Topic Modeling



What is Topic Modeling?

Anything that tries to answer...

"What is the underlying topic(s) that this document is about?"

Let's motivate with an example...

```
"I love my pet rabbit."

"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I gave leftovers of that dish to my pet, mr. rabbit"

"Rabbits make messy pets."

"My rabbit growls when I pet her."

"He has five rabbits."

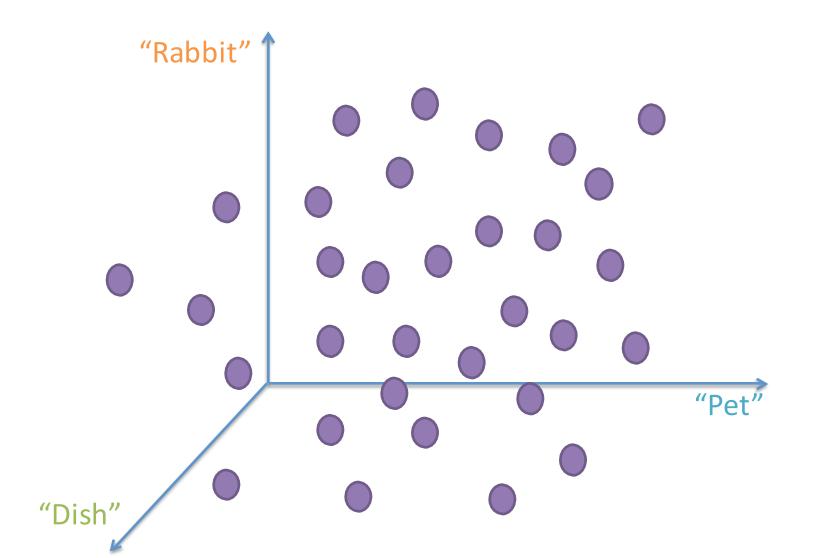
"I had this weird dish with fried rabbit."

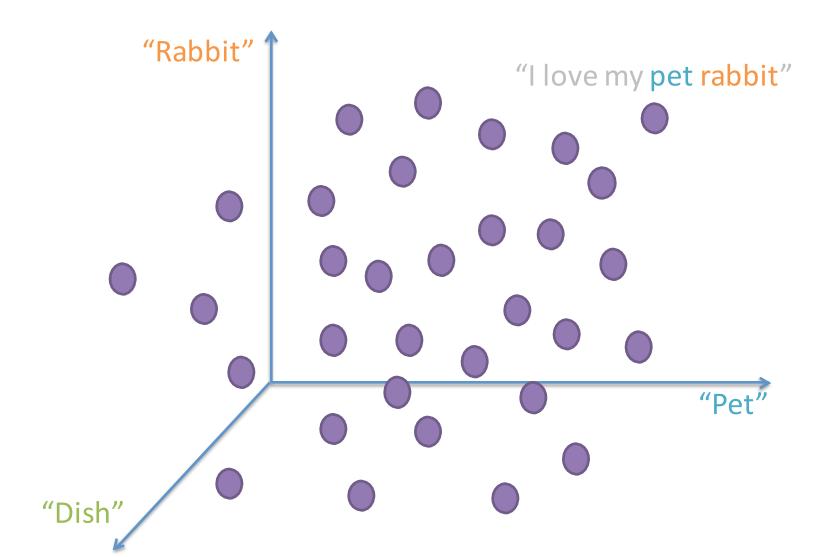
"That's my pet rabbit's favorite dish."
```

```
"I love my pet rabbit."
"That dish yesterday was amazing."
"She cooked the best rabbit dish ever."
"I gave leftovers of that dish to my pet, mr. rabbit"
"Rabbits make messy pets."
"My rabbit growls when I pet her."
"He has five rabbits."
"I had this weird dish with fried rabbit."
"That's my pet rabbit's favorite dish."
```

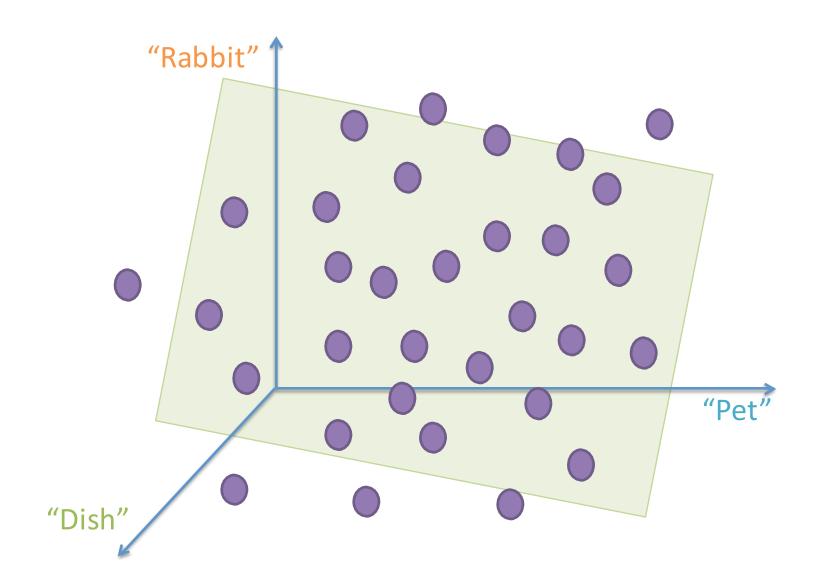
Remove stop words, only keep nouns, end up with 3 features: "rabbit", "pet", "dish"

```
"I love my pet rabbit."
"That dish yesterday was amazing."
"She cooked the best rabbit dish ever."
"I gave leHovers of that dish to my pet, mr. rabbit"
"Rabbits make messy pets."
"My rabbit growls when I pet her."
"He has five rabbits."
"I had this weird dish with fried rabbit."
"That's my pet rabbit's favorite dish."
Remove stop words, only keep nouns, end up with
3 features: "rabbit", "pet", "dish"
```

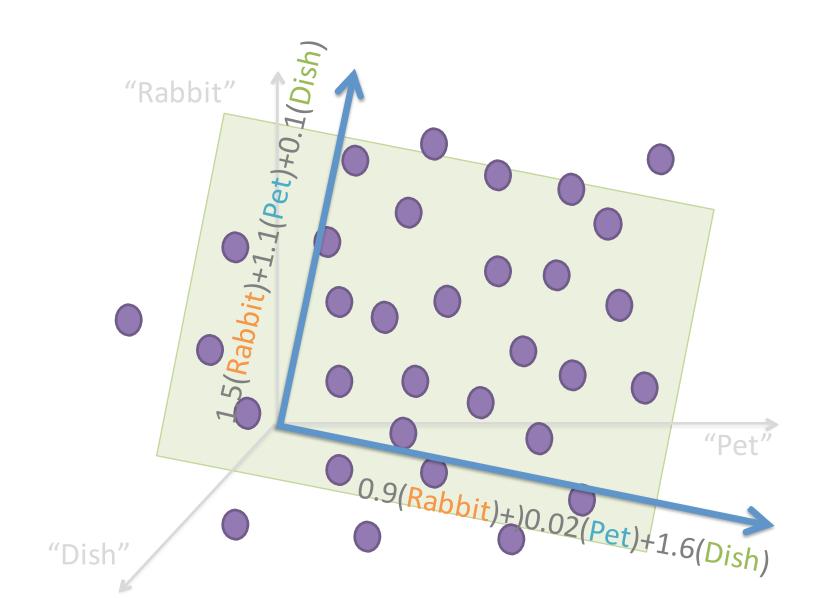




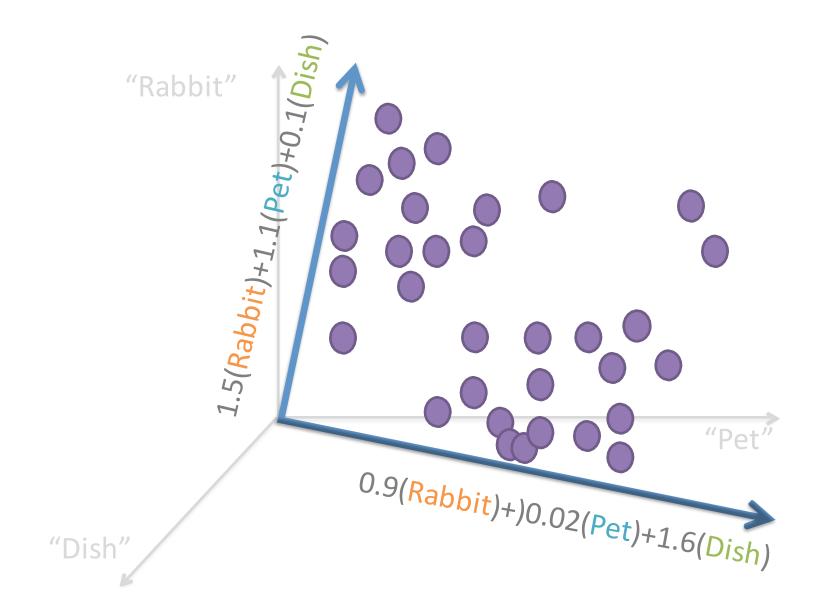
3D → 2D Feature Extraction



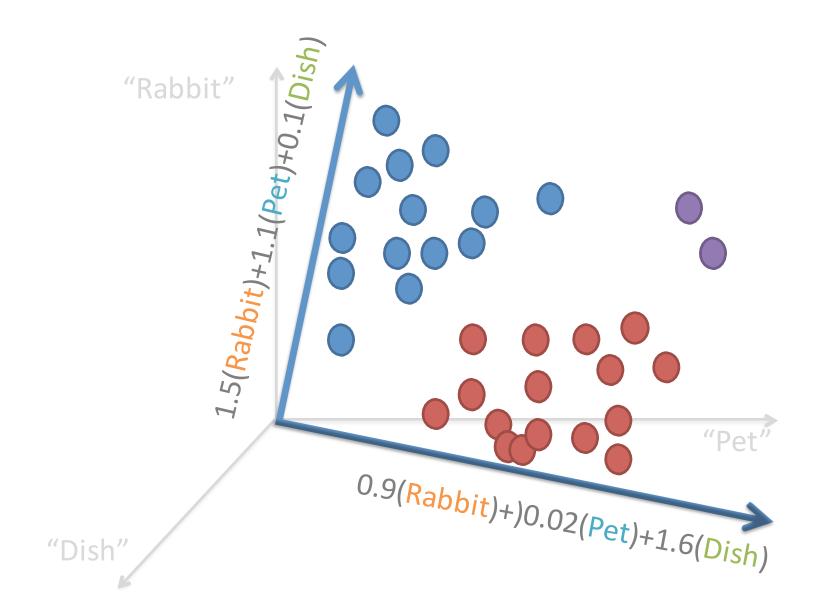
3D → 2D Feature Extraction



3D → 2D Feature Extraction



Clustering is easier on this space



What are the clusters?

```
"I love my pet rabbit."

"Rabbits make messy pets."

"My rabbit growls when I pet her."

"He has five rabbits."
```

```
"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."
```

"I gave leftovers of that dish to my pet, Mr. Rabbit" "That's my pet rabbit's favorite dish."

```
Axis 1: 1.5(Rabbit) + 1.1(Pet) + 0.1(Dish)
Axis 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish)
```

```
"I love my pet rabbit."

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"My rabbit growls when I pet her."

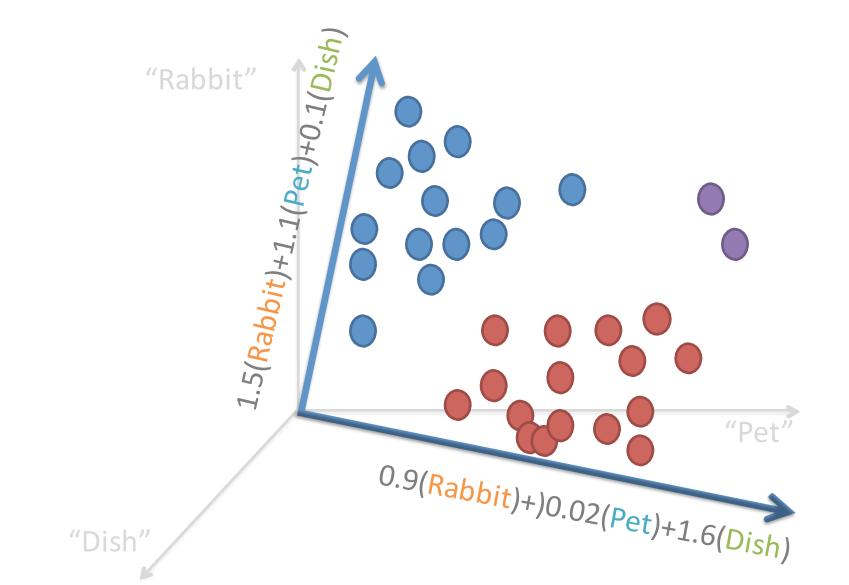
"He has five rabbits."
```

"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."

"I gave leftovers of that dish to my pet, Mr. Rabbit" "That's my pet rabbit's favorite dish."



```
Axis 1: 1.5(Rabbit) + 1.1(Pet) + 0.1(Dish)
Axis 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish)
```

```
"I love my pet rabbit."

"Rabbits make messy pets."

"My rabbit growls when I pet her."

"He has five rabbits."
```

"That **dish** yesterday was amazing."

"She cooked the best **rabbit dish** ever."

"I had this weird **dish** with fried **rabbit**."

"I gave leftovers of that **dish** to my **pet**, mr. **rabbit**" "That's my **pet rabbit**'s favorite **dish**."

```
Axis 1: 1.5(Rabbit) + 1.1(Pet) + 0.1(Dish)
Axis 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish)
```

"I love my pet rabbit."

Axis1: High

"Rabbits make messy pets."

"My rabbit growls when I pet her."

"He has five rabbits."

"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."

"I gave leftovers of that **dish** to my **pet**, mr. **rabbit**" "That's my **pet rabbit**'s favorite **dish**."

```
Axis 1: 1.5(Rabbit) + 1.1 (Pet) + 0.1(Dish)
Axis 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish)
```

"I love my pet rabbit."

Axis1: High

"Rabbits make messy pets."

"My rabbit growls when I pet her."

"He has five rabbits."

Axis1: Low
Axis2: High

"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."

"I gave leftovers of that **dish** to my **pet**, mr. **rabbit**" "That's my **pet rabbit**'s favorite **dish**."

```
Axis 1: 1.5(Rabbit) + 1.1 (Pet) + 0.1(Dish)
Axis 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish)
```

"I love my **pet rabbit**."

Axis1: High

"Rabbits make messy **pets**."

"My **rabbit** growls when I **pet** her."

"He has five **rabbits**."

Axis1: Low
Axis2: High

"That dish yesterday was amazing."

"She cooked the best rabbit dish ever."

"I had this weird dish with fried rabbit."

Axis1: High "I gave leftovers of that dish to my pet, mr. rabbit" Axis2: High "That's my pet rabbit's favorite dish."

TOPIC 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow Food, rabbit dishes

"I love my **pet rabbit**."

Topic1: High "Rabbits make messy pets."

Topic2: Low "My rabbit growls when I pet her."

"He has five rabbits."

Topic1: Low "That dish yesterday was amazing."

Topic2: High "She cooked the best **rabbit dish** ever."

"I had this weird dish with fried rabbit."

Topic1: High "I gave leftovers of that dish to my pet, mr. rabbit"

Topic2: High "That's my pet rabbit's favorite dish."

```
TOPIC 1: 1.5(Rabbit) + 1.1(Pet) + 0.1(Dish) \leftarrow Pet rabbits, pets
TOPIC 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow Food, rabbit dishes
```

T1
87% 13% "I love my pet rabbit."
88% 12% "Rabbits make messy pets."
80% 20% "My rabbit growls when I pet her."
66% 34% "He has five rabbits."

```
2% 98% "That dish yesterday was amazing."
16% 84% "She cooked the best rabbit dish ever."
15% 85% "I had this weird dish with fried rabbit."
```

47% 53% "I gave leftovers of that **dish** to my **pet**, mr. **rabbit**" 42% 58% "That's my **pet rabbit**'s favorite **dish**."

Topics are not (hard) clusters. A document does not belong to a single topic. Each topic is present in the document up to a certain degree. For each doc, we have a distribution over topics.

```
T1
     T2
             "I love my pet rabbit."
87%
      13%
     12%
             "Rabbits make messy pets."
88%
             "My rabbit growls when I pet her."
80% 20%
66% 34%
             "He has five rabbits."
             "That dish yesterday was amazing."
 2%
      98%
             "She cooked the best rabbit dish ever."
16%
     84%
15%
             "I had this weird dish with fried rabbit."
     85%
             "I gave leftovers of that dish to my pet, mr. rabbit"
47%
     53%
             "That's my pet rabbit's favorite dish."
42%
      58%
```

TOPIC 1: $1.5(Rabbit) + 1.1(Pet) + 0.1(Dish) \leftarrow Pet rabbits, pets$ TOPIC 2: $0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow Food, rabbit dishes$

What is a topic?

TOPIC 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow Food, rabbit dishes

What is a topic?

When writing about a specific topic (like pet rabbits), we use some words more often than others.

Words like "pet", "rabbit", "lettuce", "cage", "fluffy", etc. are more likely to appear, words like "dish", "transmission", "opaque", "affair" are less likely to appear.

A topic can be thought of as a Probability distribution over all possible words

TOPIC 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow Food, rabbit dishes

What is a topic?

Probability distribution over all possible words

Word	Prob in [Pet Rabbits]	Prob in [Food]
pet	2.3x10 ⁷	1.2x10 ¹⁰
rabbit	7.9x10 ⁷	3.4x10 ⁸
dish	6.8x10 ¹¹	4.5x10 ⁷
car	3.1x10 ¹²	1.8x10 ¹²
hello	8.3x10 ⁹	1.4x10 ⁹
the	7.4x10 ⁴	7.3x10 ⁴
love	5.4x10 ⁸	3.9x10 ⁸
affair	3.0x10 ¹³	2.1x10 ¹³
delicious	9.1x10 ⁹	9.8x10 ⁸

• • •

TOPIC 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow Food, rabbit dishes

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car	3.1x10 ¹²	1.8x10 ¹²
hello	8.3x10 ⁹	1.4x10 ⁹
the	7.4x10 ⁴	7.3x10 ⁴
love	5.4x10 ⁸	3.9x10 ⁸
affair	3.0x10 ¹³	2.1x10 ¹³
delicious	9.1x10 ⁹	9.8x10 ⁸

• • •

TOPIC 2: 0.9(Rabbit) + 0.02(Pet) + 1.6(Dish) \leftarrow Food, rabbit dishes

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car	3.1x10 ¹²	1.8x10 ¹²
hello	8.3x10 ⁹	1.4x10 ⁹
the	7.4x10 ⁴	7.3x10 ⁴
love	5.4x10 ⁸	3.9x10 ⁸
affair	3.0x10 ¹³	2.1x10 ¹³
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...

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...

Topic Modeling

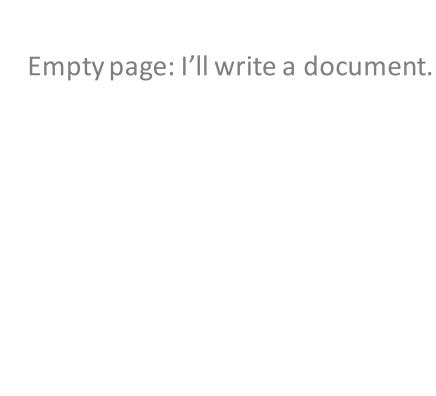
Let's use an algorithm specifically developed to find topics.

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Model the process of writing

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Model the process of writing



Let's use an algorithm specifically developed to find topics.

Model the process of writing

Empty page: I'll write a document.

First, I'll decide what topics to write on. Choose the topic distribution.

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Empty page: I'll write a document.

First, I'll decide what topics to write on. Choose the topic distribution. Sex:2%, Drugs:33%, Rock'n Roll:65%

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Empty page: I'll write a document.

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Ok. I'll write the document word by word (bag of words). First word!

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A Rock'n Roll word. Randomly pick a word according to the prob. distribution of the Rock'n Roll topic.

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Guitar

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Guitar riff

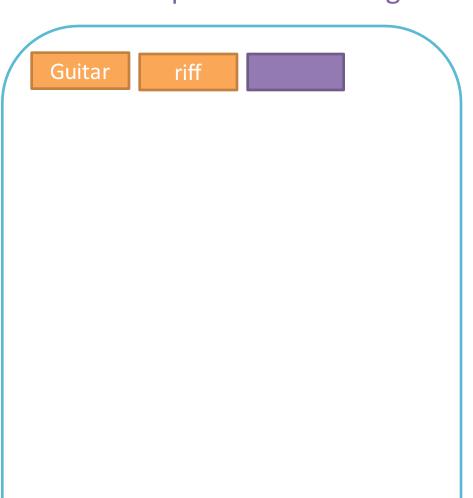
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Guitar riff cocaine

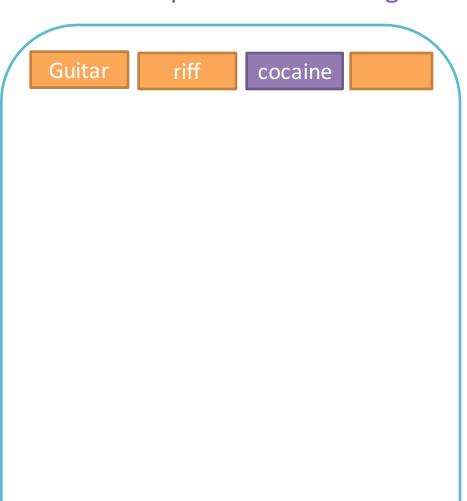
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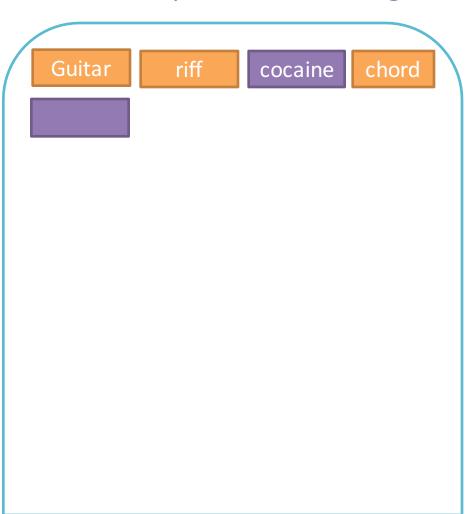
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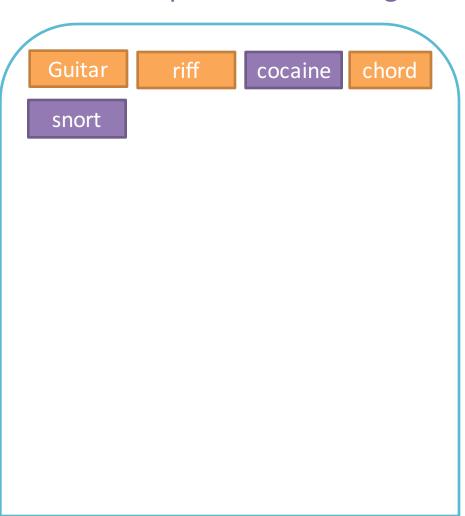


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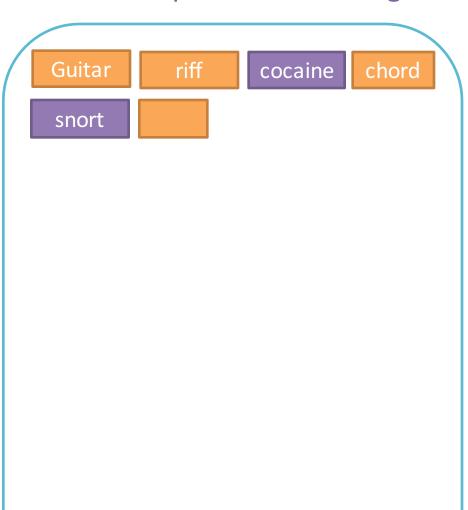
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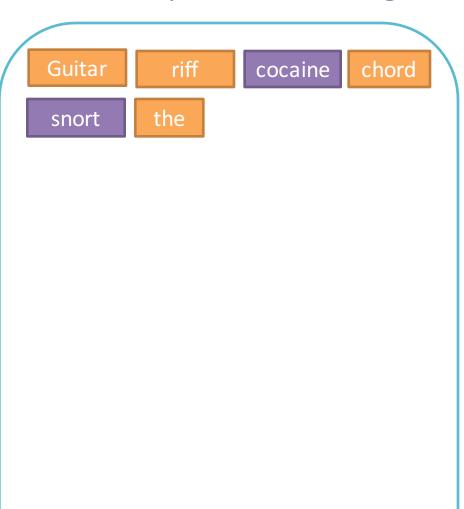


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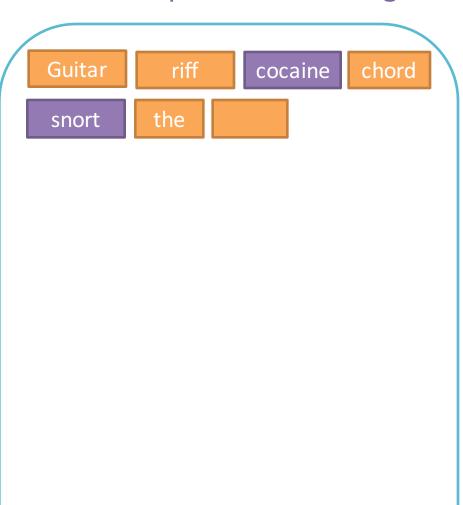
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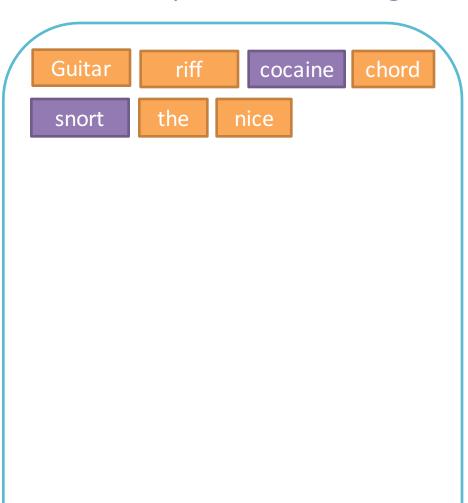


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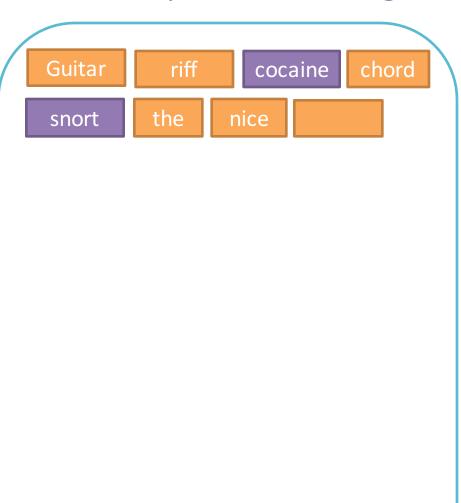
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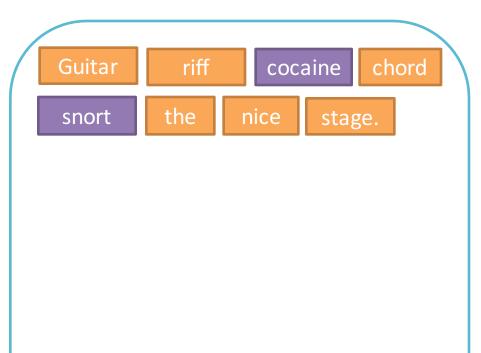


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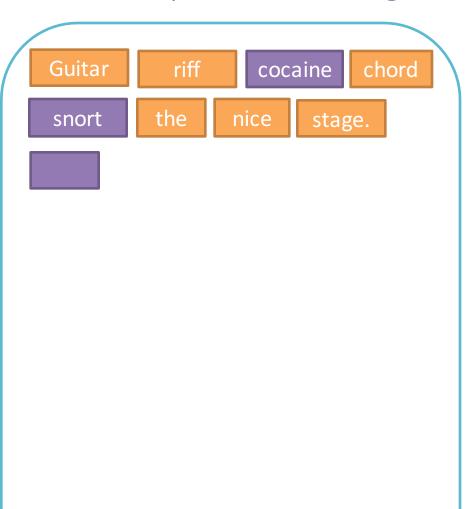
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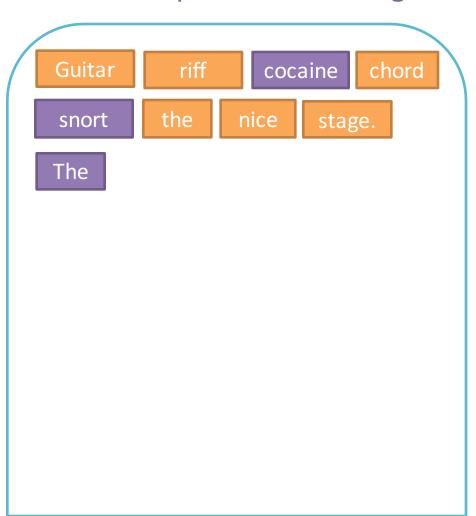


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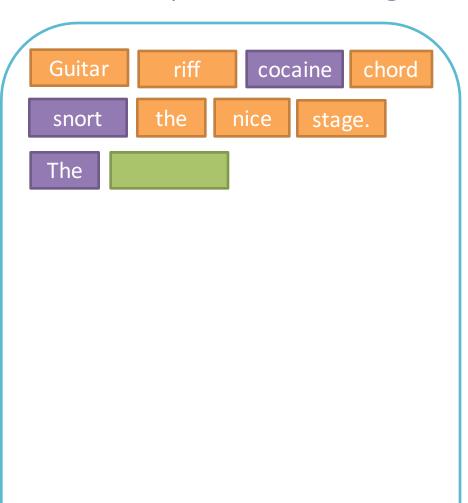
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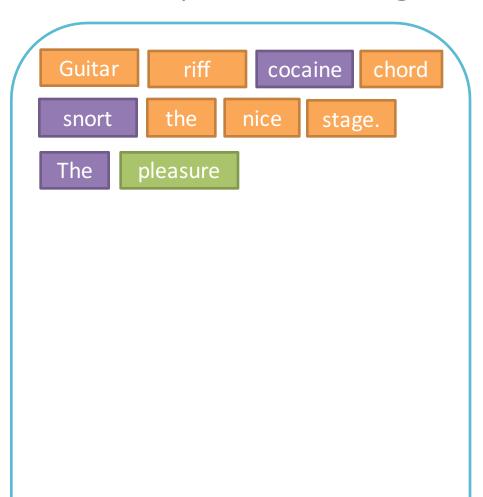


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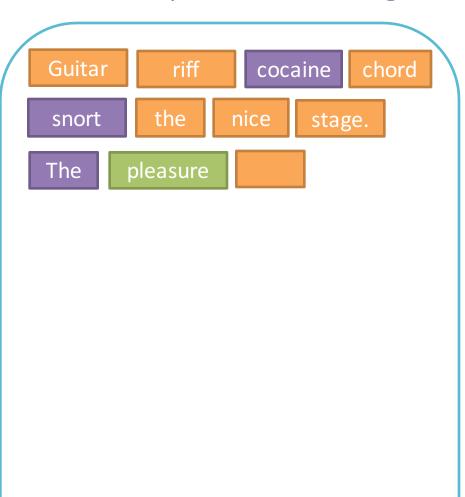
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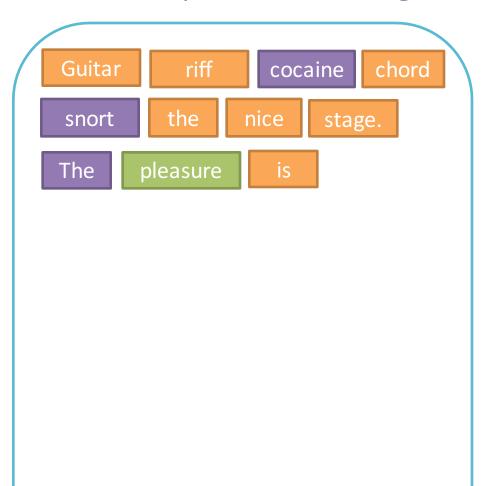


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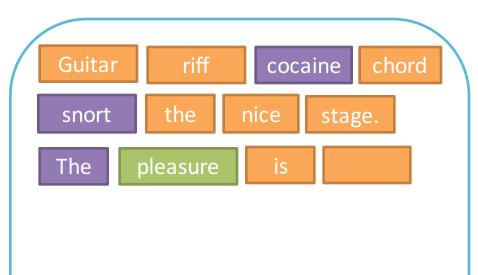
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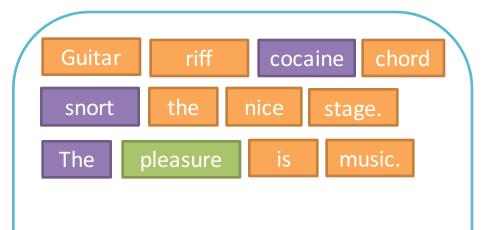


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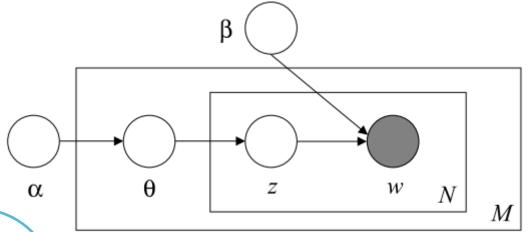
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Choose next word's topic. Roll the dice.



Guitar riff cocaine chord

snort the nice stage.

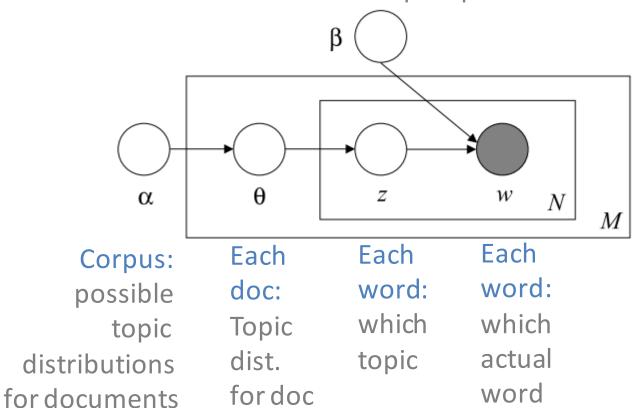
The pleasure is music.

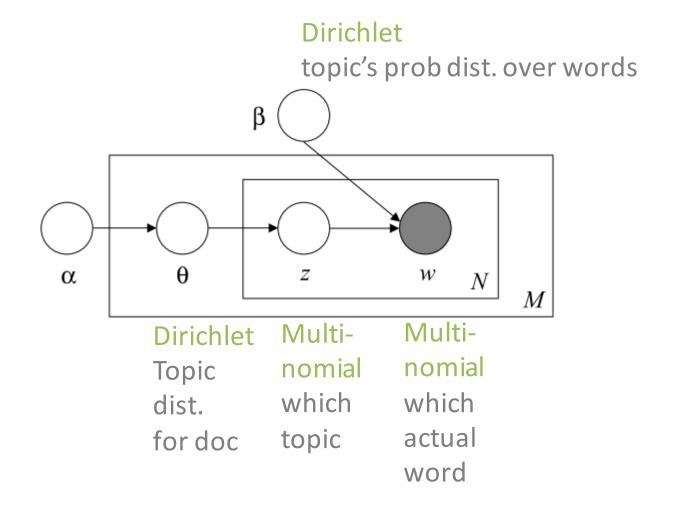
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Choose next word's topic.
Roll the dice.

Choosing word for a topic:

topic's prob dist. over words





$$p(\beta_{1:K}, \theta_{1:D}, z_{1:D} | w_{1:D}) = \frac{p(\beta_{1:K}, \theta_{1:D}, z_{1:D}, w_{1:D})}{p(w_{1:D})}$$

How to solve this?

Math is tricky, but it's still Bayes at heart...

Options (see resources):

- Gibbs Sampling
- Variational Bayesian Inference

Moving to Topic Space

What we've essentially done is transformed our higher dimensional space into a much reduced "topic space".

We can use this topic space as we would any vector space of observations, for ML purposes.

Topic Modeling

What and why

Rotating the coordinate space

We regard documents as made of different portions of topics Instead of different proportions of words.

Word space → Topic space

Similarity of docs

Searching for similar documents may be more meaningful in topic space

Dimensionality reduction

Clustering/classifying in topic space can be easier/meaningful

Intuition, Understanding

Look at prob. Dist. For topics, and how they are distributed over docs.