# Preemption Bounding Techniques for Dynamic Partial Order Reduction

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## Summary

 ${\sf Background}$ 

Algorithms

**Evaluation** 

Discussion

 ${\sf Background}$ 

Concurrent Programming is a form of computing in which several computations are executed during overlapping time periods concurrently, instead of sequentially (one completing before the next starts). Potential problems include:

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Potential problems include:

- Race Conditions
- Deadlocks
- Livelocks
- Resource Starvation

## Concurrency Errors

To be a Concurrency Error or not to be...

```
void *divider(void* arg) {
  int x = 0;
  return 42/x;
}
```

Listing 1: Example of non-concurrency error

```
volatile int x = 1;
void *divider() {
  return 42 / x;
}
void *zero() {
  x = 0;
}
```

Listing 2: Example of concurrency error

• An interleaving represents a scheduling of the concurrent program.

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- In order to find an error of a concurrent program, one must examine every possible interleaving.
- STATE SPACE EXPLOSION!

# Stateless Model Checking and Partial Order Reduction

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- We need to preform Systematic Model Checking.
- Partial Order Reduction aims to reduce the number of interleavings explored by eliminating the exploration of equivalent interleavings.
- Dynamic Partial Order Reduction: record conflicts during runtime and add appropriate rescheduling points.

# An example of Partial Order Reduction (Optimal)

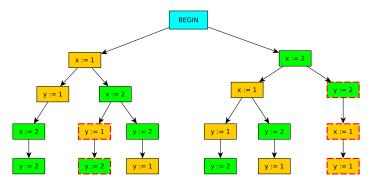


Figure: DPOR tries to avoid red nodes

#### Sufficient Sets

## Definition 1 (Sufficient Sets)

A set of transitions is sufficient in a state s if any relevant state reachable via an enabled transition from s is also reachable from s via at least one of the transitions in the sufficient set. A search can thus explore only the transitions in the sufficient set from s because all relevant states still remain reachable. The set containing all enabled threads is trivially sufficient in s, but smaller sufficient sets enable more state space reduction.

#### General form of DPOR

Algorithm 1: General form of DPOR

```
\begin{split} & \mathsf{Explore}(\emptyset); \\ & \mathbf{Function} \ Explore(E) \\ & | \ \mathbf{let} \ T = Sufficient\_set(final(E)); \\ & \mathbf{for} \ all \ t \in T \ \mathbf{do} \\ & | \ \ \mathsf{Explore}(E.t) \ ; \\ & \mathbf{end} \end{split}
```

## Implementation of DPOR Algorithm

```
\begin{split} & \mathsf{Explore}(\emptyset); \\ & \mathbf{Function} \ Explore(E) \\ & | \ \mathbf{if} \ suitable \ p \ exists \ \mathbf{then} \\ & | \ backtrack(E) := \{p\} \ ; \\ & | \ add \ \mathsf{to} \ \mathsf{previous} \ backtracks \ \mathsf{threads} \ \mathsf{due} \ \mathsf{to} \ \mathsf{dependencies} \ \mathsf{revealed} \ \mathsf{by} \ p; \\ & | \ \mathbf{while} \ \exists p \in backtrack \ \mathbf{do} \\ & | \ Explore(E.p) \ ; \\ & | \ \mathbf{end} \\ & | \ \mathbf{end} \end{split}
```

Algorithm 2: Implementation DPOR Algorithm

#### Sufficient Sets: Persistent Sets

## Definition 2 (Persistent Sets)

Let s be a state, and let  $W\subseteq E(s)$  be a set of execution sequences from s. A set T of transitions is a Persistent Set for W after s if for each prefix w of some sequence in W, which contains no occurrence of a transition in T, we have  $E \vdash t \diamondsuit w$  for each  $t \in T$ .

#### Sufficient Sets: Persistent Sets

#### A simple example:

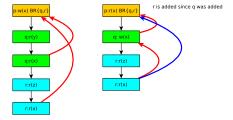


Figure: Construction of Persistent Sets

#### Sufficient Sets: Source Sets

Definition 3 (Initials after an execution sequence  $E.w, I_{[E]}(w)$ )  $p \in I_{[E]}(w)$  if and only if there is a sequence w' such that  $E.w \simeq E.p.w'$ .

Definition 4 (Weak Initials after an execution sequence E.w,  $WI_{[E]}(w)$ )  $p \in WI_{[E]}(w)$  if and only if there are sequences w' and v such that  $E.w.v \simeq E.p.w'$ .

#### Sufficient Sets: Source Sets

## Definition 5 (Source Sets)

Let E be an execution sequence, and let W be a set of sequences, such that E.w is an execution sequence for each  $w \in W$ . A set T of processes is a source set for W after E if for each  $w \in W$  we have  $WI_{[E]}(w) \cap T \neq \emptyset$ .

#### Source Sets

#### An example:

It is needless to add r since q already belongs to source set



Figure: Construction of Source Sets

# Further Optimizations: Sleep Sets

The idea behind Sleep Set Optimization:

• Sleep Sets prevent redundant explorations.

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#### The idea behind Sleep Set Optimization:

- Sleep Sets prevent redundant explorations.
- Assume that the search explores transition t from state s, backtracks t, then explores  $t_0$  from s instead. Unless the search explores a transition that is dependent with t, no states are reachable via  $t_0$  that were not already reachable via t from t0. Thus, t1 "sleeps" unless a dependent transition is explored.

## Sleep Sets

### Sleep sets in action (Using Persistent Sets):

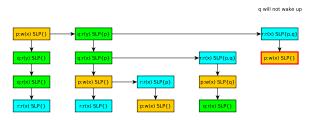


Figure: Example of Sleep Set Optimization

#### Source-DPOR

```
Explore(\langle \rangle, \emptyset);
Function Explore(E,Sleep)
    if \exists p \in (enabled(s_{[E]}) \backslash Sleep) then
         \begin{aligned} backtrack(E) &:= p \ ; \\ \textbf{while} \ \exists p \in (backtrack(E) \backslash Sleep) \ \textbf{do} \end{aligned}
              foreach e \in dom(E) such that e \lesssim_{E.p} next_{[E]}(p) do
               if I_{E'}(u) \cap backtrack(E') = \emptyset then
                       add some q' \in I_{[E']}(u) to backtrack(E');
                   end
              let Sleep' := \{q \in Sleep \mid E \models p \Diamond q\};
              Explore(E.p, Sleep');
              add p to Sleep;
    end
                            Algorithm 3: Source-DPOR Algorithm
```

 For larger programs DPOR often runs longer than developers are willing to wait.

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- Bounded techniques, alleviate state-space explosion by pruning the executions that exceed a bound.
- Many of the concurrency bugs can be tracked even when the bound limit is set to be small.
- Preemption Bounded and Delay Bounded exploration.

## Preemption Bounded Search

# Definition 6 (Preemption bound)

$$\begin{split} P_b(\emptyset) &= 0 \\ P_b(E.t) &= \\ \begin{cases} P_b(E) + 1 & \text{if } t.tid = last(E).tid \text{ and } last(E).tid \in enabled(final(E)) \\ P_b(E) & \text{otherwise} \\ \end{cases} \end{split}$$

## Bounded Dynamic Partial Order Reduction General Form

Given a bound evaluation function  $B_v$  and a bound c:

```
 \begin{array}{ll} \textbf{Result:} \  \, \textbf{Explore the whole statespace} \\ \textbf{Explore}(\emptyset); \\ \textbf{Function } \, \textit{Explore}(E) \\ & \quad T = Sufficient\_set(final(E)) \\ \textbf{for } \, \textit{all } t \in T \textbf{ do} \\ & \quad \mid \textbf{if } B_v(E.t) \leq c \textbf{ then} \\ & \quad \mid \textbf{Explore}(E.t) \\ & \quad \textbf{end} \\ & \quad \textbf{end} \\ \end{array}
```

Algorithm 4: Bounded-DPOR

## Preemption Bounded Persistent Sets

## Definition 7 (Preemption Bounded Persistent Set)

A set  $T\subseteq \mathcal{T}$  of transitions enabled in a state s=final(E) is preemption-bound persistent in s iff for all nonempty sequences a of transitions from s in  $A_G(P_b,c)$  such that  $\forall i\in dom(a), a_i\notin T$  for all  $t\in T$ ,

- 1.  $Pb(E.t) \leq Pb(E.a_1)$
- 2. if  $Pb(E.t) < Pb(E.a_1)$ , then  $t \leftrightarrow last(a)$  and  $t \leftrightarrow next(final(E.a), last(a).tid)$
- 3. if  $Pb(E.t) = Pb(E.a_1)$ , then  $ext(s,t) \leftrightarrow last(a)$  and  $ext(s,t) \leftrightarrow next(final(E.a), last(a).tid)$

### Simplified version:

• Add conservative branches at the beginning of the block.

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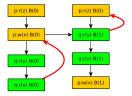


Figure: Example of Blocks and Bound Persistent Sets

# Nidhugg

- Nidhugg is a bug-finding tool which targets bugs caused by concurrency and relaxed memory consistency in concurrent programs. It works on the level of LLVM internal representation, which means that it can be used for programs written in languages such as C or C++.
- Nidhugg relies on Source-Sets.

# The Nidhugg Flow Chart

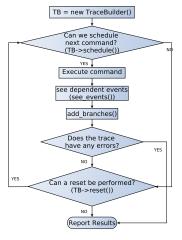


Figure: Nidhugg's Flow Chart

• Implement Preemption Bounded Search (BPOR) for Nidhugg.

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- Explore the potential of Source-Sets for BPOR.

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- Explore the potential of Source-Sets for BPOR.
- Evaluate the performance of various BPOR implementations.
- Explore alternative approaches to BPOR problem.

 ${\bf Algorithms}$ 

#### Naive-BPOR

```
Explore(\langle \rangle, \emptyset, b);
Function Explore(E, Sleep, b)
    if \exists p \in (enabled(s_{[E]}) \backslash Sleep) such that B_v(E.p) \leq b) then
         backtrack(E) := p:
         while \exists p \in (backtrack(E) \backslash Sleep \text{ and } B_v(E.p) \leq b \text{ do}
             foreach e \in dom(E) such that e \lesssim_{E,p} next_{|E|}(p) do
                  let E' = pre(E, e);
                  let u = notdep(e, E).p;
                  if I_{E'}(u) \cap backtrack(E') = \emptyset then
                       add some q' \in I_{[E']}(u) tobacktrack(E') ;
                  end
             end
             let Sleep' := \{q \in Sleep \mid E \models p \diamondsuit q\};
              Explore(E.p, Sleep, b);
             add p to Sleep;
    end
```

Algorithm 5: Naive-BPOR

### Example execution of Naive-BPOR

A Naive-BPOR execution example and the problem with it.

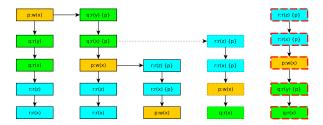


Figure: Naive-BPOR for bound=0

### Nidhugg-DPOR

Requirement for BPOR

```
Explore(\langle \rangle, \emptyset);
Function Explore(E,Sleep)
    if \exists p \in (enabled(s_{[E]}) \backslash Sleep then
        backtrack(E) := \{p\};
         while \exists p \in (backtrack(E) \backslash Sleep) do
             foreach e \in dom(E) such that e \lesssim_{E,p} next_{[E]}(p) do
                 let E' = pre(E, e);
                 let u = notdep(e, E).p;
                 let CI = \{i \in I_{E'}(u) \mid i \to p\};
                 if CI \cap backtrack(E') = \emptyset then
                      if CI \neq \emptyset then
                          add some q' \in CI to backtrack(E');
                      end
                      else
                          add some q'I_{E'}(u) to backtrack(E')
                      end
                 end
             end
             let Sleep' := \{q \in Sleep \mid E \models p \Diamond q\};
             Explore(E.p, Sleep);
             add p to Sleep;
    end
```

Algorithm 6: Nidhugg-DPOR

## Correctness of Nidhugg-DPOR

Case 1: At least one process contains a write command. We know that the two processes will be inverted at some point. Since Nidhugg-DPOR ignores weak initials it will branch both processes. In Source-DPOR only one of the two processes should be branched since they share the same initials. However, in Nidhugg-DPOR this is not true since the  ${\it CI}$  set does not contain steps from the other process.

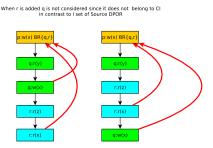


Figure: Construction of Persistent Sets in Nidhugg when there is a write process

## Correctness of Nidhugg-DPOR

Case 2: Both processes are read operations. Since we do not calculate I but CI the first read operation will not be considered as it does not happen before the second read operation and as result both processes will be added to backtrack. We notice that by calculating the CI set when the race between p and r is detected q process will be ignored and, thus, r will be added as a branch.

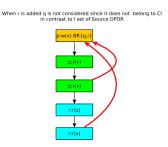


Figure: Construction of Persistent Sets in Nidhugg when both are read processes

# Nidhugg-BPOR

```
Explore(\langle \rangle, \emptyset, b);
Function Explore(E, Sleep, b)
    if \exists p \in ((enabled(s_{[E]}) \backslash Sleep) \text{ and } B_v(E.p) <= b \text{ then }
         backtrack(E) := p;
        while \exists p \in (backtrack(E) \backslash Sleep \text{ and } B_v(E.p) <= b \text{ do}
             foreach e \in dom(E) such that e \lesssim_{E,p} next_{[E]}(p) do
                  add non-conservative branches according to Persistent Sets;
                 add conservative branches according to Persistent Sets at the
                   beginning of blocks;
             end
             let Sleep' := \{ q \in Sleep \mid E \models p \Diamond q \} ;
             Explore(E.p, Sleep);
             if p is not conservative then
                  add p to Sleep;
             end
    end
```

Algorithm 7: Nidhugg-BPOR

# Source-BPOR: The main question

Can we use source sets instead of Persistent Sets in order to implement BPOR?

## Source-BPOR: First approach

We should use Source Sets for both conservative and non-conservative branches.

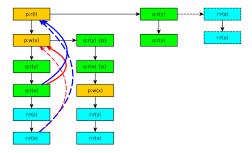


Figure: Following source sets for conservative branches

# Source-BPOR: A Correct Approach

We should use Source Sets for non-conservative branches and Persistent Sets for conservative branches.

#### Source-BPOR

```
Explore(\langle \rangle, \emptyset, b);
Function Explore(E, Sleep, b)
    if \exists p \in ((enabled(s_{[E]}) \backslash Sleep) \text{ and } B_v(E.p) <= b \text{ then}
         backtrack(E) := p;
        while \exists p \in (backtrack(E) \backslash Sleep \text{ and } B_v(E.p) <= b \text{ do}
             foreach e \in dom(E) such that e \lesssim_{E,p} next_{[E]}(p) do
                  add non-conservative backtracks according to Source Sets;
                  add conservative backtracks according to Persistent Sets at the
                   beginning of blocks;
             end
             let Sleep' := \{ q \in Sleep \mid E \models p \Diamond q \} ;
             Explore(E.p, Sleep);
             if p is not conservative then
                  add p to Sleep;
             end
    end
```

Algorithm 8: Source-BPOR

# Nidhugg-BPOR vs Source-BPOR

#### Similarities:

Same structure.

#### Differences:

 Source-BPOR relies on Source Sets for the addition of non-conservative branches while Nidhugg-BPOR relies on Persistent Sets.

# Challenges with Conservative Branches

The usage of conservative branches leads to explosion of the state space:

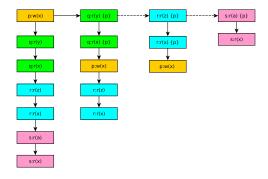


Figure: writer-3-readers explosion

# Challenges with Conservative Branches

### Sleep Sets are no longer that useful:

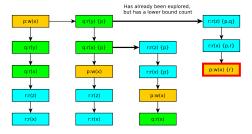


Figure: Sleep set contradiction

## Concluding Remarks

The Performance - Soundness Tradeoff: Some algorithms are faster but compromise the soundness of the exploration while others are slower but sound as well.

**Evaluation** 

# Nidhugg-DPOR Evaluation

### Evaluation of Nidhugg-DPOR on Synthetic Tests

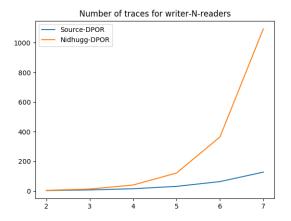


Figure: writer-N-readers

# Nidhugg-DPOR Evaluation

Test case	Traces for Source-DPOR	Traces for Classic-DPOR
account.c	6	7
lazy.c	6	7
micro.c	52495	53084
lastzero.c	97	97
lastzeromod.ll	13	17
indexer0.c	8	8
indexermod.c	120	226

Table: Source-DPOR vs Nidhugg-DPOR for Synthetic tests

# Nidhugg-BPOR Evaluation

### Evaluation of Nidhugg-BPOR on Synthetic Tests

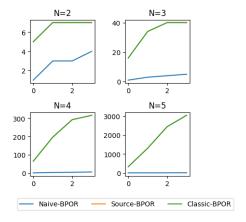


Figure: writer-N-readers bounded

# Nidhugg-BPOR Evaluation

## Evaluation of Nidhugg-BPOR on Synthetic Tests

Technique:	Na	ive-E	BPOR	Ni	dhugg-B	POR	Source-BPOR					
Bound:	0	1	2	0	1	1 2		1	2			
account.c	1	1	4	6	27	42	6	27	42			
lazy.c	1	1	4	6	27	42	6	27	42			
micro.c	1	1	10	6	93	886	6	93	886			
lastzero.c	1	2	5	252	2444	10614	252	2444	10614			
lastzeromod.ll	1	1	6	64	290	651	64	290	651			
indexer0.c	1	4	1	2	8	14	2	8	14			
indexermod.c	1	1	5	120	1320	7920	120	1320	7920			

Table: Traces for various bound limits

#### Evalution of BPOR on RCU

Read-Copy-Update (RCU): Read-copy update (RCU) is a synchronization mechanism that was added to the Linux kernel in October of 2002. Let's start with a small bound...

ver:	3.0									19		4.9.6						
method:	Naive-BPOR Classic-BPOR			OR	Naive-BPOR Classic-BPO					OR	Na	ive-BPC	R	Classic-BPOR				
	traces	time	error	traces	time	error	traces	time	error	traces	time	error	traces	time	error	traces	time	error
-	3	0.2	NF	44	0.72	NF	2	0.32	NF	28	0.76	NF	2	0.61	NF	24	1.21	NF
-DFORCE_FAILURE_1	3	0.2	NF	44	0.72	NF	2	0.32	NF	28	0.76	NF	2	0.6	NF	24	1.21	NF
-DFORCE_FAILURE_3	3	0.2	NF	44	0.72	NF	2	0.32	NF	33	1.06	NF	2	0.61	NF	41	2.11	NF
-DFORCE_FAILURE_5	3	0.2	NF	44	0.71	NF	2	0.31	NF	18	0.55	NF	2	0.6	NF	16	0.93	NF
-DLIVENESS_CHECK_1	3	0.2	NF	44	0.72	NF	2	0.32	NF	28	0.74	NF	2	0.61	NF	24	1.19	NF
-DLIVENESS_CHECK_2	3	0.2	NF	52	0.84	NF	2	0.32	NF	28	0.73	NF	2	0.6	NF	24	1.2	NF
-DLIVENESS_CHECK_3	3	0.2	NF	44	0.71	NF	2	0.31	NF	28	0.75	NF	2	0.6	NF	24	1.19	NF

Table: RCU results for bound b = 1

## Evalution of BPOR on RCU

#### Let's increase the bound...

ver:	3.0								3	.19			4.9.6						
method:	Naive-BPOR		Classic-BPOR			Naive-BPOR			Classic-BPOR			Naive-BPOR			Classic-BPOR		₹		
	traces	time	error	traces	time	error	traces	time	error	traces	time	error	traces	time	error	traces	time	error	
-	50	1.18	NF	5634	88.78	NF	10	0.49	NF	2083	60.48	NF	10	0.89	NF	2469	122.71	NF	
-DFORCE_FAILURE_1	50	1.06	NF	275	4.2	F	10	0.49	NF	182	5.51	F	10	0.89	NF	300	15.42	F	
-DFORCE_FAILURE_3	50	1.05	NF	1627	23.09	NF	15	0.72	NF	100000	0.0	NF	15	1.2	NF	100000	0.0	NF	
-DFORCE_FAILURE_5	49	1.05	NF	4155	59.47	NF	9	0.45	NF	60	2.34	F	9	0.81	NF	60	3.92	F	
-DLIVENESS_CHECK_1	48	1.04	NF	1493	21.19	NF	10	0.5	NF	517	10.66	NF	10	0.88	NF	404	13.58	NF	
-DLIVENESS_CHECK_2	61	1.28	NF	2105	30.5	NF	10	0.5	NF	517	10.61	NF	10	0.88	NF	582	20.28	NF	
-DLIVENESS_CHECK_3	49	1.04	NF	1788	24.98	NF	10	0.5	NF	655	14.04	NF	10	0.88	NF	506	17.32	NF	

Table: RCU results for bound  $b=4\,$ 

### Evalution of BPOR on RCU

### What did we achieve?

ver:	3.0						3.19							4.9.6						
method:	Source-DPOR		Classic-BPOR			Source-DPOR			Classic-BPOR			Sc	urce-DPC	)R	Classic-BPOR					
	traces	time	bound	traces	time	bound	traces	time	bound	traces	time	bound	traces	time	bound	traces	time	bound		
-DFORCE_FAILURE_1	247	3.81	F	275	4.2	4	515	16.88	F	182	5.51	4	861	45.69	F	300	15.42	4		
-DFORCE_FAILURE_3	2372	33.42	NF				17094	626.4	F	201	7.03	2	15349	883.98	F	258	14.24	2		
-DFORCE_FAILURE_5	12426	178.8	NF				118	3.99	F	60	2.34	4	112	6.34	F	60	3.92	4		

Table: Comparison between DPOR and BPOR

# Equivalence of Source-BPOR with Nidhugg-BPOR

#### Equivalence Case1:

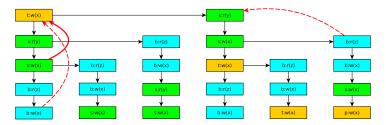


Figure: Source-BPOR and Nidhugg-BPOR equivalence Case 1

# Equivalence of Source-BPOR with Nidhugg-BPOR

### Equivalence Case 2:

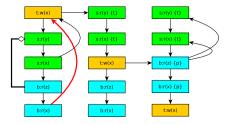


Figure: Source-BPOR and Nidhugg-BPOR equivalence Case 2

Discussion

#### Motivation

Some preemption-switches can be easily avoided. For example:

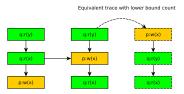


Figure: An example of avoidable preemption-switch

# Alternating the General Form of BPOR

### What if calculate something more than the preemption-bound?

```
Result: Explore the whole state space within the bound
Explore(∅);
Function Explore(S)
   T = Sufficient set(final(S)) for all t \in T do
      if min\{B_v([S.t])\} \le c then
       Explore(S.t)
       Algorithm 9: General form of the BPOR without branch addition
```

# Applying the Graph Construction Algorithm

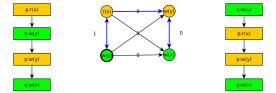


Figure: Graph example

# Introducing Lazy-BPOR

```
let G =: \emptyset:
Explore(\langle \rangle, \emptyset, G, b);
Function Explore(E,Sleep,G,b)
    if \exists p \in (enabled(s_{[E]}) \backslash Sleep) such that B_v(E.p) \leq b then
        backtrack(E) := p:
        while \exists p \in (backtrack(E) \backslash Sleep do
             foreach e \in dom(E) such that e \lesssim_{E,p} next_{|E|}(p) do
                 let E' = pre(E, e);
                 let u = notdep(e, E).p;
                 if I_{E'}(u) \cap backtrack(E') = \emptyset then
                     add some q' \in I_{[E']}(u) tobacktrack(E');
                 end
             end
             \textbf{let }Sleep':=\{q\in Sleep\mid E\models p\Diamond q\};
             if p creates a new block then
                 let block = last \ block(E);
                 let G' = \text{add block}(block, G);
             end
             if
              min\{Ham\ path(G')\ which\ compensate\ with\ all\ happens-before\ relations\ of\ E\} \le
              b then
                 Explore(E.p, Sleep, G', b);
                 add p to Sleep;
    end
```

Algorithm 10: Lazy-BPOR

### Evaluation on Synthetic Tests:

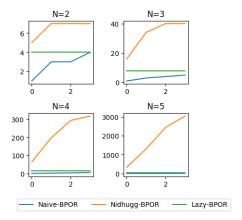


Figure: writer-N-readers bounded by the first estimation algorithm

### Evaluation on Synthetic Tests:

Technique:	Na	ive-E	3POR	La	azy-BP	OR	Nidhugg-BPOR						
Bound:	0	1	2	0	1	2	0	1	2				
account.c	1	1	4	6	6	6	6	27	42				
lazy.c	1	1	4	6	6	6	6	27	42				
micro.c	1	1	10	60	805	4362	6	93	886				
lastzero.c	1	2	5	97	97	97	252	2444	10610				
lastzeromod.ll	1	1	6	13	13	13	64	290	651				
indexer0.c	1	4	1	4	8	8	2	8	14				
indexermod.c	1	1	5	120	120	120	120	1320	7920				

Table: Traces for the first estimation algorithm for various bound limits

### Evaluation on RCU (Nidhugg-BPOR vs Lazy-BPOR):

ver.			3	.0				3.19				43						4.7						4.9.6						
method	N	ichugg-Bl	POR		Lazy-BPI	OR	N N	ichugg-Bl	POR		Lazy-BPC	R	No.	dhugg-Bf	OR	_	.azy-BPO	R	Ni	thugg-Bi	POR		azy-BP(	98	Ni	dhugg-Bi	*OR	_	azy-BPC	8
	time	traces	bound	time	traces	bound	time	traces	bound	time	traces	bound	time	traces	bound	time	traces	bound	time	traces	bound	time	traces	bound	time	traces	bound	time	traces	bound
-ASSERT_0	2.65	183	3	2.79	104	2	2.96	106	3	4.06	73	2	5.39	128	3	8.57	85	2	5.28	118	3	6.28	75	2	5.91	128	3	9.44	85	2
-DFORCE_FAILURE_0	3.74	275	4	3.45	141	3	5.02	182	4	8.68	121	3	12.69	300	4	21.73	163	3	9.73	220	4	11.28	123	3	13.93	300	4	23.54	163	3
-DFORCE FAILURE 1	0.35	- 6	1	0.35	4	1	0.54	- 5	1	0.52	3	0	0.75	5	1	0.71	3	0	0.91	- 5	1	0.87	3	0	0.95	- 5	1	0.9	3	0
-DFORCE FAILURE 2		-	NF		-		6.49	201	2	54.62	200	1	12.11	258	2	103.89	233	1	12.59	258	2	107.1	233	1	12.84	258	2	111.37	233	1
	0.91	47	2	1.38	51	2	1.78	41	2	2.1	24	1	1.89	21	2	1.79	14	1	2.3	24	2	2.27	17	1	2.39	24	2	2.34	17	1
-DFORCE_FAILURE_4			NF				2.26	60	4	3.58	52	3	3.12	60	4	5.26	52	3	3.47	60	4	5.66	52	3	3.61	60	4	5.92	52	3
-DFORCE FAILURE 5	0.95	1	0	0.94	- :	0	2.74	2	0	2.77	2	0	4.47	2	0	4.33	2	0	8.7	2	0	8.45	2	0	8.73	2	0	8.56	2	0

Table: Comparison between BPOR and Lazy-BPOR

The Big Picture

### Evaluation on RCU (Nidhugg-BPOR vs Lazy-BPOR):

ver.			4.	.7			4.9.6								
method	Nic	dhugg-BP	OR	L	.azy-BPO	R	Nic	dhugg-BF	OR	Lazy-BPOR					
	time	traces	bound	time	traces	bound	time	traces	bound	time	traces	bound			
-ASSERT_0	5.28	118	3	6.28	75	2	5.91	128	3	9.44	85	2			
-DFORCE_FAILURE_0	9.73	220	4	11.28	123	3	13.93	300	4	23.54	163	3			
-DFORCE_FAILURE_1	0.91	5	1	0.87	3	0	0.95	5	1	0.9	3	0			
-DFORCE_FAILURE_2	12.59	258	2	107.1	233	1	12.84	258	2	111.37	233	1			
-DFORCE_FAILURE_3	2.3	24	2	2.27	17	1	2.39	24	2	2.34	17	1			
-DFORCE_FAILURE_4	3.47	60	4	5.66	52	3	3.61	60	4	5.92	52	3			
-DFORCE_FAILURE_5	8.7	2	0	8.45	2	0	8.73	2	0	8.56	2	0			

Table: Comparison between BPOR and Lazy-BPOR

#### Conclusion:

 It is possible to explore a preemption-bounded state space without the addition of conservative branches.

#### Conclusion:

- It is possible to explore a preemption-bounded state space without the addition of conservative branches.
- It provides an upper bound for the number of traces explored in BPOR no matter the bound. In fact the number of traces explored by Lazy-BPOR at worst case equal to the number of traces explored by the unbounded DPOR. This is true since no conservative branches are added.

#### Conclusion:

- It is possible to explore a preemption-bounded state space without the addition of conservative branches.
- It provides an upper bound for the number of traces explored in BPOR no matter the bound. In fact the number of traces explored by Lazy-BPOR at worst case equal to the number of traces explored by the unbounded DPOR. This is true since no conservative branches are added.
- The most important is that it provides a reduction of the preemption-bounded search to a well known graph problem where many heuristics can be applied in order to expedite the calculation of the minimum hamiltonian path.

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Thank you for your attention!

# Nidhugg-BPOR (Detailed)

Explore( $\langle \rangle, \emptyset, b$ );

```
Function Explore(E,Sleep,b)
    if \exists p \in ((enabled(s_{|E|}) \backslash Sleep) \text{ and } B_v(E.p) <= b \text{ then}
        backtrack(E) := p;
        while \exists p \in (backtrack(E) \backslash Sleep \text{ and } B_v(E.p) <= b \text{ do}
            foreach e \in dom(E) such that e \lesssim_{E,p} next_{[E]}(p) do
                 let E' = pre(E, e);
                 let u = notdep(e, E).p;
                 let CI = \{i \in I_{E'}(u) \mid i \rightarrow p\};
                 if CI \cap backtrack(E') = \emptyset then
                     if CI \neq \emptyset then
                         add some q' \in CI to backtrack(E');
                     end
                     else
                         add some q' \in I_{[E']}(u) to backtrack(E');
                     end
                 end
                 let E'' = pre \quad block(e, E);
                 let u = notdep(e, E).p;
                 let CI = \{i \in I_{E''}(u) \mid i \rightarrow p\};
                 if CI \cap backtrack(E') = \emptyset then
                     if CI \neq \emptyset then
                         add some q' \in CI to backtrack(E');
                     end
                     else
                         add some c(q') \in I_{[E'']}(u) to backtrack(E'') ;
                     end
                 end
            end
            let Sleep' := \{q \in Sleep \mid E \models p \Diamond q\};
             Explore(E.p, Sleep);
            if p is not conservative then
                 add p to Sleep;
            end
                                                                           4□ > 4問 > 4 = > 4 = > = 900
```

# Source-BPOR (Detailed)

```
Explore(\langle \rangle, \emptyset, b);
Function Explore(E,Sleep,b)
    if \exists p \in ((enabled(s_{[E]}) \backslash Sleep) \text{ and } B_v(E.p) <= b \text{ then}
        backtrack(E) := p;
        while \exists p \in (backtrack(E) \backslash Sleep \text{ and } B_n(E.p) <= b \text{ do}
             foreach e \in dom(E) such that e \lesssim_{E,p} next_{[E]}(p) do
                 let E' = pre(E, e);
                 let u = notdep(e, E).p;
                 if I_{E'}(u) \cap backtrack(E') = \emptyset then
                      add some q' \in I_{[E']}(u) to backtrack(E');
                  end
                 let E'' = pre block(e, E);
                 let u = notdep(e, E).p;
                 let CI = \{i \in I_{E''}(u) \mid i \rightarrow p\};
                 if CI \cap backtrack(E') = \emptyset then
                      if CI \neq \emptyset then
                          add some q' \in CI to backtrack(E');
                      end
                      else
                          add some c(q') \in I_{[E'']}(u) to backtrack(E'');
                      end
                 end
             end
             let Sleep' := \{q \in Sleep \mid E \models p \Diamond q\};
             Explore(E.p, Sleep);
             if p is not conservative then
                 add p to Sleep;
             end
        end
```

#### Classic-BPOR

```
Function Explore(E)
   let s := last(E):
   for all process p do
       for all process q \neq p do
           if \exists i = max(\{i \in dom(E) \mid E_i \text{ is dependent and may be co-enabled})
             with next(s, p) and E_i.tid = q} then
               if p \in enabled(pre(E, i))) then
                   add p to backtrack(pre(E, i));
                else
                   add enabled(pre(E, i)) to backtrack(pre(E, i));
                end
               if j = max(\{j \in dom(E) \mid j = 0 \text{ or } S_{i-1}.tid \neq S_j.tid \text{ and } j < i\})
                 then
                   if p \in enabled(pre(E, i))) then
                       add p to backtrack(pre(E, i));
                    else
                       add enabled(pre(E, i)) to backtrack(pre(E, i));
                    end
           end
       end
   end
   if p \in enabled(s) then
       add p to backtrack(s);
   end
   else
       add any u \in enabled(s) to backtrack(s);
    end
   let visited = \emptyset;
   while \exists u \in (enabled(s) \cap backtrack(s) \backslash visited) do
       add u to visited:
       if (B_v(S.next(s, u)) \le c) then
           Explore(S.next(s, u));
   end
                               Algorithm 13: BPOR
```