# An Innovative Crowd Segmentation Approach based on Social Force Modelling

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Abstract—The effective segmentation of the crowd in the video data serves as a crucial role in the analysis of crowd behavior. The conventional crowd segmentation techniques usually rely on the spatial distribution or temporal trajectories of the agent in the crowd. However, the psychological influence among the relatively high density of people is omitted. In this research, an enhanced Social Force Model is utilized to describe motions of each agent. In this model, an innovative pattern namely Grouping Center is modeled as the primary descriptor for the crowd segmentation. The extracted optical flow is firstly mapped to the detected agents, next the experiment indicates that by estimating the model components such as desired force and repulsive force in the phycological perspective, the successful segmentation could still be achieved on the circumstance that agents from different groups are randomly mixed up. The game engine simulated crowd video with ideal behavior scenario are exploited to assess the performance of the proposed segmentation approach, the result indicates the algorithm is capable of handling the segmentation of the mixed crowd at early stage.

Keywords- crowd segmentation, motion prediction, social force model,

#### I. INTRODUCTION

The analysis of crowd behaviors is becoming the crucial research issue to support the maintenance of public safety. With the widely installation of CCTV cameras at public area, the massive amount of recorded video data could be exploited for the prediction of potential danger, real-time anomaly alarming and the forensic evidences. The segmentation of the crowd in video data usually serve as the pre-processing stage in the framework of crowd analysis, yet it is a vital component of the entire pipeline. The precise segmentation of the crowd would have significant influence on the performance of feature extraction, model training and behavior recognition.

The technique of Crowd Segmentation usually consists two fundamental procedures, which are Individual Detection and Motion Prediction. The aim of Individual Detection is to verify as much agents from the crowd as possible. In most crowded videos, the density of the crowd is high. The high density will cause the difficulty to maintain the accuracy of individual detection, for example the issue of frequent occlusion will make the tracking and locating of the pedestrian extremely difficult. In order to address this issue, approaches of individual detection under heavy occlusion are proposed by various researches [1][2][3][4][5][6][7]. Some other segmentation approaches attempt to consider the crowd as a single entity to avoid the

individual detection. By analyzing the flow-based information of this entity, the crowd is segmented according to its spatial and temporal relationship. However, this kind of approach isn't capable of handling the following situation. Assuming agents with two different destination are randomly distributed, the approach can't segment these agents into two groups until they are spatially separated, or the temporal information such as trajectory are calculated after some amount of time. In order to achieve the successful segmentation of these two groups in the early stage, this contribution devised a segmentation approach based on Individual Detection and the concept of Social Force. This approach will be able to segment the randomly distributed crowd according to the proposed Group Attraction Force. The detailed algorithm will be introduced in next section. The aim of Motion Prediction is to predict the long-term behavior of detected individuals according to their spatial and temporal information. In the procedure of Motion Prediction, the state such as position and trajectory are fed to a behavioral model to estimate the individual's next motion. Once the long-term behavior of each detected individual is obtained, a classifier could be implemented to cluster the estimated behavior for the segmentation of the crowd.

The techniques of individual detection consist of two approaches. In the first approach, the statistical or shape information is extracted from the image and feed to the trained classifier for the detection result [1][2][3][4][5]. In the second approach, a rough estimation such as head/shoulder detector is implemented to generate hypotheses, and then the concept of Expectation Maximization (EM) is exploited to verify these hypotheses based on various iterations [6][7].

In the research of Lan [1], the image is firstly preprocessed into a foreground image. Then the silhouette of the foreground image is sampled and transformed with Discrete Fourier Transform as a Fourier Descriptor. The silhouette can be reconstructed anytime with Fourier coefficients. The Euclidean distance between two Fourier Descriptors is utilized to measure the similarity of silhouettes. Next, KNN and locally-weighted regression are used to find the closest match of target image among the trained sample sets. The machine learning techniques are frequently utilized as well in recent researches. Kang [3] mentioned for crowd with high density, appearance-based approaches with patterns such as HOG, Scale-invariant feature transform (SIFT) and Linear Binary Pattern (LBP) don't have good performance. Techniques of Deep Learning are widely implemented in computer vision field. In the research, the so called Fully Convolutional Neural Network (FCNN) is used for crowd segmentation with both appearance and motion features. In the FCNN, a multiple stage deep learning architecture with features of appearance, motion and structure is devised. In this research, the FCNN claims to have advantages than the conventional CNN.

In the research of Tu [6], the concept of EM is utilized to verify the segmentation hypothesis, and attempt to achieve the correct detection under serious occlusion situation. In the first step this approach, a rough head and shoulder detection is applied on the image, each detected pedestrian is named hypotheses. However, since the complexity of scene and the occlusion problem, much false positive detection occurred. For the second step, the image is divided into a grid of patches. Next this research proposed an algorithm to calculate the so-called 'Affinity' between each patch and hypotheses. In order to further optimize the segmentation hypotheses, the concept of EM is imported to address this problem. An approach with similar methodology but different details is proposed in [7]. In this approach, a scale-invariant interest point operator [8] is firstly used to locate the Points of Interests. Around these points, patches with certain radius are extracted from the image. Next an agglomerative clustering scheme [9] is implemented on each patch to obtain a representation of its structure as the signature for the hypotheses verification. Then the spatial occurrence distribution is used to measure the distance between different signatures. For each iteration of the E-step, patches are extracted from the interest points, and the distance is measured to the trained codebook using spatial occurrence distribution to verify the hypotheses. And for the M-step, the measured result will be used to update the codebook. After several iterations, the updated hypotheses are recognized as detected pedestrians.

With the premise of well devised agent behavioral model and successfully detected agent motion state, it is expected to have an accurate prediction of agent's next motion. However, in real-life cases, this premise is very difficult to be fulfilled. This fact results the performance of conventional motion prediction approaches is not satisfying in real-life scenario. Furthermore, the conventional approach is only capable of making the prediction of short term movement. As long as the approach is applied onto the longer-term prediction, the accuracy decays drastically. In order to address this issue, two alternative approaches are proposed by following up researches. 1) Instead of detecting the motion state of an agent, a grid is placed onto the current image. For each cell of this grid, the transition probability is calculated for an agent moving to next cell [10] [11]. 2) All trajectories inside scene are first detected, and then trajectories with similar patterns are clustered. The clustered trajectory will be used for prediction of next motion [12] [13].

The Social Force Model [15] is primarily applied in the field of crowd simulation, and sometime crowd analysis. In most of the segmentation algorithm, spatial information such as co-ordinate, size and shape, temporal information such as trajectory are exploited. However, the behavior of pedestrians within highly dense environment could be easily influenced by the psychological factor with its neighbors. In this research, the Social Force Model along

with the improved concept such as personal space and perception field are utilized to devise an innovative signature for crowd segmentation namely Grouping Center. The result of following experiments indicates the segmentation approach with psychological concept is capable of handling the mixed crowd from multiple groups.

The structure of this contribution is composed as follows. Section 2 gives a detailed introduction of the proposed crowd segmentation approach. To be specific, the innovative concept of Group Attraction Force is explained and the extraction algorithm is introduced. In section 3, the proposed algorithm is formulated to achieve a more explicit explanation. In section 4, the proposed approach is implemented on the simulated crowd video to assess the performance of segmentation. Section 5 provides the conclusion and discusses the future work.

## II. CROWD SEGMENTATION APPROACH AT HIGHLY MIXED STATE

In the previous work [14], a simulation model based on the Social Force Model (SFM) is devised to generate crowd behavior with visual realism. The concept of SFM is firstly proposed by Helbing [15], and widely exploited on crowd simulation and behavioral modeling. The fundamental concept of SFM is the motion of every pedestrian among the crowd is affected by three types of psychological-related forces: Desired Force, Repulsive Force and Avoidance Force, which is formulated as Equation 1. Which  $sf_i$  is the final force determines the motion of pedestrian i.  $f_d$  is the desired force,  $f_{ji}$  is the repulsive force from neighbor j, and  $f_{oi}$  is the avoidance force from obstacle o.

$$sf_i = f_d + \sum_{j \neq i} f_{ji} + \sum_{j \neq i} f_{oi}$$
 (1)

In the proposed simulation model, an innovative group attraction force is devised to achieve a better visual realism of the simulated crowd. In the simulation scenario, sixty agents from three different groups are randomly distributed on the stage. Each agent is mapped with a behavioral model which controls the agent's motion. The behavioral model contains parameters such as personal space, radius, angle of perception. The radius describes the size of each agent. The personal space and angle of perception determine the repulsive force affected to the agent. If a neighboring agent exists in the range of personal space and perception angle, the repulsive force will be generated, otherwise it will be omitted. In order to further increase the visual realism, based on the assumption that simulated agents always attempt to stay closer to the cluster with agents from same group, the concept of Group Attraction Force is devised to enhance the conventional SFM. To model the Group Attraction Force, agents with same group number appeared in the perception field of current agent are allocated firstly. Then the average position of the allocated agents is calculated as the Grouping Center. Next a force from current agent to the grouping center will be estimated as the Group Attraction Force. The simulation result shows the group attraction force embedded behavioral model presents the better performance than the conventional SFM on the visual realism. The enhanced SFM with Group Attraction

Force could be adjusted as Equation 2, in which  $f_{Gi}$  is the Group Attraction Force.

$$sf_i = f_d + \sum_{j \neq i} f_{ji} + \sum_{j \neq i} f_{oi} + f_{Gi}$$
 (2)

By further investigating the distribution of Grouping Center, it could be observed that despite the spatial distribution of agents from three different groups is sparse and random, the Grouping Centers from different groups are naturally clustered. As illustrated in Fig. 1(a), the spatial distribution of agents is rather random. It is almost impossible to use classifiers such as KNN to segment. However, according to the Group Attraction Force Model, the calculated distribution of group centers exhibits significant patterns, as illustrated in Fig. 1(b). The Fig.1(c) shows the distribution of grouping centers in large scale. It could be explicitly observed that grouping centers are naturally clustered.

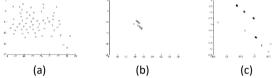


Fig.1 The comparison of distribution between spatial position and group center. (a) Spatial distribution. (b) Grouping center distribution. (c) Magnified grouping center distribution

Upon this observation, it is worthy to try segmenting agents according to the clustering result of group centers. Therefore, the simple KNN clustering algorithm is exploited for the segmentation. It's assumed that the value of K is correctly determined, in this case K equals to 3. As illustrated in Fig. 2(a) shows the Ground Truth spatial distribution of agents from three different groups. Agents from same group are labeled with same shape. Fig. 2(b) shows the segmented result using proposed approach. In this case, 53 out of 60 agents are correctly segmented comparing to the ground truth.

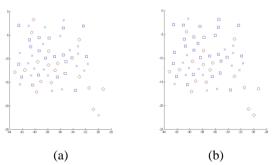


Fig. 2. Comparison between ground truth and segmentation result. (a) Ground Truth. (b) Segmentation Result using Grouping Center

The previous paragraphs proved that the Grouping Center is capable of segmenting crowd consists of multiple groups at randomly distributed state. In order to exploit the Grouping Center to achieve desired segmentation performance, there is still a fundamental issue needs to be addressed. In the previous paragraph, it is assumed that agent knows the group number of other agents. Based on this assumption, the Grouping Center could be calculated. Nevertheless, in the process of segmentation on the crowd

video obtained from the CCTV cameras, the group number of each pedestrian is unknown. Thus, the Group Centers for pedestrians can't be obtained directly. Therefore, an innovative algorithm to estimate Group Attraction Force from two consecutive frames are introduced. The architecture of the algorithm is illustrated as Fig. 3.

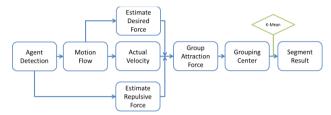


Fig. 3. The framework of the proposed crowd segmentation approach

For each agent, the group attraction force  $f_{Gi}$  is unknown. if the actual force  $sf_i$ , desired force  $f_d$ , repulsive force  $\sum_{j \neq i} f_{ji}$  and avoidance force  $\sum f_{oi}$  are obtained, the group attraction force could be calculated according to Equation 2. With group attraction force obtained, the Grouping Center could be calculated.

In the procedure illustrated in Fig. 3, every agent needs to be detected at the first step using the main stream pedestrian detection algorithm such as [3]. For each detected agent, the parameters of SFM such as personal space, radius and angle of perception are estimated according to the current environment. The radius of agent could be estimated upon the average pixel number of all detected agents. Once the radius is determined, the personal space could be decided empirically. The angle of perception could be set the same value of the simulation model. Therefore, the repulsive force  $\sum_{j\neq i} f_{ji}$  of all detected agents i could be calculated.

On the other hand, the global flow-based information between two consecutive frames are extracted, and mapped to each agent. The flow-based information such as optical flow could be transformed into the actual velocity of mapped agent and set as the actual social force  $sf_i$ . The estimation of desired force  $f_d$  could be a difficult task, since the group number of current agents is unknown, the destination can't be determined so far. In order to address this issue, several constrains have been made to simplify the problem. First, agents are assigned into two groups. The destinations of these groups located at opposite directions on the scene. Second, if the actual force of agent is large enough, the direction of desired force is same to the actual force, since the magnitude of repulsive and group attraction force are usually much smaller than the desired force. Third, if the actual force isn't large enough, which means it closes to repulsive force. In this case, the direction of agent's desired force will be randomly determined. Consider the complexity of the scenario, the avoidance force  $\sum f_{oi}$  is omitted. In the following experiment, the scene consists with only floor, agents, destination. The obstacle is removed from scene.

With the estimated desired force, repulsive force and actual social force, the group attraction force could be estimated according to Equation 2. Since the group attraction force is a vector, the grouping center could be

calculated with the current position of agent. With the estimated grouping centers, the simple classifier such as KNN could be utilized to segment the crowd.

In next section, the proposed algorithm is formulated in order to help better understanding the proposed approach.

#### III. FORMULATION OF THE PROPOSED APPROACH

According to the framework introduced in Fig. 3, the group attraction force  $f_{Gi}$  of agent i could be derived from the Equation 2. As explained in previous section, the avoidance force is omitted in order to simplify the model. The estimated group attraction force  $f_{Gi}$  of agent i is presented as Equation 3.

$$f_{Gi} = sf_i - f_d - \sum_{i \neq i} f_{ji}$$
 (3)

In which  $sf_i$  is the actual social force obtained from the optical flow information.  $f_d$  is the estimated desired force, the magnitude of  $f_d$  is a constant  $\alpha$ , and its direction could be presented as Equation 4.

$$dir(f_d) = \begin{cases} dir(sf_i) & ||sf_i||_2 > \tau \\ \theta & otherwise \end{cases} \tag{4}$$

Which  $\tau$  is a threshold constant, if the magnitude of actual force  $sf_i$  is greater than the threshold  $\tau$ , the estimated direction of  $f_d$  will be same as actual force. Otherwise the direction of  $f_d$  will be randomly determined between two goals.

The calculation of actual force  $sf_i$ , is based on the flow-based information. In this research, the classic Horn Schunk optical flow patterns are first extracted from two consecutive frames. Next the standard pedestrian detection algorithm is applied to obtain the position of every agent. By mapping the optical flow to each agent, the actual force could be determined. The actual force  $sf_i$  could be represented as Equation 5.

$$sf_i^{x,y} = \sum k f_o^{x\pm 1,y\pm 1} \tag{5}$$

Which  $sf_i^{x,y}$  is the actual force of agent i at position xy,  $f_o^{x\pm 1,y\pm 1}$  is the optical flow vector on position xy, k is the weight factor, when x=0 and y=0, k=1, otherwise k=0.4 in this case.

The calculation of repulsive force  $f_{ji}$  is imported from Qingge [16]'s Velocity Perception Based SFM. In the conventional SFM, the repulsive force is set as a constant magnitude value  $\beta$ . If the distance between current agent and any neighboring agents is less than personal space  $\rho$ , the repulsive force will be applied to the agent, otherwise no repulsive force will be applied. This solution will generate the significant 'vibration' phenomenon between agents. Instead of using a constant value, Equation 6 is devised to describe the most realistic repulsive force between agent i and j.

$$f_{ji} = A_i e^{(r_{ij} - d_{ij})/B_i} n_{ij}$$
(6)

In which  $A_i$  and  $B_i$  are the constant values to control the magnitude scale of the repulsive force.  $r_{ij}$  is the sum of two agents' radius.  $d_{ij}$  is the distance between two agents. The exponential function assures the fast dispersing when the

distance between two agents increase and vice versa.  $n_{ij}$  describe the direction of the repulsive force. In order to further increase the realism of simulated repulsive force, the personal space  $\rho$  and perception field are also considered. The extracted repulsive force is further regulated using Equation 7. If the distance between two agents is smaller than the summation of agent i's personal space and agent j's radius, the repulsive force remain the same. Otherwise the repulsive force equals to zero since the distance between two agents is not in the range of the personal space.

$$f_{ji} = \begin{cases} f_{ji} & d_{ij} \le \rho_i + r_j \\ 0 & otherwise \end{cases}$$
 (7)

Even if the distance satisfied the range of personal space, the perception of agent and the motion direction could still be specifically modeled. In real-life, the repulsive force exhibits different patterns at three different circumstances. While two agents are moving along similar direction, the agent in the front shouldn't be affected by the repulsive force from the one behind it. While two agents are moving along opposite direction and about to collide, they should be both affected by the repulsive force. While two agents are moving along opposite direction but back to back, both of them shouldn't be affected by the repulsive force. According to these details, the repulsive force  $f_{ji}$  could be further constrained using Equation 8.

$$f'_{ji} = \begin{cases} \theta((v_j - v_i)n_{ij})G_{ij}f_{ji} & d_{ij} > \rho_i + r_j \\ (1 + \theta((v_j - v_i)n_{ij})G_{ij})f_{ji} & d_{ij} \le \rho_i + r_j \end{cases}$$
(8)  
In which  $\theta(z)$  equals to zero if  $z < 0$ , and equals to  $z < 0$ .

In which  $\theta(z)$  equals to zero if z < 0, and equals to z otherwise. The range of  $G_{ij}$  is from 0 to 1, which is used to impact the magnitude of repulsive force when two agents are moving along opposite directions.

With the proposed Equations, the Group Attraction Force  $f_{Gi}$  of agent i could be estimated. Since  $f_{Gi}$  is a vector, the co-ordinate of Grouping Center could be finally obtained using  $f_{Gi}$  and agent i's co-ordinate  $(x_i, y_i)$ .



Fig. 4. A snapshot of the simulated video

### IV. EXPERIMENTAL SETTINGS AND RESULTS

The video data used for experiment is generated by 3D game engine Unity. The scene is composed with 40 agents, each agent is replaced with a sphere for easier individual detection. Agents are assigned to two different groups, 20 agents for each. Agents from different groups are mapped

with different textures. As illustrated in Fig. 4, agents from group 1 are mapped with dark green color and those from group 2 are mapped with bright white color. The two hexagons marked destinations of these two groups, group 1 will attempt to move toward to the upper destination and group 2 to the lower one. Each agent in the stage is mapped with a behavioral model which consists with the desired force, repulsive force and group attraction force strictly defined using previously proposed formulations.

Fig. 4 illustrates the randomly distribution of two groups. Agents from both groups are mixed up. It's very difficult to segment the crowd in current state using spatial information. According to the architecture of the proposed segmentation procedure in Fig. 3, the first step is to extract the optical flow using the Horn Schunk algorithm. In the experiment, frame number 20 and 22 are selected for the optical flow extraction. The reason of using the early frames is that agents at this time are still in randomly distributed state. Since the distribution of agents would quickly become clustered under the impact of the group attraction force. The purpose of skipping one frame instead of using two consecutive ones is to ensure the magnitude of extracted optical flow is large enough. Because if the magnitude is too small, the optical flow field would be easily affected by factors such as deviation and noise. Fig. 5(a) illustrates the extracted HS optical flow field from Fig. 4. In this experiment, the grid size is set to 10 pixels. Since the ultimate goal of this research is to achieve real-time detection, the overly condensed sampling grid would have the chance to affect the performance of the system. It is necessary to declare that the magnitude of the optical flow is amplified by 3 times to provide a better visual experience. However, the actual motion of each agent isn't as drastic as the figure shows.

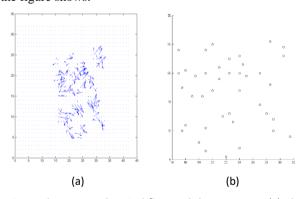


Fig. 5. The extracted optical flow and detect agents. (a) The extracted optical flow field using frame 20 and 22. (b) The spatial distribution of detected agents

According to the framework proposed in Fig. 3, agents in the scene need to be correctly detected. In most of the case, conventional people detectors could satisfy the requirement unless the crowd density is too high. Since the agent is simplified into a sphere, shape detection algorithm such as Hough Circles could be more reliable. The agent detection result is shown as Fig. 5(b).

Next step of the procedure is mapping the detected agents with extracted optical flow flied to obtain the actual social force. According to the Equation 5 proposed in previous section, the average of all nine neighboring optical

flow vectors is exploited as the final optical flow for current agent, and the parameter K is still set to 0.4. The obtained actual social forces are illustrated as Fig. 6. By comparing the detected agent's motion with the group truth, most behaviors of the agent are basically matched, despite with some deviations.

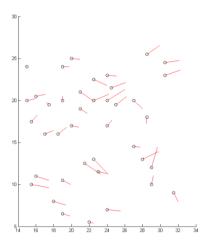


Fig. 6. The mapping result of actual social force

In next step, the repulsive force of each agent is calculated according to the Equation (7)(8) and (9). The estimation result of the repulsive force is illustrated as Fig. 8. In this case, the value of personal space  $\rho$  is set to 5 pixels, radius of agent r is set to 0.5 pixel. The value of parameter  $A_i$  and  $B_i$  should be 2 and 0.5. In Fig. 7 the value of  $B_i$  is set as 1 for a better visual presentation, the actual calculation would still be using 0.5.

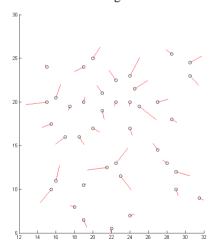


Fig. 7. The estimated repulsive force

The Fig. 8 illustrated the estimation result of desired force of each agent. In the experiment, it is assumed the two destinations are successfully detected using Points of Interest detection techniques. Therefore, the only estimation in this step is to determine which destination the agent belongs to using Equation 4. In the experiment, the magnitude of the desired force is set to the average amount of actual force affected from agents.

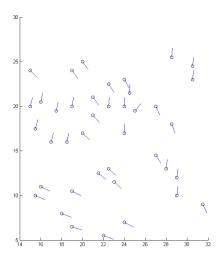


Fig. 8. The estimated desired force

Once the Actual Force is extracted, and repulsive force and desired force are extracted, the final Group Attraction Force could be estimated with Equation 3. According to the definition of Group Attraction Force, the Grouping Center of each agent could be calculated. Next, the ordinary classifier is applied to the grouping center for the clustering. The clustering result is illustrated as Fig. 9. Agents from different groups are marked with different labels. Comparing the ground truth shown in Fig. 4, most of agents are correctly segmented, the accuracy in this example is 87.5%.

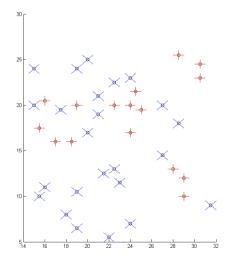


Fig. 9. The segmentation result using the proposed approach

#### V. CONCLUSION

In order to achieve the crowd segmentation at the highly mixed state, an innovative segmentation approach involved with enhanced Social Force Model is devised in this contribution. Based on the assumption that pedestrians from same group would attempt to move toward its group, a novel concept namely Group Attraction Force is devised to achieve a more accurate description of the simulated crowd. On the opposite, the generated Grouping Center could be utilized for the crowd segmentation even at agents from two different groups are highly mixed up. Unlike the conventional segmentation techniques who is relying on patterns such as co-ordinate and trajectory, the proposed approach attempts to achieve the crowd segmentation with

certain semantic explanation. The experiment on the simulated video data indicates the proposed approach is capable of handling the crowd segmentation with the high accuracy.

#### REFERENCES

- Lan Dong, Vasu Parameswaran, Visvanathan Ramesh, Imad Zoghlami. Fast Crowd Segmentation Using Shape Indexing. 2007 IEEE 11th International Conference on Computer Vision. 14-21 Oct. 2007. 10.1109/ICCV.2007.4409075
- [2] Navneet Dalal, Bill Triggs. Histograms of Oriented Gradients for Human Detection. In International Conference on Computer Vision Pattern Recognition (CVPR '05), Jun 2005, San Diego, United States. IEEE Computer Society, 1, pp.886–893, 2005.
- [3] Kai Kang, Xiaogang Wang. Fully Convolutional Neural Networks for Crowd Segmentation. arXiv:1411.4464v1 [cs.CV] 17 Nov 2014
- [4] Navneet Dalal, Bill Triggs. Histograms of Oriented Gradients for Human Detection. In International Conference on Computer Vision Pattern Recognition (CVPR '05), Jun 2005, San Diego, United States. IEEE Computer Society, 1, pp.886–893, 2005.
- [5] P. Sinha. Object Recognition via Image Invariants: A Case Study. In Investigative Ophthalmology and Visual Science. Volume 35, Pages 1735-1740. Sarasota. Florida, May 1994.
- [6] Tu P., Sebastian T., Doretto G., Krahnstoever N., Rittscher J., Yu T. (2008) Unified Crowd Segmentation. In: Forsyth D., Torr P., Zisserman A. (eds) Computer Vision ECCV 2008. ECCV 2008. Lecture Notes in Computer Science, vol 5305. Springer, Berlin, Heidelberg
- [7] Bastian Leibe, Edgar Seemann, Bernt Schiele. Pedestrian Detection in Crowded Scenes. In 2005 IEEE Computer Society Conference on Computer Vision and Pattern Recognition (CVPR'05) (2005). San Diego, California. June 20, 2005 to June 26, 2005. pp: 878-885.
- [8] D. Lowe. Distinctive image features from scale-invariant keypoints. IJCV, 60(2):91–110, 2004.
- [9] B. Leibe, A. Leonardis, and B. Schiele. Combined object categorization and segmentation with an implicit shape model. In ECCV'04 Workshop on Stat. Learn. in Comp. Vis., pages 17–32, 2004
- [10] K. Tanaka, "Detecting collision-free paths by observing walking people," in Proceedings of the 2002 IEEE/RSJ International Conference on Intelligent Robots and Systems, (Lausanne, Switzerland), pp. 55—60, 2002.
- [11] S. Tadokoro, M. Hayashi, Y. Manabe, Y. Nakami, and T. Takamori, "Motion planner of mobile robots which avoid moving human obstacles on the basis of stochastic prediction," in IEEE International Conference on Systems, Man and Cybernetics, pp. 3286—3291, 1995.
- [12] S. Gaffney and P. Smyth, "Tra jectory clustering with mixtures of regression models," Tech. Rep. 99-15, University of Californa, Irvine, 1999.
- [13] M. Bennewitz, W. Burgard, and S. Thrun, "Learning motion patterns of persons for mobile service robots," in Proceedings of the 2002 IEEE/RSJ International Conference on Intelligent Robots and Systems, pp. 3601—3606, 2002.
- [14] Yu Hao, Zhijie Xu, Ying Liu, Jing Wang, Jiulun Fan. Crowd Synthesis Based on Hybrid Simulation Rules for Complex Behaviour Analysis. In Proceedings of the 24th International Conference on Automation & Computing, 2018
- [15] Helbing, Dirk, and Peter Molnar. Social force model for pedestrian dynamics, Physical review E 51, no. 5, 4282. 1995.
- [16] Qingge Ji, Fuchuan Wang, Ting Zhu, VPBS: A Velocity-Perception-Based SFM Approach for Crowd Simulation, 2016 International Conference on Virtual Reality and Visualization