugg when both are read processes

Naive-BPOR

```

Explore( $\langle \rangle, \emptyset, b$ );
Function Explore( $E, Sleep, b$ )
  if  $\exists p \in (enabled(s_{[E]}) \setminus Sleep)$  such that  $B_v(E.p) \leq b$  then
    backtrack( $E$ ) :=  $p$  ;
    while  $\exists p \in (backtrack(E) \setminus Sleep)$  and  $B_v(E.p) \leq b$  do
      foreach  $e \in dom(E)$  such that  $e \lesssim_{E.p} next_{[E]}(p)$  do
        let  $E' = pre(E, e)$ ;
        let  $u = notdep(e, E).p$ ;
        if  $I_{E'}(u) \cap backtrack(E') = \emptyset$  then
          add some  $q' \in I_{[E']}(u)$  to  $backtrack(E')$  ;
        end
      end
      let  $Sleep' := \{q \in Sleep \mid E \models p \Diamond q\}$ ;
      Explore( $E.p, Sleep', b$ ) ;
      add  $p$  to  $Sleep$  ;
    end
  end

```

Algorithm 7: Naive-BPOR

Example execution of Naive-BPOR

A Naive-BPOR execution example and the problem with it.

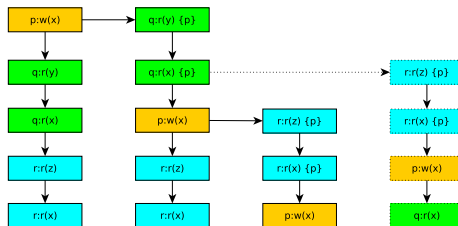


Figure: Naive-BPOR for bound=0

Classic-BPOR

```

Function Explore( $E$ )
  let  $s := \text{last}(E)$ ;
  for all process  $p$  do
    for all process  $q \neq p$  do
      if  $\exists i = \max(\{i \in \text{dom}(E) \mid E_i \text{ is dependent and may be co-enabled}$ 
        with  $\text{next}(s, p) \text{ and } E_i.\text{tid} = q\}$  then
        if  $p \in \text{enabled}(\text{pre}(E, i))$  then
          add  $p$  to  $\text{backtrack}(\text{pre}(E, i))$  ;
        else
          add  $\text{enabled}(\text{pre}(E, i))$  to  $\text{backtrack}(\text{pre}(E, i))$  ;
        end
      if  $j = \max(\{j \in \text{dom}(E) \mid j = 0 \text{ or } S_{j-1}.\text{tid} \neq S_j.\text{tid} \text{ and } j < i\})$ 
        then
          if  $p \in \text{enabled}(\text{pre}(E, i))$  then
            add  $p$  to  $\text{backtrack}(\text{pre}(E, i))$  ;
          else
            add  $\text{enabled}(\text{pre}(E, i))$  to  $\text{backtrack}(\text{pre}(E, i))$  ;
          end
        end
      end
    end
  end
  if  $p \in \text{enabled}(s)$  then
    add  $p$  to  $\text{backtrack}(s)$  ;
  end
  else
    add any  $u \in \text{enabled}(s)$  to  $\text{backtrack}(s)$  ;
  end
  let  $\text{visited} = \emptyset$ ;
  while  $\exists u \in (\text{enabled}(s) \cap \text{backtrack}(s) \setminus \text{visited})$  do
    add  $u$  to  $\text{visited}$  ;
    if  $(B_v(S.\text{next}(s, u)) \leq c)$  then
      Explore( $S.\text{next}(s, u)$ ) ;
    end
  end

```

Algorithm 8: BPOR

Nidhugg-BPOR

Explore($\langle \rangle, \emptyset, b$);

Function Explore(E, Sleep, b)

```

if  $\exists p \in ((\text{enabled}(s_{[E]}) \setminus \text{Sleep}) \text{ and } B_v(E.p) \leq b)$  then
  backtrack( $E$ ) :=  $p$  ;
  while  $\exists p \in (\text{backtrack}(E) \setminus \text{Sleep} \text{ and } B_v(E.p) \leq b)$  do
    foreach  $e \in \text{dom}(E)$  such that  $e \lesssim_{E.p} \text{next}_{[E]}(p)$  do
      let  $E' = \text{pre}(E, e)$ ;
      let  $u = \text{notdep}(e, E).p$ ;
      let  $CI = \{i \in I_{E'}(u) \mid i \rightarrow p\}$ ;
      if  $CI \cap \text{backtrack}(E') = \emptyset$  then
        if  $CI \neq \emptyset$  then
          | add some  $q' \in CI$  to  $\text{backtrack}(E')$  ;
        end
        else
          | add some  $q' \in I_{[E']}(u)$  to  $\text{backtrack}(E')$  ;
        end
      end
      let  $E'' = \text{pre\_block}(e, E)$ ;
      let  $u = \text{notdep}(e, E).p$ ;
      let  $CI = \{i \in I_{E''}(u) \mid i \rightarrow p\}$ ;
      if  $CI \cap \text{backtrack}(E') = \emptyset$  then
        if  $CI \neq \emptyset$  then
          | add some  $q' \in CI$  to  $\text{backtrack}(E')$  ;
        end
        else
          | add some  $c(q') \in I_{[E'']}(u)$  to  $\text{backtrack}(E'')$  ;
        end
      end
    end
  end
  let  $\text{Sleep}' := \{q \in \text{Sleep} \mid E \models p \Diamond q\}$  ;
  Explore( $E.p, \text{Sleep}'$ ) ;
  if  $p$  is not conservative then
    | add  $p$  to  $\text{Sleep}$  ;
  end
end

```

The main question

Can we use source sets instead of persistent sets in order implement BPOR?

First approach

We should use Source Sets for both conservative and non-conservative branches.

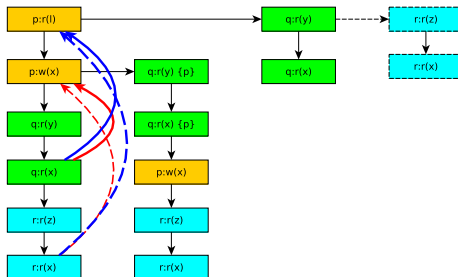


Figure: Following source sets for conservative branches

A Correct Approach

We should use Source Sets for non-conservative branches and persistent sets for conservative branches.

Source-BPOR

```

Explore( $\langle \rangle, \emptyset, b$ );
Function Explore( $E, Sleep, b$ )
  if  $\exists p \in ((enabled(s_{[E]}) \setminus Sleep) \text{ and } B_v(E.p) \leq b)$  then
    backtrack( $E$ ) :=  $p$  ;
    while  $\exists p \in (backtrack(E) \setminus Sleep \text{ and } B_v(E.p) \leq b)$  do
      foreach  $e \in dom(E)$  such that  $e \lesssim_{E.p} next_{[E]}(p)$  do
        let  $E' = pre(E, e)$ ;
        let  $u = notdep(e, E).p$ ;
        if  $I_{E'}(u) \cap backtrack(E') = \emptyset$  then
          | add some  $q' \in I_{E'}(u)$  to  $backtrack(E')$  ;
        end
        let  $E'' = pre\_block(e, E)$ ;
        let  $u = notdep(e, E).p$ ;
        let  $CI = \{i \in I_{E''}(u) \mid i \rightarrow p\}$ ;
        if  $CI \cap backtrack(E') = \emptyset$  then
          | if  $CI \neq \emptyset$  then
            | | add some  $q' \in CI$  to  $backtrack(E')$  ;
          | end
          | else
            | | add some  $c(q') \in I_{[E'']}(u)$  to  $backtrack(E'')$  ;
          | end
        end
      end
    end
    let  $Sleep' := \{q \in Sleep \mid E \models p \Diamond q\}$  ;
    Explore( $E.p, Sleep'$ ) ;
    if  $p$  is not conservative then
      | add  $p$  to  $Sleep$  ;
    end
  end
end

```

Algorithm 10: Source-BPOR

Nidhugg-BPOR vs Source-BPOR

Similarities:

- Same structure.

Differences:

- Source-BPOR relies on Source Sets for the addition of non-conservative branches while Nidhugg-BPOR relies on persistent sets.

Conservative Branches

The usage of conservative branches leads to explosion of the state space:

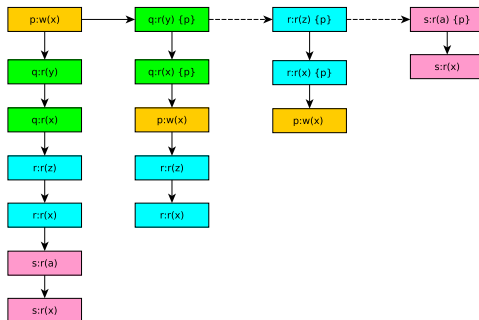


Figure: writer-3-readers explosion

Sleep Sets are no longer that useful:

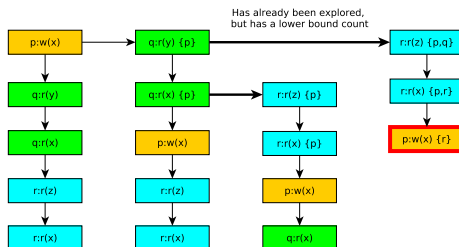


Figure: Sleep set contradiction

Concluding Remarks

The Performance - Soundness Tradeoff

Nidhugg Implementation

Nidhugg is a bug-finding tool which targets bugs caused by concurrency and relaxed memory consistency in concurrent programs. It works on the level of LLVM internal representation, which means that it can be used for programs written in languages such as C or C++.

The Nidhugg Flow Chart

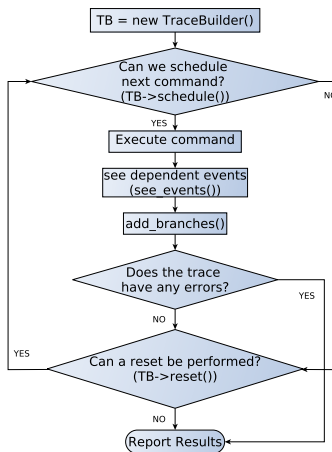


Figure: Nidhugg's Flow Chart

Modifications in Nidhugg

The implementation mainly is focused, as expected, on `see_events()` and `add_branches()`

Section 3

Evaluation

Nidhugg-DPOR Evaluation

Evaluation of Nidhugg-DPOR on Synthetic Tests

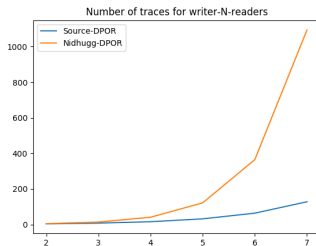


Figure: writer-N-readers

Test case	Traces for Source-DPOR	Traces for Classic-DPOR
account.c	6	7
lazy.c	6	7
micro.c	52495	53084
lastzero.c	97	97
lastzeromod.ll	13	17
indexer0.c	8	8
indexermod.c	120	226

Table: Source-DPOR vs Nidhugg-DPOR for Synthetic tests

Evaluation of Nidhugg-BPOR on Synthetic Tests

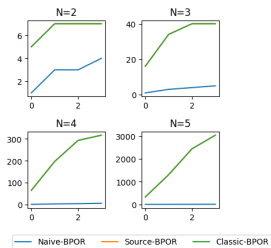


Figure: writer-N-readers bounded

Technique:	Naïve-BPOR			Nidhugg-BPOR			Source-BPOR		
Bound:	0	1	2	0	1	2	0	1	2
account.c	1	1	4	6	27	42	6	27	42
lazy.c	1	1	4	6	27	42	6	27	42
micro.c	1	1	10	6	93	886	6	93	886
lastzero.c	1	2	5	252	2444	10614	252	2444	10614
lastzeromod.ll	1	1	6	64	290	651	64	290	651
indexer0.c	1	4	1	2	8	14	2	8	14
indexermod.c	1	1	5	120	1320	7920	120	1320	7920

Table: Traces for various bound limits

Evaluation of BPOR on RCU

Read-Copy-Update (RCU): Read-copy update (RCU) is a synchronization mechanism that was added to the Linux kernel in October of 2002.

Let's start with a small bound...

ver:	3.0						3.19						4.9.6					
method:	Naive-BPOR			Classic-BPOR			Naive-BPOR			Classic-BPOR			Naive-BPOR			Classic-BPOR		
	traces	time	error	traces	time	error	traces	time	error	traces	time	error	traces	time	error	traces	time	error
-	3	0.2	NF	44	0.72	NF	2	0.32	NF	28	0.76	NF	2	0.61	NF	24	1.21	NF
-DFORCE_FAILURE_1	3	0.2	NF	44	0.72	NF	2	0.32	NF	28	0.76	NF	2	0.6	NF	24	1.21	NF
-DFORCE_FAILURE_3	3	0.2	NF	44	0.72	NF	2	0.32	NF	33	1.06	NF	2	0.61	NF	41	2.11	NF
-DFORCE_FAILURE_5	3	0.2	NF	44	0.71	NF	2	0.31	NF	18	0.55	NF	2	0.6	NF	16	0.93	NF
-DLIVENESS_CHECK_1	3	0.2	NF	44	0.72	NF	2	0.32	NF	28	0.74	NF	2	0.61	NF	24	1.19	NF
-DLIVENESS_CHECK_2	3	0.2	NF	52	0.84	NF	2	0.32	NF	28	0.73	NF	2	0.6	NF	24	1.2	NF
-DLIVENESS_CHECK_3	3	0.2	NF	44	0.71	NF	2	0.31	NF	28	0.75	NF	2	0.6	NF	24	1.19	NF

Table: RCU results for bound $b = 1$

Evaluation of BPOR on RCU

Let's increase the bound...

ver:	3.0						3.19						4.9.6					
method:	Naive-BPOR			Classic-BPOR			Naive-BPOR			Classic-BPOR			Naive-BPOR			Classic-BPOR		
	traces	time	error	traces	time	error	traces	time	error	traces	time	error	traces	time	error	traces	time	error
-	50	1.18	NF	5634	88.78	NF	10	0.49	NF	2083	60.48	NF	10	0.89	NF	2469	122.71	NF
-DFORCE FAILURE 1	50	1.06	NF	275	4.2	F	10	0.49	NF	182	5.51	F	10	0.89	NF	300	15.42	F
-DFORCE FAILURE 3	50	1.05	NF	1627	23.09	NF	15	0.72	NF	100000	0.0	NF	15	1.2	NF	100000	0.0	NF
-DFORCE FAILURE 5	49	1.05	NF	4155	59.47	NF	9	0.45	NF	60	2.34	F	9	0.81	NF	60	3.92	F
-DLIVENESS CHECK 1	48	1.04	NF	1493	21.19	NF	10	0.5	NF	517	10.66	NF	10	0.88	NF	404	13.58	NF
-DLIVENESS CHECK 2	61	1.28	NF	2105	30.5	NF	10	0.5	NF	517	10.61	NF	10	0.88	NF	582	20.28	NF
-DLIVENESS CHECK 3	49	1.04	NF	1788	24.98	NF	10	0.5	NF	655	14.04	NF	10	0.88	NF	506	17.32	NF

Table: RCU results for bound $b = 4$

Evaluation of BPOR on RCU

What did we achieve?

ver:	3.0						3.19						4.9.6					
method:	Source-DPOR			Classic-BPOR			Source-DPOR			Classic-BPOR			Source-DPOR			Classic-BPOR		
	traces	time	bound	traces	time	bound	traces	time	bound	traces	time	bound	traces	time	bound	traces	time	bound
-DFORCE FAILURE 1	247	3.81	F	275	4.2	4	515	16.88	F	182	5.51	4	861	45.69	F	300	15.42	4
-DFORCE FAILURE 3	2372	33.42	NF				17094	626.4	F	201	7.03	2	15349	883.98	F	258	14.24	2
-DFORCE FAILURE 5	12426	178.8	NF				118	3.99	F	60	2.34	4	112	6.34	F	60	3.92	4

Table: Comparison between DPOR and BPOR with the bug

Equivalence of Source-BPOR with Nidhugg-BPOR

Equivalence Case1:

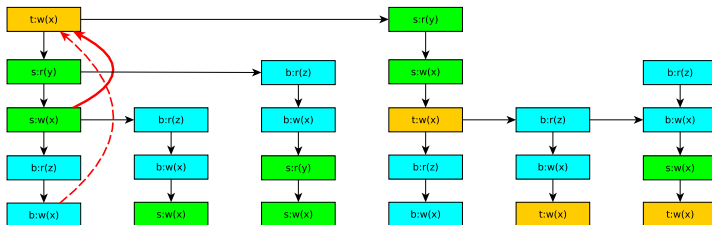


Figure: Source-BPOR and Nidhugg-BPOR equivalence Case 1

Equivalence of Source-BPOR with Nidhugg-BPOR

Equivalence Case2:

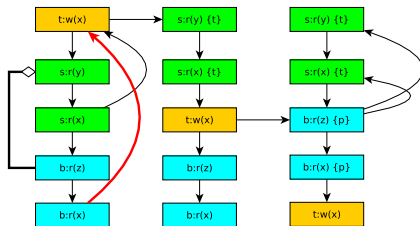


Figure: Source-BPOR and Nidhugg-BPOR equivalence Case 2

Section 4

Further Discussion

Motivation

Some preemption-switches can be easily avoided. For example:

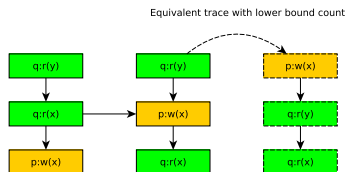


Figure: An example of avoidable preemption-switch

Alternating the General Form of BPOR

What if calculate something more than the preemption-bound?

Result: Explore the whole state space within the bound

Explore(\emptyset);

Function *Explore*(*S*)

$T = \text{Sufficient_set}(\text{final}(S))$ **for all** $t \in T$ **do**

if $\min\{B_v([S.t])\} \leq c$ **then**

 Explore(*S.t*)

end

end

Algorithm 11: General form of the BPOR without branch addition

Applying the Graph Construction Algorithm

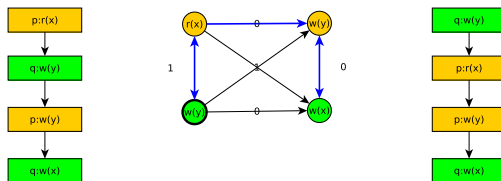


Figure: Graph example

Introducing Lazy-BPOR

```

let  $G =: \emptyset$ ;
Explore( $\langle \rangle, \emptyset, G, b$ );
Function Explore( $E, Sleep, G, b$ )
  if  $\exists p \in (enabled(s_{[E]}) \setminus Sleep)$  such that  $B_v(E.p) \leq b$  then
    backtrack( $E$ ) :=  $p$  ;
    while  $\exists p \in (backtrack(E) \setminus Sleep)$  do
      foreach  $e \in dom(E)$  such that  $e \lesssim_{E.p} next_{[E]}(p)$  do
        let  $E' = pre(E, e)$ ;
        let  $u = notdep(e, E).p$ ;
        if  $I_{E'}(u) \cap backtrack(E') = \emptyset$  then
          | add some  $q' \in I_{[E']}(u)$  to backtrack( $E'$ ) ;
        end
      end
      let  $Sleep' := \{q \in Sleep \mid E \models p \Diamond q\}$ ;
      if  $p$  creates a new block then
        let  $block = last\_block(E)$ ;
        let  $G' = add\_block(block, G)$ ;
      end
      if
         $min\{Ham\_path(G') \text{ which compensate with all happens-before relations of } E\} \leq b$ 
      then
        | Explore( $E.p, Sleep, G', b$ ) ;
        | add  $p$  to Sleep ;
      end
    end
  end

```

Algorithm 12: Lazy-BPOR

Evaluation of Lazy-BPOR

Evaluation on Synthetic Tests:

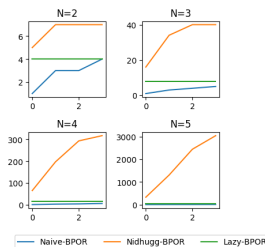


Figure: writer-N-readers bounded by the first estimation algorithm

Technique:	Naive-BPOR			Lazy-BPOR			Nidhugg-BPOR		
Bound:	0	1	2	0	1	2	0	1	2
account.c	1	1	4	6	6	6	6	27	42
lazy.c	1	1	4	6	6	6	6	27	42
micro.c	1	1	10	60	805	4362	6	93	886
lastzero.c	1	2	5	97	97	97	252	2444	10610
lastzeromod.ll	1	1	6	13	13	13	64	290	651
indexer0.c	1	4	1	4	8	8	2	8	14
indexermod.c	1	1	5	120	120	120	120	1320	7920

Table: Traces for the first estimation algorithm for various bound limits

Evaluation of Lazy-BPOR

Evaluation on RCU (DPOR vs Lazy-BPOR):

ver. method	3.0					3.19					4.3					4.7					4.9.8									
	frames	time	error	frames	time	bound	frames	time	error	frames	time	bound	frames	time	error	frames	time	error	frames	time	bound	frames	time	error	frames	time	bound			
-DASSERT 0	240	3.83	F	104	2.79	2	512	17.67	F	75	4.06	2	808	37.31	F	85	8.57	2	338	15.94	F	75	5.28	2	858	40.42	F	85	9.44	2
-DPORCE FAILURE 1	247	3.55	F	141	3.45	3	515	18.21	F	121	8.68	3	861	37.8	F	163	21.73	3	345	15.9	F	123	11.29	3	861	40.52	F	163	23.54	3
-DPORCE FAILURE 2	4	0.34	F	4	0.35	1	3	0.52	F	3	0.52	0	3	0.71	F	3	0.71	0	3	0.86	F	3	0.87	0	3	0.88	F	3	0.9	0
-DPORCE FAILURE 3	2372	32.1	NF	38	1.87	NF	12094	609.75	F	200	54.82	1	15360	796.84	F	233	102.89	1	15360	774.61	F	233	107.1	1	15360	793.79	F	233	113.37	1
-DPORCE FAILURE 4	78	1.43	F	51	1.38	2	61	2.74	F	26	2.1	1	26	1.67	F	14	1.79	1	27	2.48	F	17	2.27	1	27	2.6	F	17	2.34	1
-DPORCE FAILURE 5	12426	185.57	NF	38	3.96	NF	118	4.1	F	52	3.58	3	112	5.12	F	52	5.26	3	112	5.51	F	52	5.66	3	112	5.8	F	52	5.92	3
-DPORCE FAILURE 6	1	0.96	F	1	0.94	0	2	2.93	F	2	2.77	0	2	4.23	F	2	4.33	0	2	8.13	F	2	8.45	0	2	8.62	F	2	8.56	0

Table: Comparison between DPOR and Lazy-BPOR

Evaluation of Lazy-BPOR

Evaluation on RCU (Nidhugg-BPOR vs Lazy-BPOR):

ver	3.0						3.10						4.3						4.7						4.9.6					
method	Nidhugg-BPOR			Lazy-BPOR			Nidhugg-BPOR			Lazy-BPOR			Nidhugg-BPOR			Lazy-BPOR			Nidhugg-BPOR			Lazy-BPOR			Nidhugg-BPOR			Lazy-BPOR		
	time	tracks	bound	time	tracks	bound	time	tracks	bound	time	tracks	bound	time	tracks	bound	time	tracks	bound	time	tracks	bound	time	tracks	bound	time	tracks	bound	time	tracks	bound
-ASSERT 0	2.65	183	3	2.79	184	2	2.96	186	3	4.06	75	2	5.39	128	3	8.59	85	2	5.26	118	3	6.26	75	2	5.91	128	3	6.44	85	2
-BPORC FAILURE 0	3.74	275	4	3.45	141	3	5.02	182	4	0.68	121	3	12.69	300	4	21.73	163	3	0.73	220	4	11.28	123	3	13.93	300	4	23.54	163	3
-BPORC FAILURE 1	0.35	6	1	0.35	4	1	0.54	5	1	0.52	3	0	0.75	5	1	0.75	3	0	0.91	5	1	0.87	3	0	0.95	5	1	0.9	3	0
-BPORC FAILURE 2							6.48	281	2	34.62	200	1	12.11	264	2	103.66	233	1	12.58	254	2	107.1	233	1	37.46	254	2	113.31	233	1
-BPORC FAILURE 3	0.91	47	2	1.38	51	2	1.78	41	2	2.1	34	1	1.89	31	2	1.79	14	1	2.3	24	2	2.27	17	1	2.39	34	2	2.34	17	1
-BPORC FAILURE 4							2.26	80	4	3.58	52	3	3.12	80	4	5.26	52	3	3.47	80	4	5.86	52	3	3.61	60	4	5.02	52	3
-BPORC FAILURE 5	0.65	1	0	0.94	1	0	2.14	2	0	2.77	2	0	4.47	2	0	4.33	2	0	8.7	2	0	8.45	2	0	8.73	2	0	8.56	2	0

Table: Comparison between BPOR and Lazy-BPOR

Conclusion:

- It is possible to explore a preemption-bounded state space without the addition of conservative branches.

Conclusion:

- It is possible to explore a preemption-bounded state space without the addition of conservative branches.
- It provides an upper bound for the number of traces explored in BPOR no matter the bound. In fact the number of traces explored by Lazy-BPOR at worst case equal to the number of traces explored by the unbounded DPOR. This is true since no conservative branches are added.

Conclusion:

- It is possible to explore a preemption-bounded state space without the addition of conservative branches.
- It provides an upper bound for the number of traces explored in BPOR no matter the bound. In fact the number of traces explored by Lazy-BPOR at worst case equal to the number of traces explored by the unbounded DPOR. This is true since no conservative branches are added.
- The most important is that provides a reduction of the preemption-bounded search to a well known graph problem where many heuristics can be applied in order to expedite the calculation of the minimum hamiltonian path.