

title: "Regression Model Assignment"  
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# Motor Trend Analysis

## Summary

The dataset is a extract from 1974 Motor Trend US magazine compromises the fuel consupmption and 10 aspects of automobile design and performance.

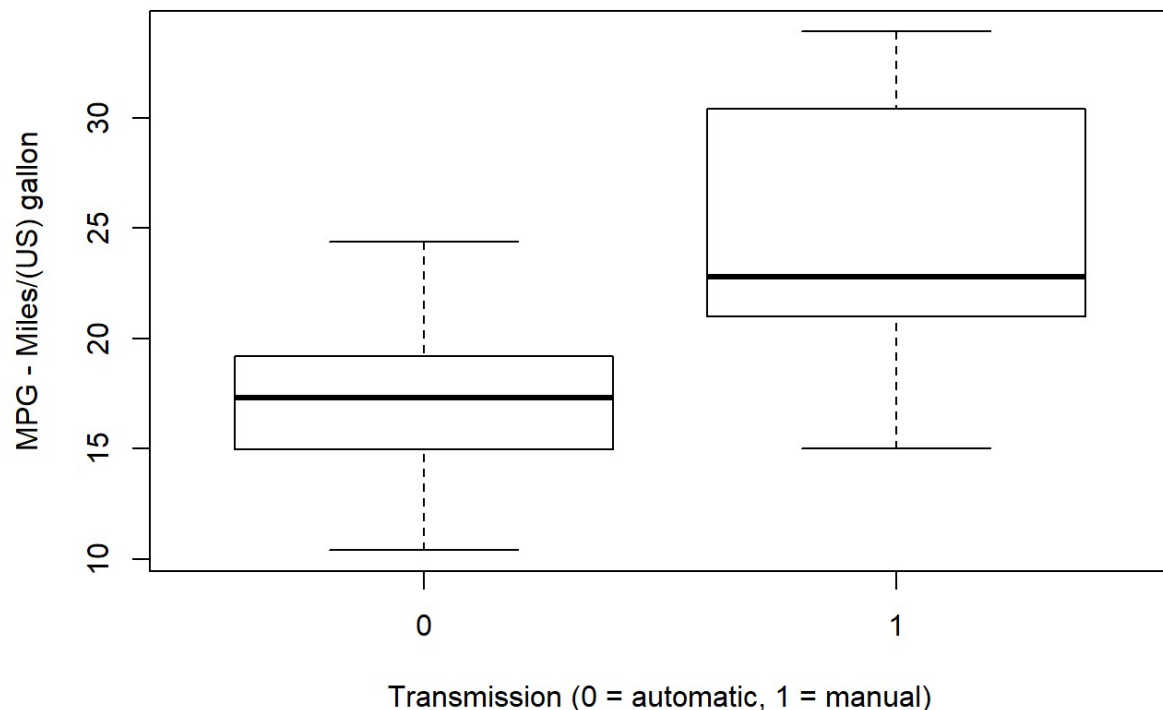
```
head(mtcars)
```

##	mpg	cyl	disp	hp	drat	wt	qsec	vs	am	gear	carb
## Mazda RX4	21.0	6	160	110	3.90	2.620	16.46	0	1	4	4
## Mazda RX4 Wag	21.0	6	160	110	3.90	2.875	17.02	0	1	4	4
## Datsun 710	22.8	4	108	93	3.85	2.320	18.61	1	1	4	1
## Hornet 4 Drive	21.4	6	258	110	3.08	3.215	19.44	1	0	3	1
## Hornet Sportabout	18.7	8	360	175	3.15	3.440	17.02	0	0	3	2
## Valiant	18.1	6	225	105	2.76	3.460	20.22	1	0	3	1

```
str(mtcars)
```

```
## 'data.frame': 32 obs. of 11 variables:
## $ mpg : num 21 21 22.8 21.4 18.7 18.1 14.3 24.4 22.8 19.2 ...
## $ cyl : num 6 6 4 6 8 6 8 4 4 6 ...
## $ disp: num 160 160 108 258 360 ...
## $ hp : num 110 110 93 110 175 105 245 62 95 123 ...
## $ drat: num 3.9 3.9 3.85 3.08 3.15 2.76 3.21 3.69 3.92 3.92 ...
## $ wt : num 2.62 2.88 2.32 3.21 3.44 ...
## $ qsec: num 16.5 17 18.6 19.4 17 ...
## $ vs : num 0 0 1 1 0 1 0 1 1 1 ...
## $ am : num 1 1 1 0 0 0 0 0 0 0 ...
## $ gear: num 4 4 4 3 3 3 3 4 4 4 ...
## $ carb: num 4 4 1 1 2 1 4 2 2 4 ...
```

```
mtcars$am <- factor(mtcars$am)
boxplot(mpg ~ am, data = mtcars,
        xlab="Transmission (0 = automatic, 1 = manual)",
        ylab="MPG - Miles/(US) gallon")
```



According on the boxplot chart, it's quite obvious that the mean and distribution of the Miles per Gallon (MPG) in manual transmission is higher than automatic transmission.

## Simple Linear Regression Model

MPG (mpg) vs Transmission (am)

```
fit <- lm(mpg ~ am , mtcars)
summary(fit)$coeff
```

```
##           Estimate Std. Error  t value    Pr(>|t|)
## (Intercept) 17.147368   1.124603 15.247492 1.133983e-15
## am1         7.244939   1.764422  4.106127 2.850207e-04
```

```
summary(fit)$adj.r.squared
```

```
## [1] 0.3384589
```

The p-value 0.000285 is lower than 5% confidence level. We can reject the null hypothesis that  $\beta_1 = 0$ . In other words, there is significant relationship between MPG and transmission type in the linear regression model with confidence level  $> 95\%$ . However, the Adjusted R-squared value is quite low that only 33.85% of regression variance can be explained by this model. It may lead to higher chance of under fitting with this model. In other words, there might need to be more variables that we take into consideration.

# Multivariate Linear Regression Model

## Covariates Selection

```
all_fit <- lm(mpg ~ ., data = mtcars)
all_fit$coefficients
```

```
## (Intercept)      cyl      disp      hp      drat      wt
## 12.30337416 -0.11144048  0.01333524 -0.02148212  0.78711097 -3.71530393
##          qsec      vs      am1      gear      carb
##   0.82104075  0.31776281  2.52022689  0.65541302 -0.19941925
```

```
summary(all_fit)$adj.r.squared
```

```
## [1] 0.8066423
```

Weight (wt) and Gross Horsepower (hp) are selected because they are the other 2 variables with lowest p-values and standard errors.

```
wt_fit <- lm(mpg ~ wt, data = mtcars)
wt_fit$coefficients
```

```
## (Intercept)      wt
##   37.285126  -5.344472
```

```
summary(wt_fit)$adj.r.squared
```

```
## [1] 0.7445939
```

Obviously, weight (wt) variable has near to zero empirical p-values and very high Adjusted R-squared value at 74.46%.

```
hp_fit <- lm(mpg ~ hp, data = mtcars)
hp_fit$coefficients
```

```
## (Intercept)      hp
## 30.09886054 -0.06822828
```

```
summary(hp_fit)$adj.r.squared
```

```
## [1] 0.5891853
```

Obviously, horsepower (hp) variable has near to zero empirical p-values and high Adjusted R-squared value at 58.92%. So, weight (wt) and horsepower (hp) are best covariates to be associated into the regression model.

## MPG (mpg) vs Transmission (am) + Weight (wt) + Horsepower (hp)

```
best_fit <- lm(mpg ~ am + wt + hp, data = mtcars)
best_fit$coefficients
```

```
## (Intercept)          am1           wt           hp
## 34.00287512   2.08371013  -2.87857541  -0.03747873
```

```
summary(best_fit)$adj.r.squared
```

```
## [1] 0.8227357
```

In this Multivariate Regression Model, the p-value is near to zero, hence null hypothesis is rejected. This time, the R-squared value (82.27%) is much higher than the previous Simple Regression Model.

```
par(mfrow = c(2,2))
plot(best_fit)
```

