

## yli130\_Assignment 2

1. (a)

$X_i$ : the number of the full-time workers ( $i=1,2,3$ )

$Y_i$ : the number of the part-time workers( $i=1,2,3,4$ )

Objective Function:

$$\text{Pay}(\min) = 112*X_1 + 112*X_2 + 112*X_3 + 48*Y_1 + 48*Y_2 + 48*Y_3 + 48*Y_4$$

S.T:

$$X_1 + Y_1 \geq 4$$

$$X_1 + X_2 + Y_2 \geq 8$$

$$X_2 + X_3 + Y_3 \geq 10$$

$$X_3 + Y_4 \geq 6$$

$$X_1 \geq Y_1$$

$$X_1 + X_2 \geq Y_2$$

$$X_2 + X_3 \geq Y_3$$

$$X_3 \geq Y_4$$

Solution:

$$2X_1 + 2X_2 + 2X_3 + Y_1 + Y_2 + Y_3 + Y_4 \geq 28$$

$$2X_1 + 2X_2 + 2X_3 - Y_1 - Y_2 - Y_3 - Y_4 \geq 0$$

$$4X_1 + 4X_2 + 4X_3 \geq 28$$

$$X_1 + X_2 + X_3 \geq 7 \quad \text{means at least need 7 full time workers}$$

$$\text{And } Y_1 + Y_2 + Y_3 + Y_4 \geq 14 \quad \text{at least 14 part time workers}$$

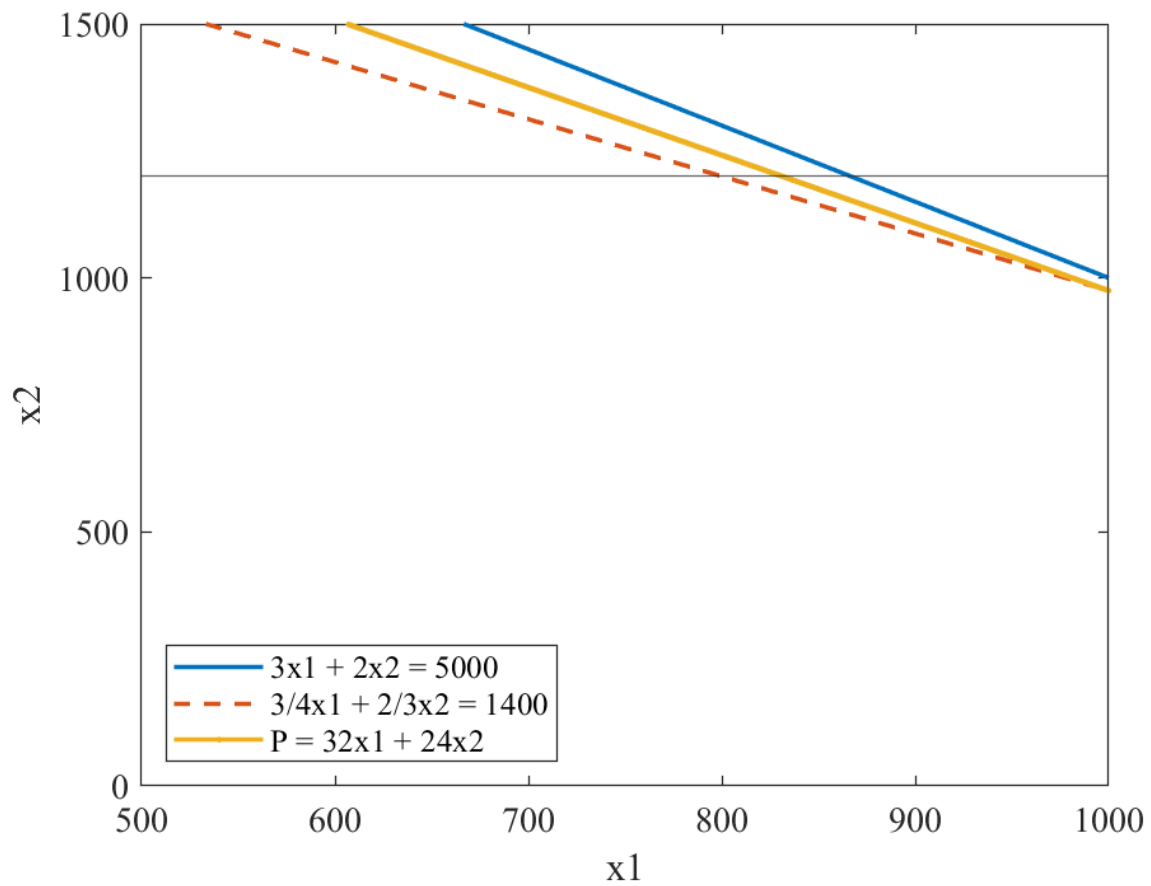
$$\text{Pay}(\min) = 112*7 + 48*14 = 784 + 672 = 1456$$

(b)

Full time worker lunch for 1 hour

$$\text{Pay}(\min) = 98*7 + 48*14 = 686 + 672 = 1358$$

2.



I draw this picture with Matlab.

And found the maximum profit is the right border point,  $X_1 = 1000$ ,  $X_2 = 975$ .

So, the number of Collegiates production per week is 1000, for Minis is 975.

3.

(a)

There are 9 decision variables

$L_i$ : the number of large sizes produced by each plant,  $i=1,2,3$

$M_i$ : the number of medium sizes produced by each plant,  $i=1,2,3$

$S_i$ : the number of small sizes produced by each plant,  $i=1,2,3$

(b)

Objective Function:

$$P(\text{profit}) = 420*L1 + 420*L2 + 420*L3 + 360*M1 + 360*M2 + 360*M3 + 300*S1 + 300*S2 + 300*S3$$

S.T.:

$$L1 + M1 + S1 \leq 750$$

$$L2 + M2 + S2 \leq 900$$

$$L3 + M3 + S3 \leq 450$$

$$20L1 + 15M1 + 12S1 \leq 13000$$

$$20L2 + 15M2 + 12S2 \leq 12000$$

$$20L3 + 15M3 + 12S3 \leq 5000$$

$$L1 + L1 + L3 \leq 900$$

$$M1 + M2 + M3 \leq 1200$$

$$S1 + S2 + S3 \leq 750$$

$$L_i, M_i, S_i \geq 0$$

According to RMD, the maximum profit is 707940, and each plant & sizes production is shown in the other RMD knitted pdf file.