Application of Millepede algorithm to Time and Position Calibration of NeuLAND

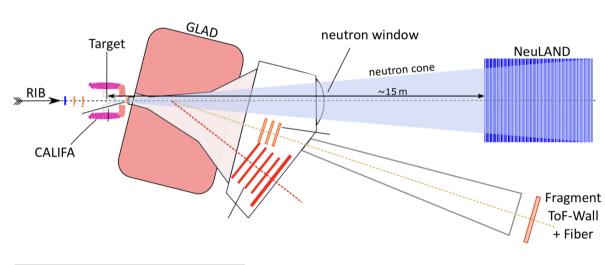
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Institute for Nuclear Physics, University of Cologne

HK 51.3 DPG-Frühjahrstagung Gießen 2024

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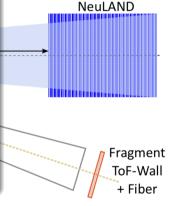






Geometry:

- 26 planes
- $\bullet \ 250 \times 250 \, \mathrm{cm}^2$
- 50 scintillators each plane
- 100 PMTs each plane



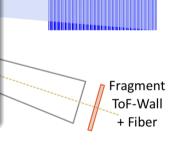


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Measurements:

- interaction position
- interaction time
- energy deposition



NeuLAND

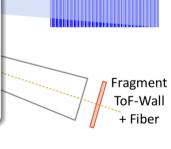


Geometry:

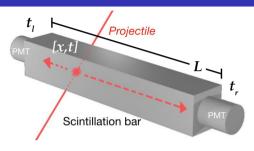
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NeuLAND



Symbols:

x: position of the interaction

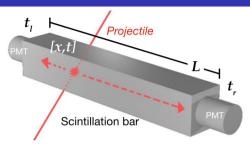
t: time of the interaction

 $L: \mathsf{length} \ \mathsf{of} \ \mathsf{the} \ \mathsf{scintillator}$

 t_l : time of the left PMT signal

 t_r : time of the right PMT signal

 C_e : effective speed of light



Time relation:

$$t = \frac{t_r + t_l}{2} - \frac{L}{2 \cdot \underline{C_e}}$$

Position relation:

$$x = \frac{C_e}{2} \left(t_r - t_l \right)$$

Symbols:

x: position of the interaction

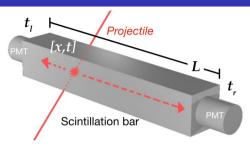
t: time of the interaction

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Symbols:

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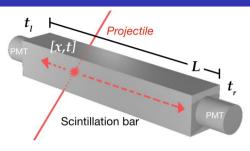
$$t = rac{t_r + t_l}{2} - rac{L}{2 \cdot extstyle C_e} + extstyle t_{ extstyle sync}$$

Position relation:

$$x = \frac{C_e}{2} \left(t_r - t_l \right)$$

Additional calibration parameters:

t_{sync}: time synchronization among scintillators



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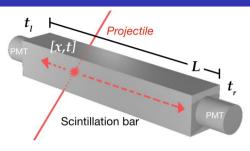
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Position relation:

$$x = rac{C_e}{2} \left(t_r - t_l + t_{\mathsf{offset}}
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Additional calibration parameters:

- t_{sync}: time synchronization among scintillators
- ullet $t_{
 m offset}$: time offset between adjacent PMTs



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Additional calibration parameters:

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- t_{offset} : time offset between adjacent PMTs

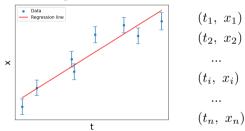
Total number of calibration parameters: 3900

Calibration principle

Calibration relation

$$x = C_1 \cdot t + C_2$$

Data fitting:



Minimize

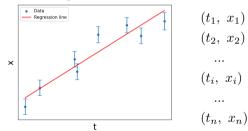
$$\mathsf{residual} = \sum_i \frac{(x_i - x(t_i, C_1, C_2))}{2 * \sigma_i^2}$$

Calibration principle

Calibration relation

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Data fitting:



Minimize

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Calibration with muon tracks

$$t = (t_r + t_l)/2 - L/(2 \cdot C_e) + t_{\text{sync}}$$
 (1)

$$x = \frac{C_e}{t_l} \cdot \left(t_r - t_l + \frac{t_{\text{offset}}}{t_l}\right) / 2 \tag{2}$$

$$x_{\mu} = a_x^i \cdot z_{\mu} + b_x^i \tag{3}$$

$$y_{\mu} = a_y^i \cdot z_{\mu} + b_y^i \tag{4}$$

$$t_{\mu} = a_t^i \cdot z_{\mu} \tag{5}$$

Calibration parameters for the *i*th event:

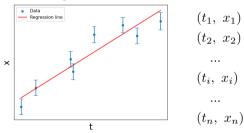
$$C_e, t_{\mathsf{sync}}, t_{\mathsf{offset}}, a_x^i, a_y^i, a_t^i, b_x^i, b_y^i$$

Calibration principle

Calibration relation

$$x = C_1 \cdot t + C_2$$

Data fitting:



Minimize

$$\mathsf{residual} = \sum_{i} \frac{(x_i - x(t_i, C_1, C_2))}{2 * \sigma_i^2}$$

Calibration with muon tracks

$$t = (t_r + t_l)/2 - L/(2 \cdot \underline{C_e}) + \underline{t_{\text{sync}}} \quad (1)$$

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$$x_{\mu} = a_x^i \cdot z_{\mu} + b_x^i \tag{3}$$

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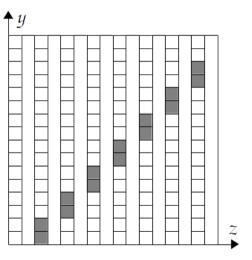
Calibration parameters for the *i*th event:

$$C_e, t_{\sf sync}, t_{\sf offset}, a_x^i, a_y^i, a_t^i, b_x^i, b_y^i$$

With 10'000 events, the total number of

calibration parameters: 53'900!

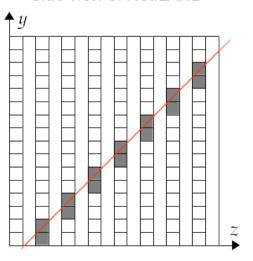
Side view of NeuLAND



Procedures

Obtain the positions of bars with signals

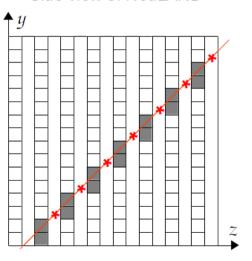
Side view of NeuLAND



Procedures

- Obtain the positions of bars with signals
- Reconstruct the muon track from the bar positions

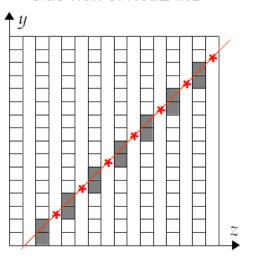
Side view of NeuLAND



Procedures

- Obtain the positions of bars with signals
- Reconstruct the muon track from the bar positions
- 3 Calculate positions of interaction point of the muon

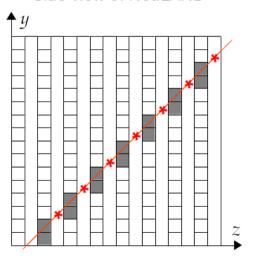
Side view of NeuLAND



Procedures

- Obtain the positions of bars with signals
- Reconstruct the muon track from the bar positions
- Calculate positions of interaction point of the muon
- Obtain calibration parameters via data fitting

Side view of NeuLAND



Procedures

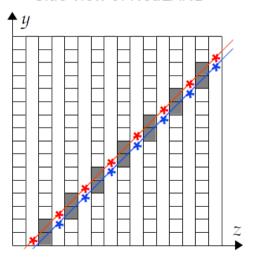
- Obtain the positions of bars with signals
- Reconstruct the muon track from the bar positions
- Calculate positions of interaction point of the muon
- Obtain calibration parameters via data fitting

Data fitting on positions:



(Original size: 32.361×200 bp)

Side view of NeuLAND



Procedures

- Obtain the positions of bars with signals
- Reconstruct the muon track from the bar positions
- Calculate positions of interaction point of the muon
- Obtain calibration parameters via data fitting

Data fitting on positions:



(Original size: 32.361×200 bp)

Simultaneous fitting of global and local parameters

Comparisons on PMT time offsets

Comparisons on effective speed of light

Comparisons on time synchronization

Summary and outlook