Plan:

1. Define p-values
2. Explain concept of p-values
3. Explain null distributions and relationship to p-values

Inferential Analysis: p-values

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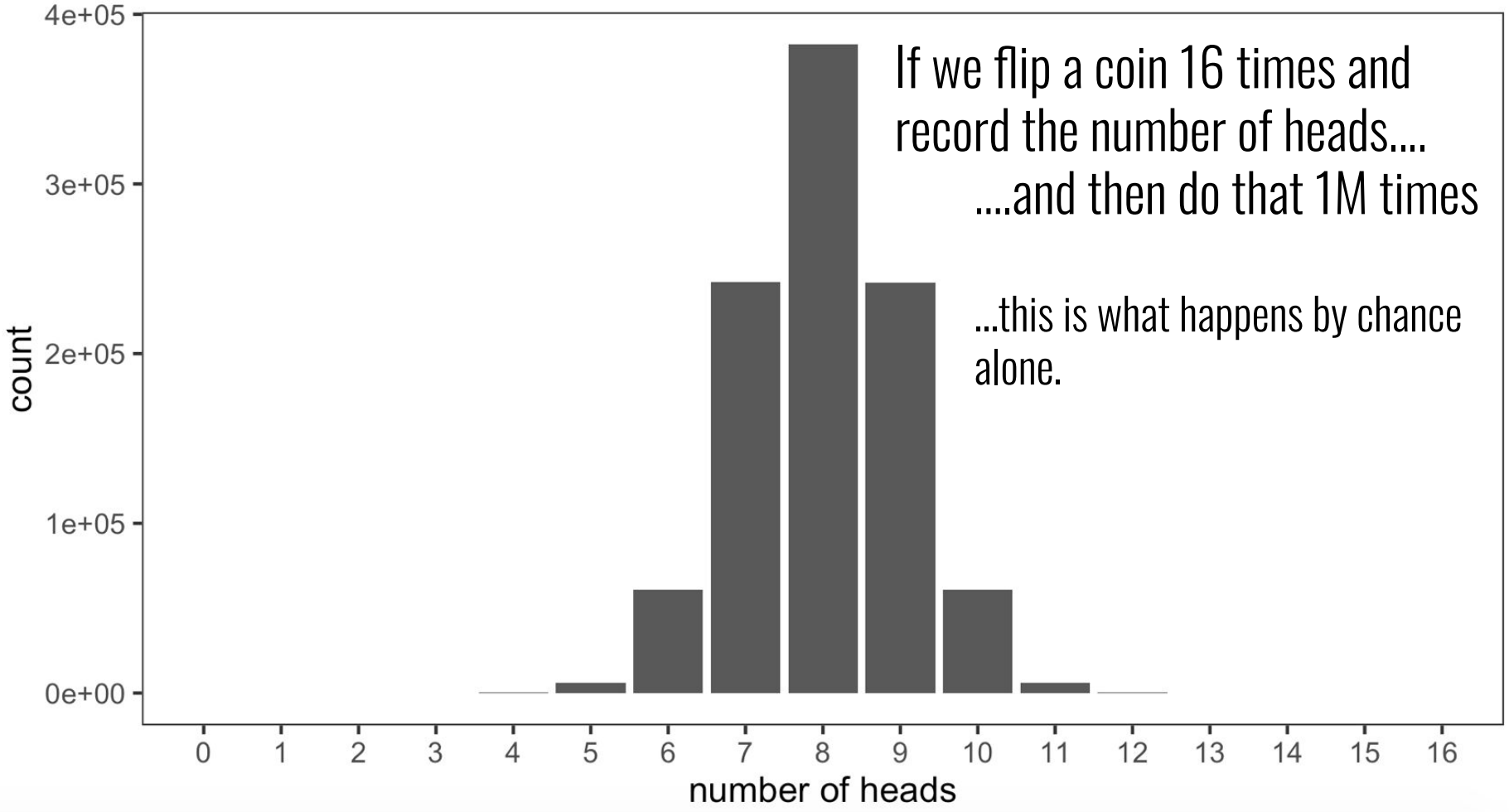
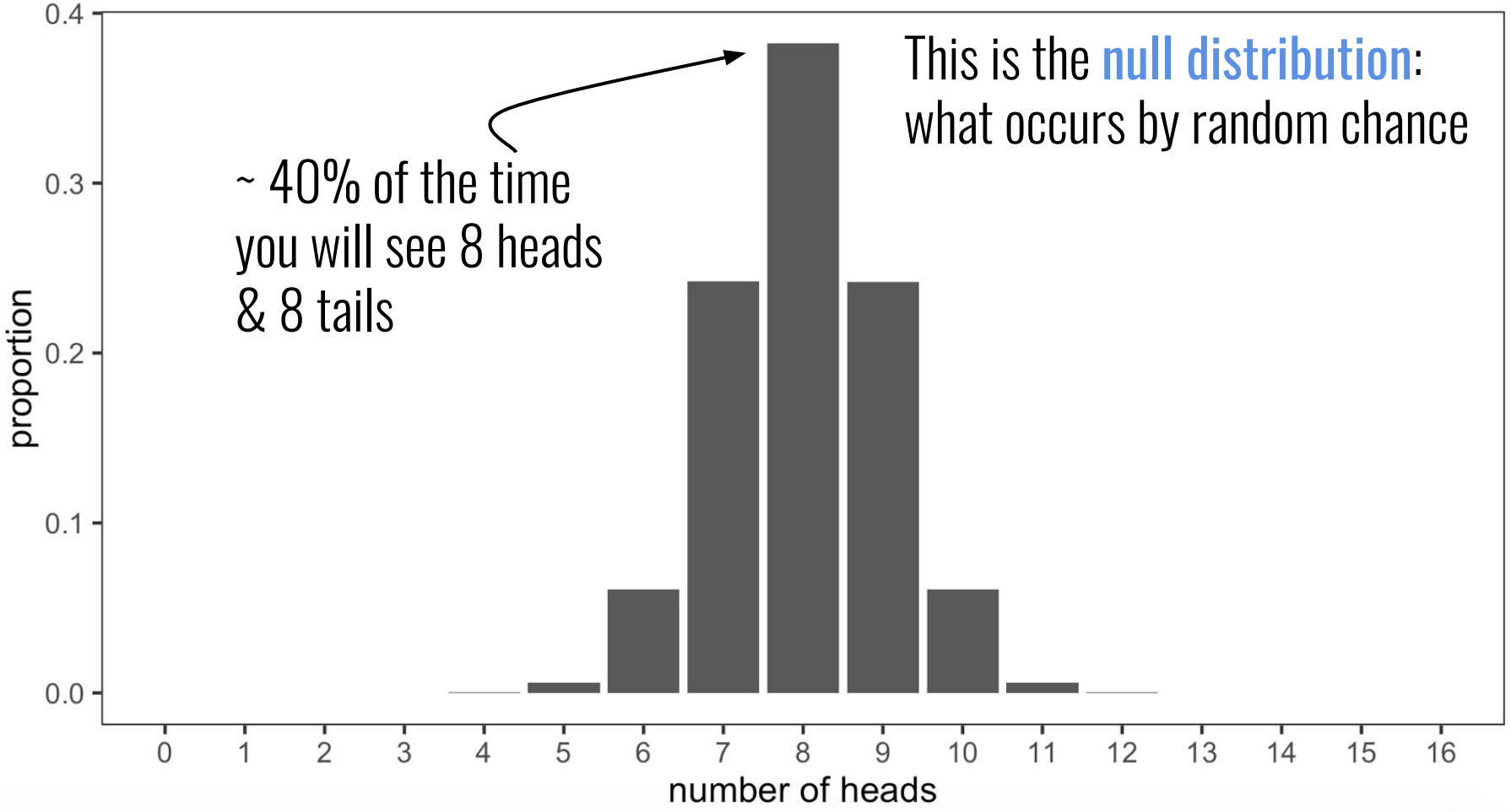
p-value : the probability of getting the observed results (or results more extreme) by chance alone

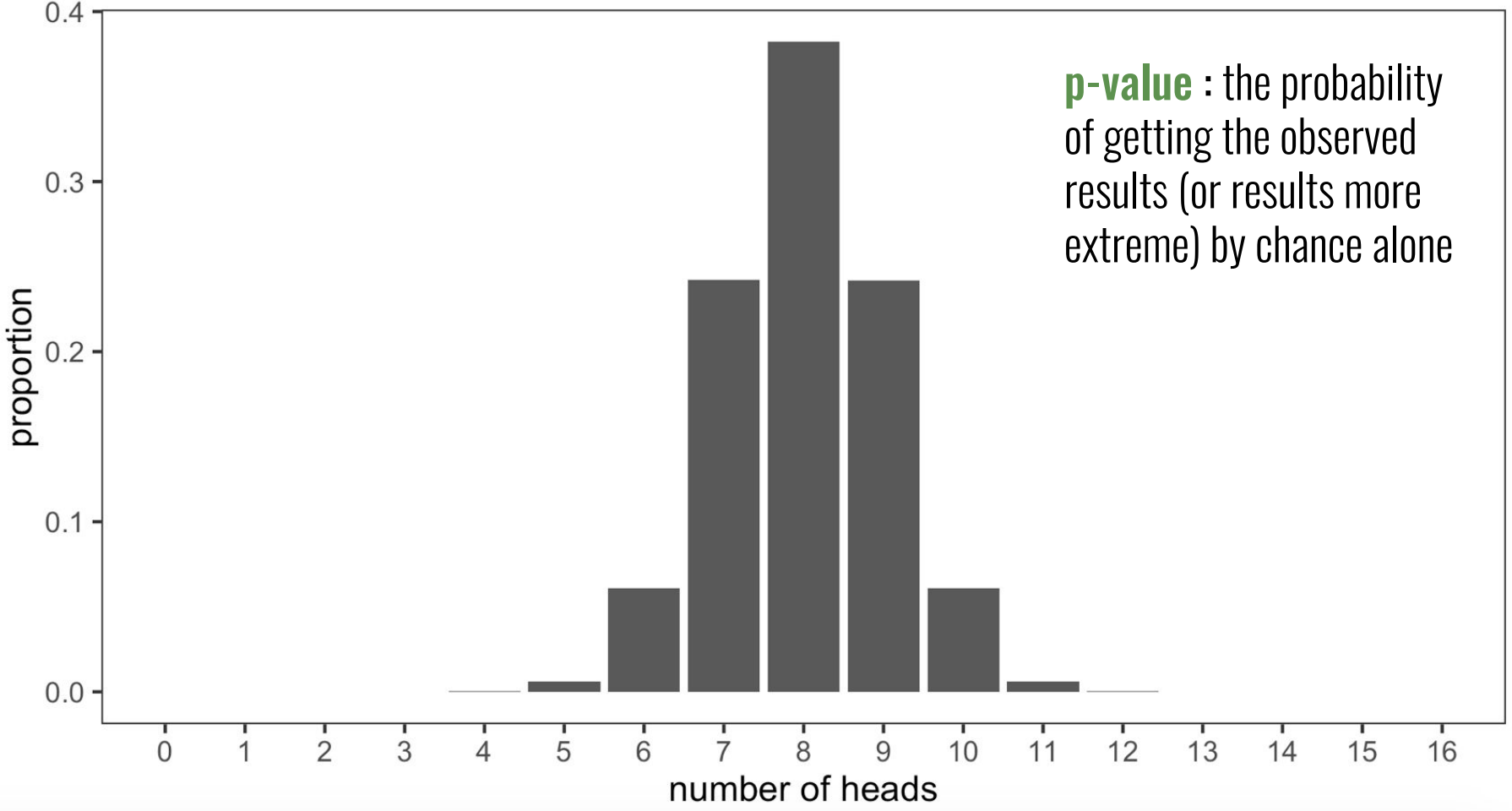


If we flip a coin 16 times and record the number of heads....

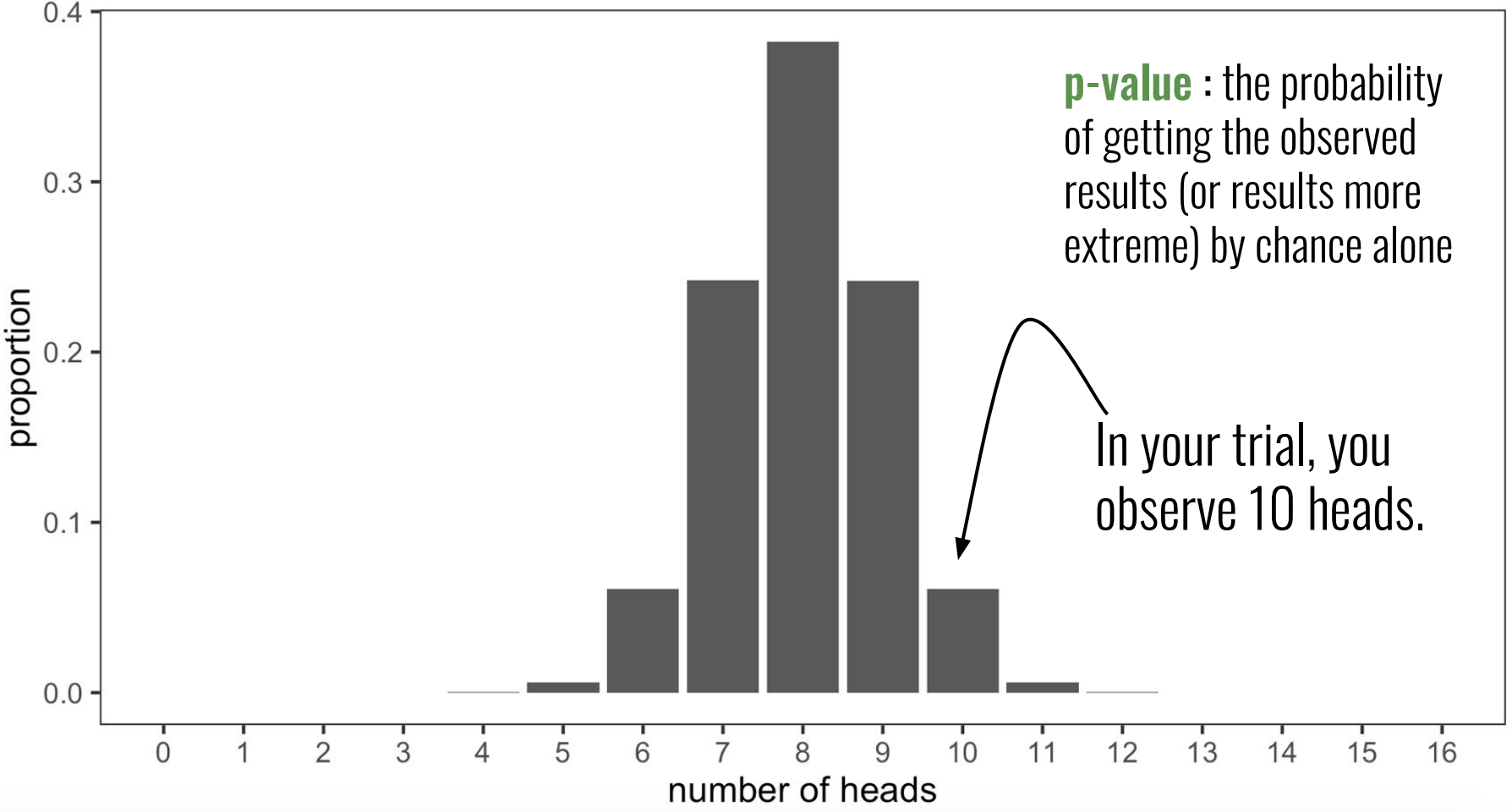
....and then do that 1M times

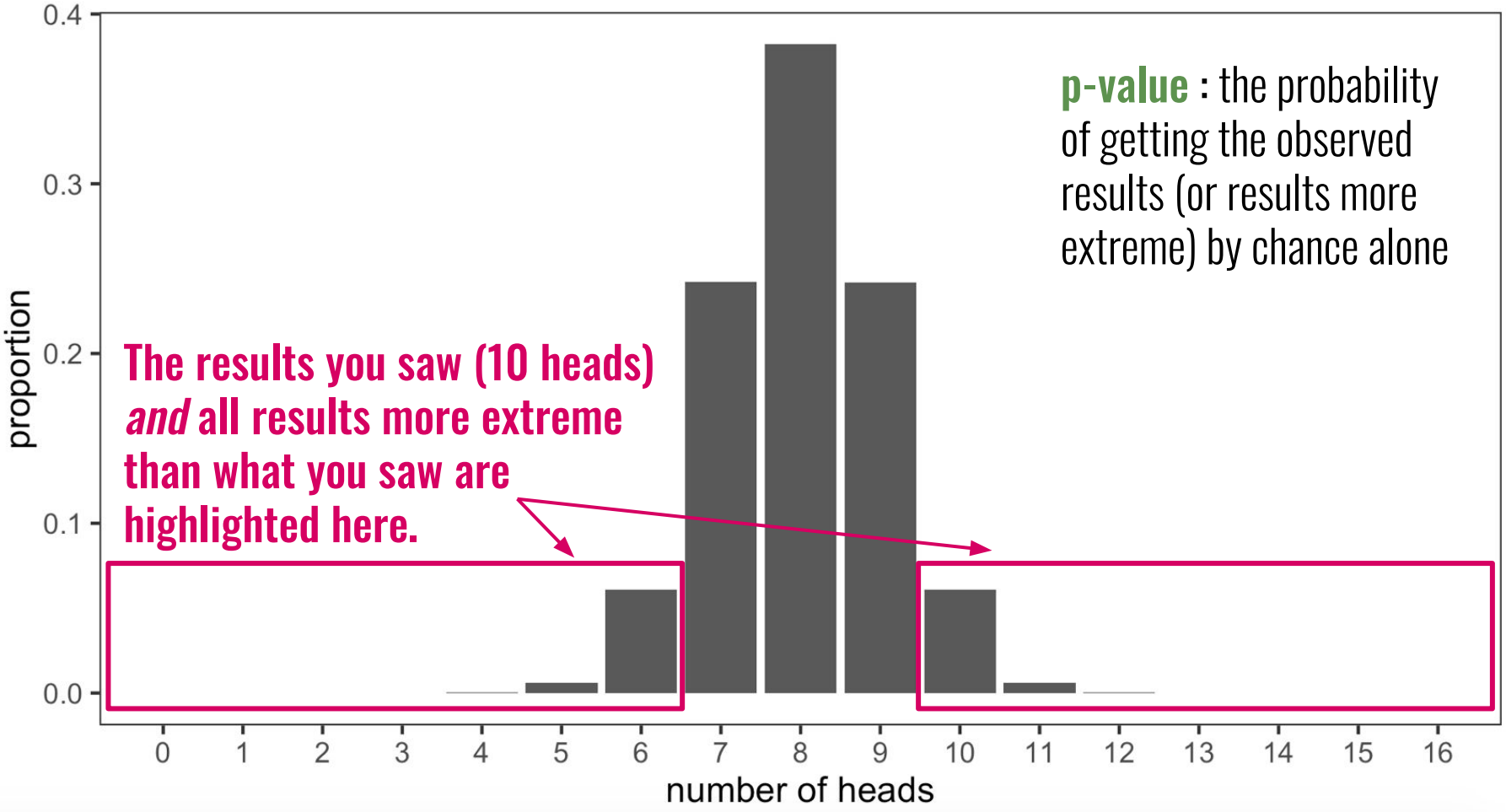
...this is what happens by chance alone.

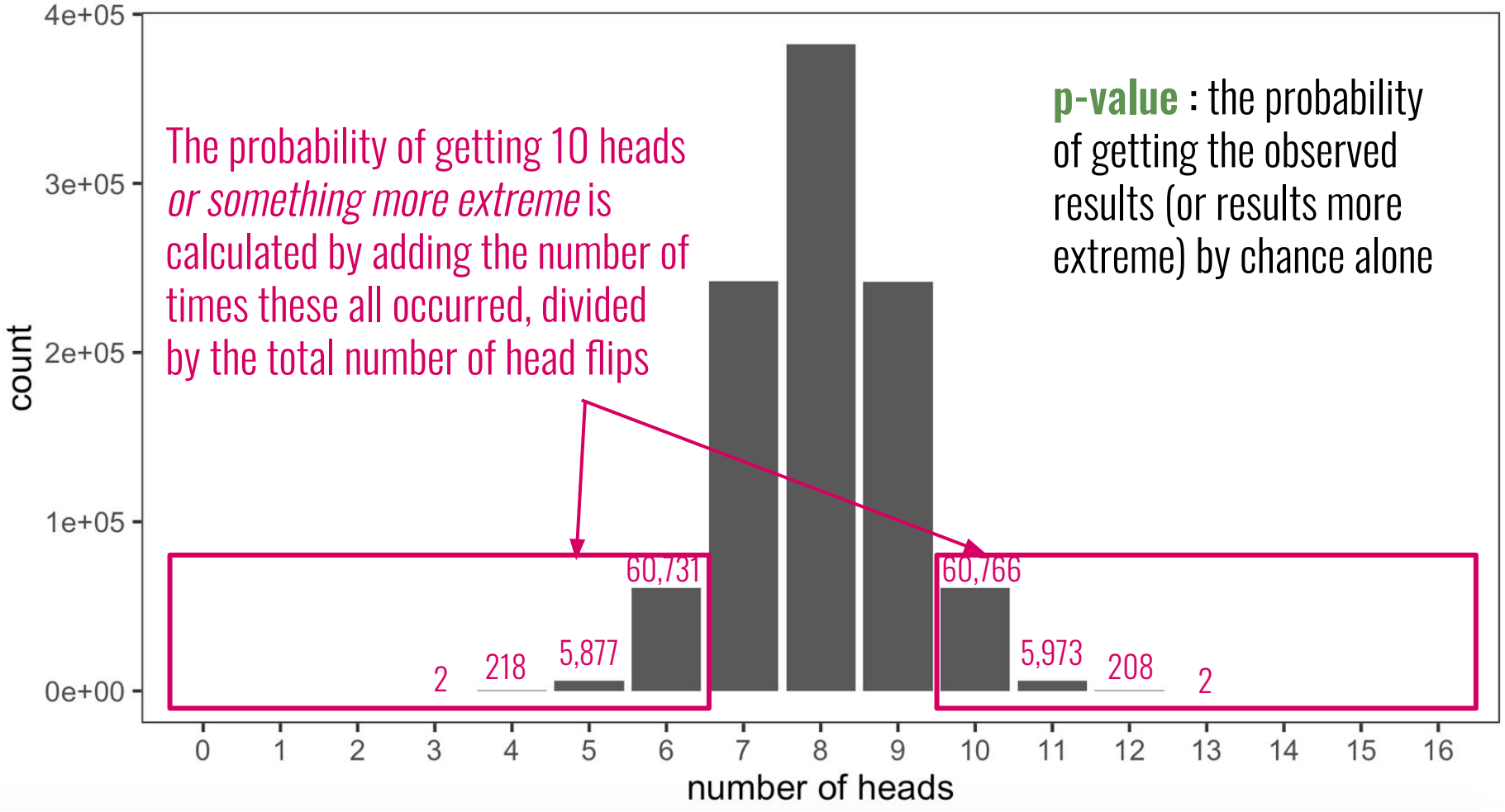

This is the null distribution:
what occurs by random chance
~ 40% of the time
you will see 8 heads
& 8 tails
proportion
0.4
0.3
0.2
0.1
0.0
0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
number of heads

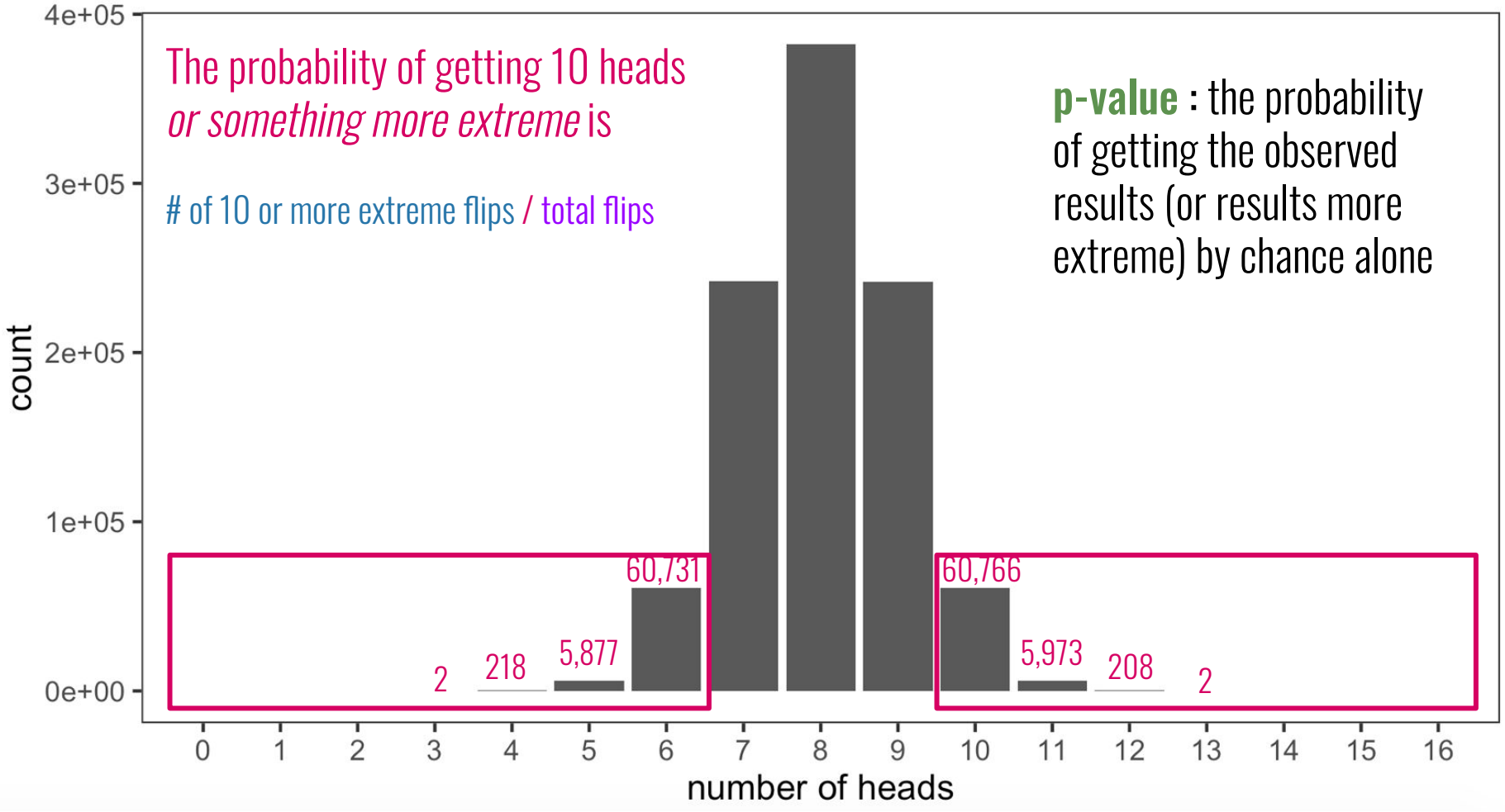


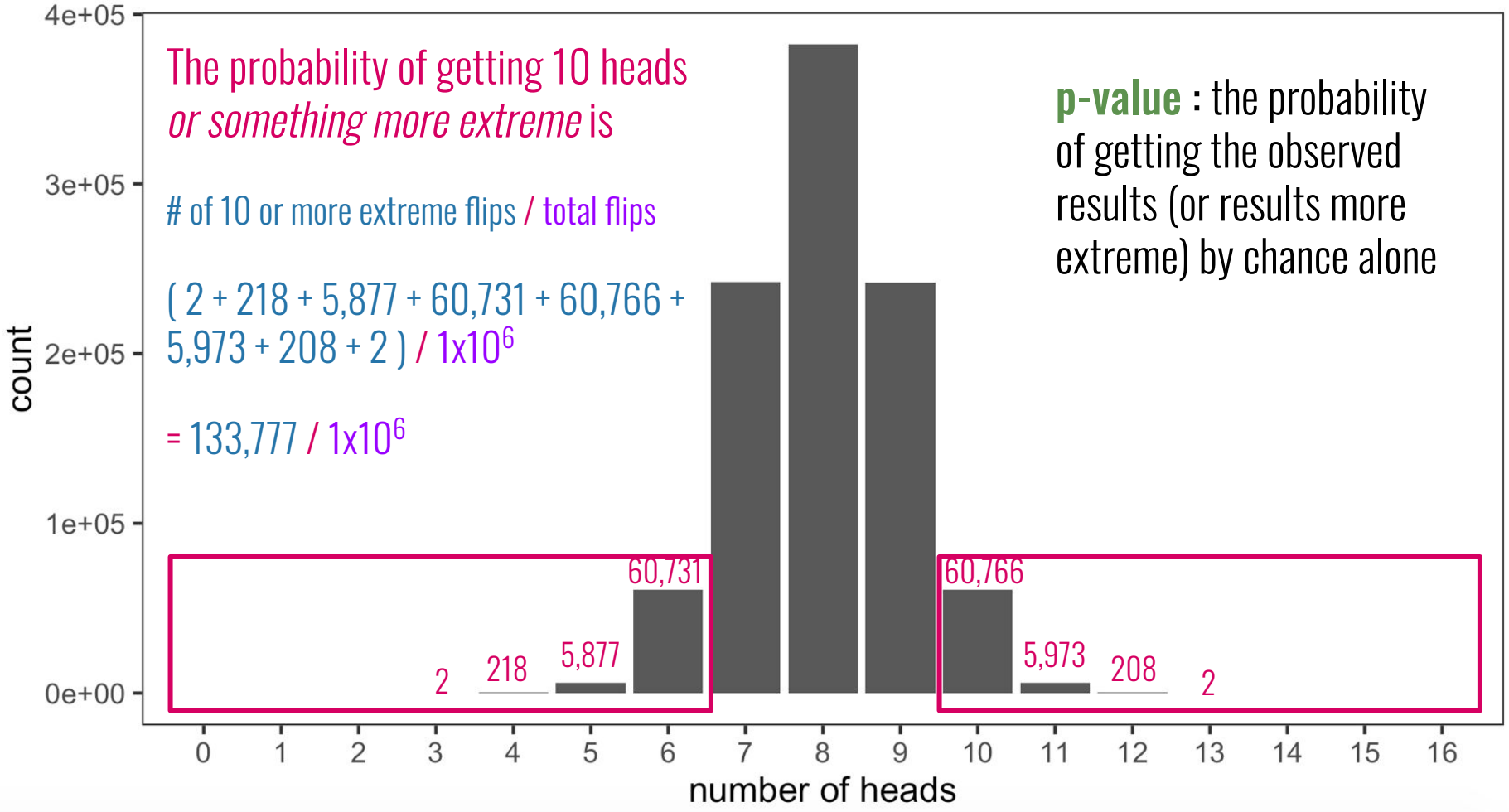
p-value : the probability of getting the observed results (or results more extreme) by chance alone

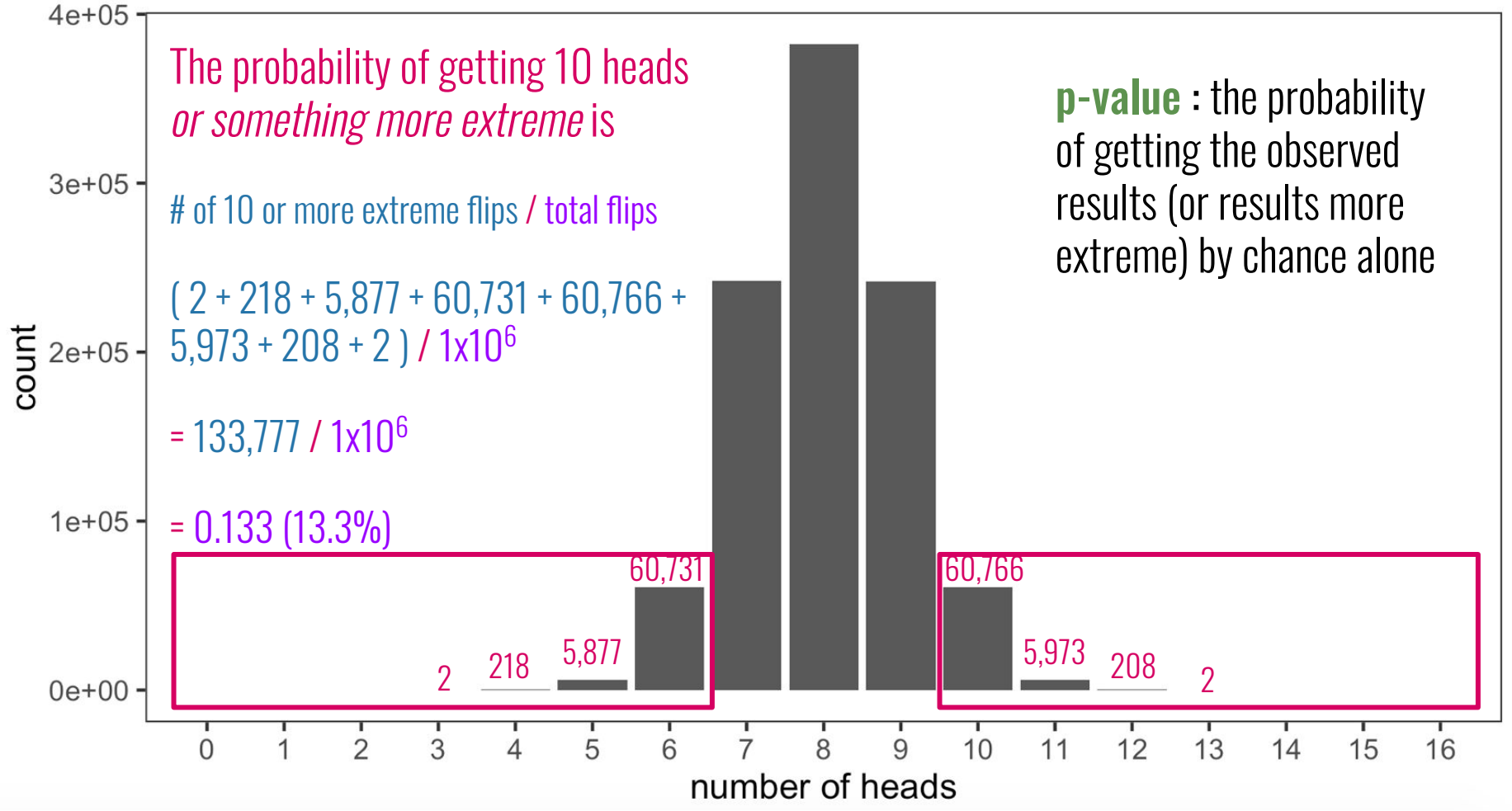

0.4
0.3
0.2
0.1
0.0
proportion
0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
number of heads
p-value : the probability of getting the observed results (or results more extreme) by chance alone
In your trial, you observe 10 heads.

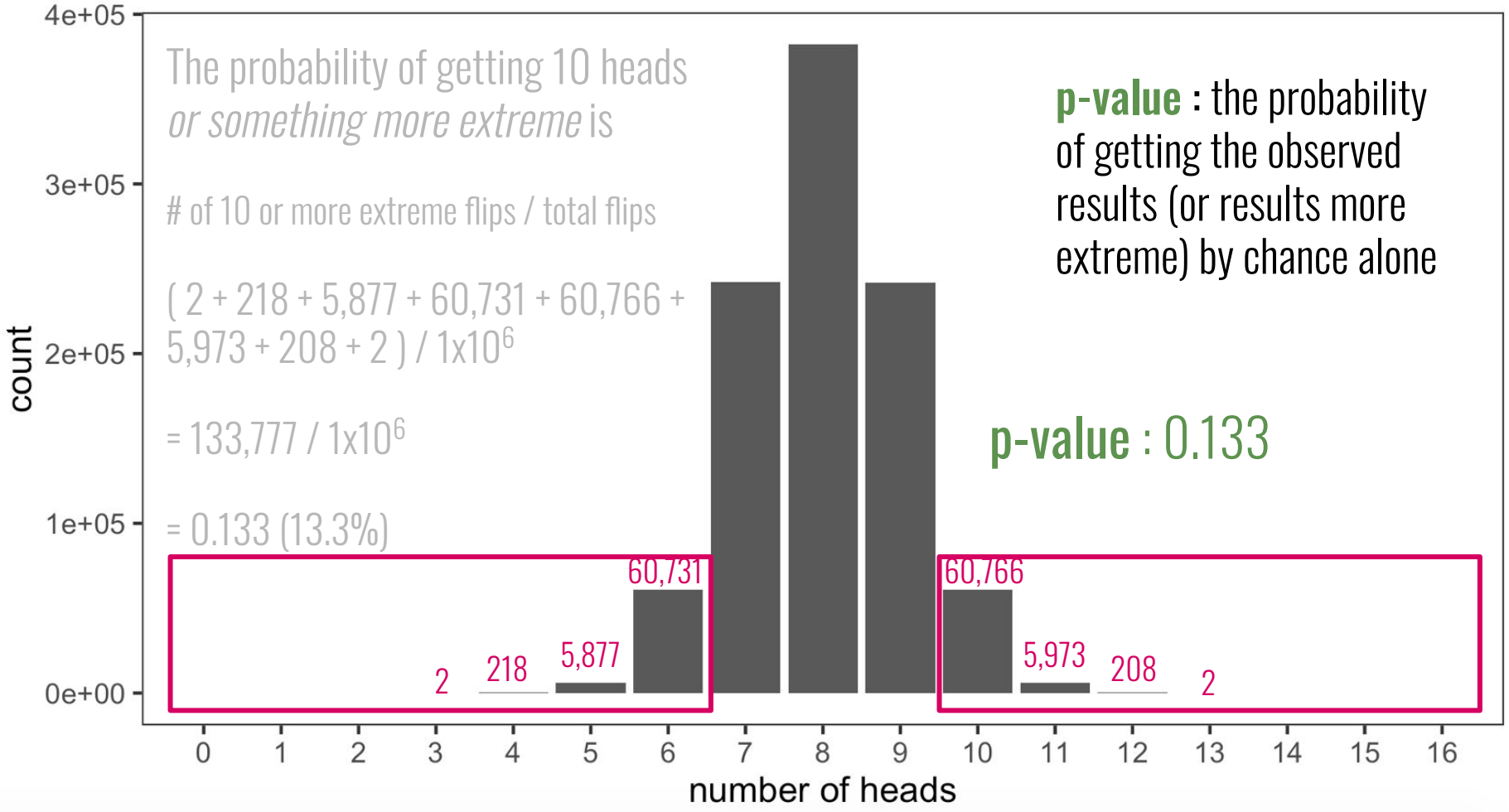

0.4
0.3
0.2
0.1
0.0
proportion
0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
number of heads
p-value : the probability of getting the observed results (or results more extreme) by chance alone
The results you saw (10 heads) *and* all results more extreme than what you saw are highlighted here.

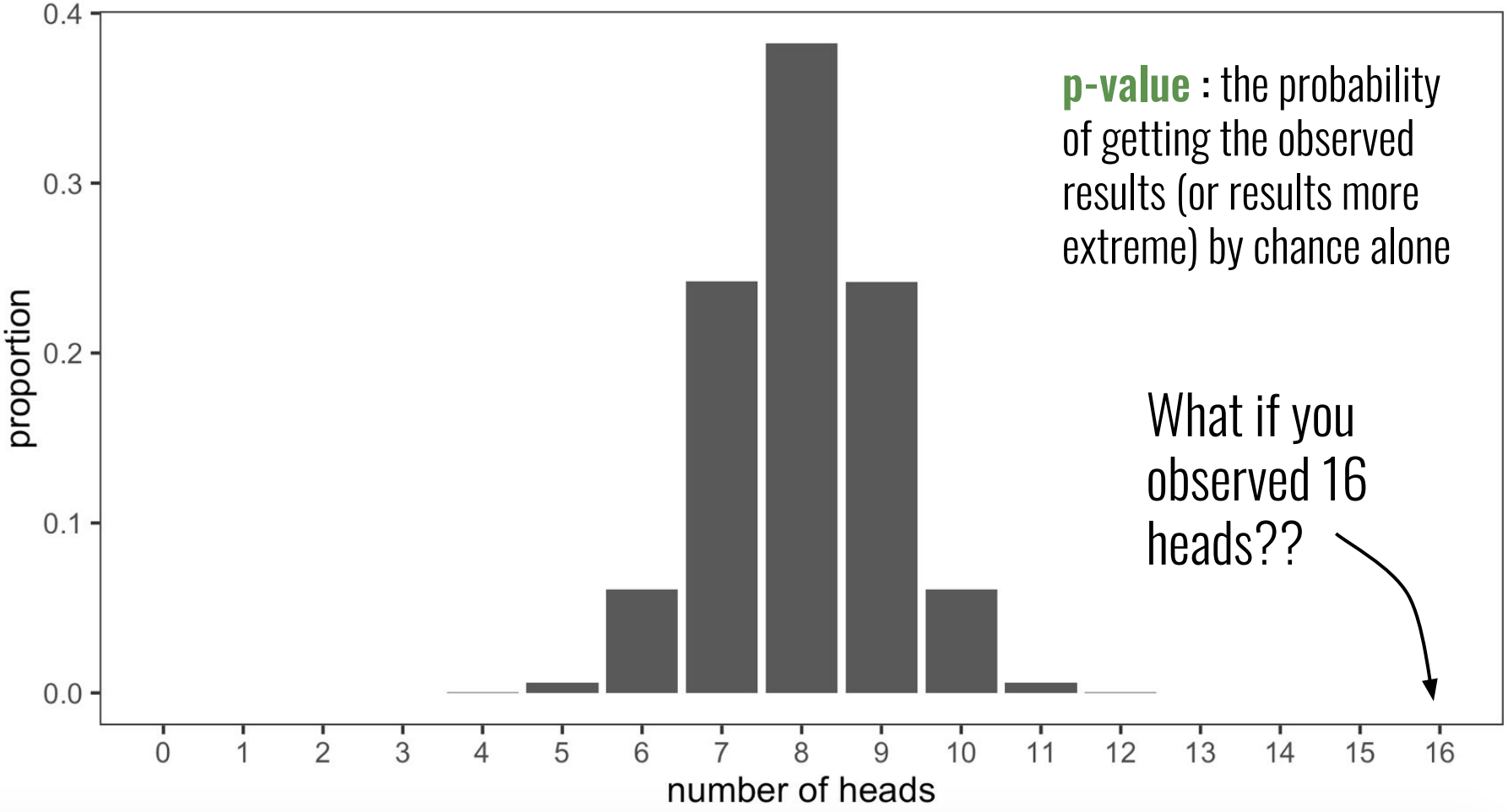

4e+05
3e+05
2e+05
1e+05
0e+00
count
The probability of getting 10 heads *or something more extreme* is calculated by adding the number of times these all occurred, divided by the total number of head flips
p-value : the probability of getting the observed results (or results more extreme) by chance alone
2
218
5,877
60,731
60,766
5,973
208
2
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
number of heads

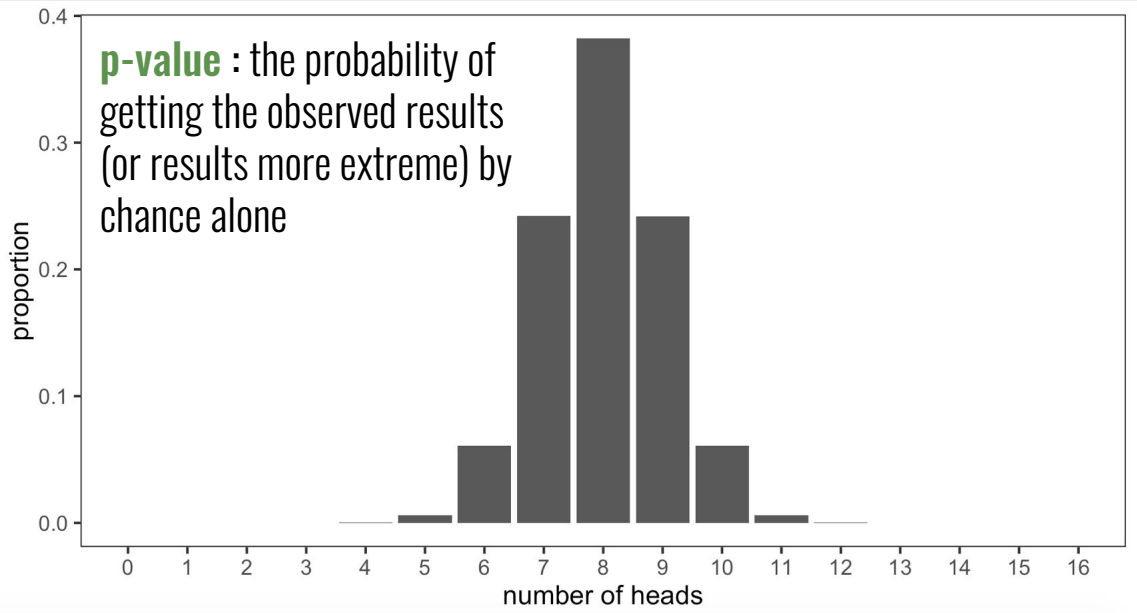

The probability of getting 10 heads
or something more extreme is
# of 10 or more extreme flips / total flips
p-value : the probability of getting the observed results (or results more extreme) by chance alone
count
4e+05
3e+05
2e+05
1e+05
0e+00
2
218
5,877
60,731
60,766
5,973
208
2
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
number of heads


The probability of getting 10 heads
or something more extreme is
# of 10 or more extreme flips / total flips
(2 + 218 + 5,877 + 60,731 + 60,766 + 5,973 + 208 + 2) / 1x10^6
= 133,777 / 1x10^6
p-value : the probability of getting the observed results (or results more extreme) by chance alone
count
4e+05
3e+05
2e+05
1e+05
0e+00
2
218
5,877
60,731
60,766
5,973
208
2
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
number of heads


The probability of getting 10 heads
or something more extreme is
# of 10 or more extreme flips / total flips
(2 + 218 + 5,877 + 60,731 + 60,766 + 5,973 + 208 + 2) / 1x10^6
= 133,777 / 1x10^6
= 0.133 (13.3%)
p-value : the probability of getting the observed results (or results more extreme) by chance alone
count
4e+05
3e+05
2e+05
1e+05
0e+00
2
218
5,877
60,731
60,766
5,973
208
2
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
number of heads


The probability of getting 10 heads
or something more extreme is
# of 10 or more extreme flips / total flips
(2 + 218 + 5,877 + 60,731 + 60,766 + 5,973 + 208 + 2) / 1x10^6
= 133,777 / 1x10^6
= 0.133 (13.3%)
p-value : the probability of getting the observed results (or results more extreme) by chance alone
p-value : 0.133
count
4e+05
3e+05
2e+05
1e+05
0e+00
2
218
5,877
60,731
60,766
5,973
208
2
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
number of heads

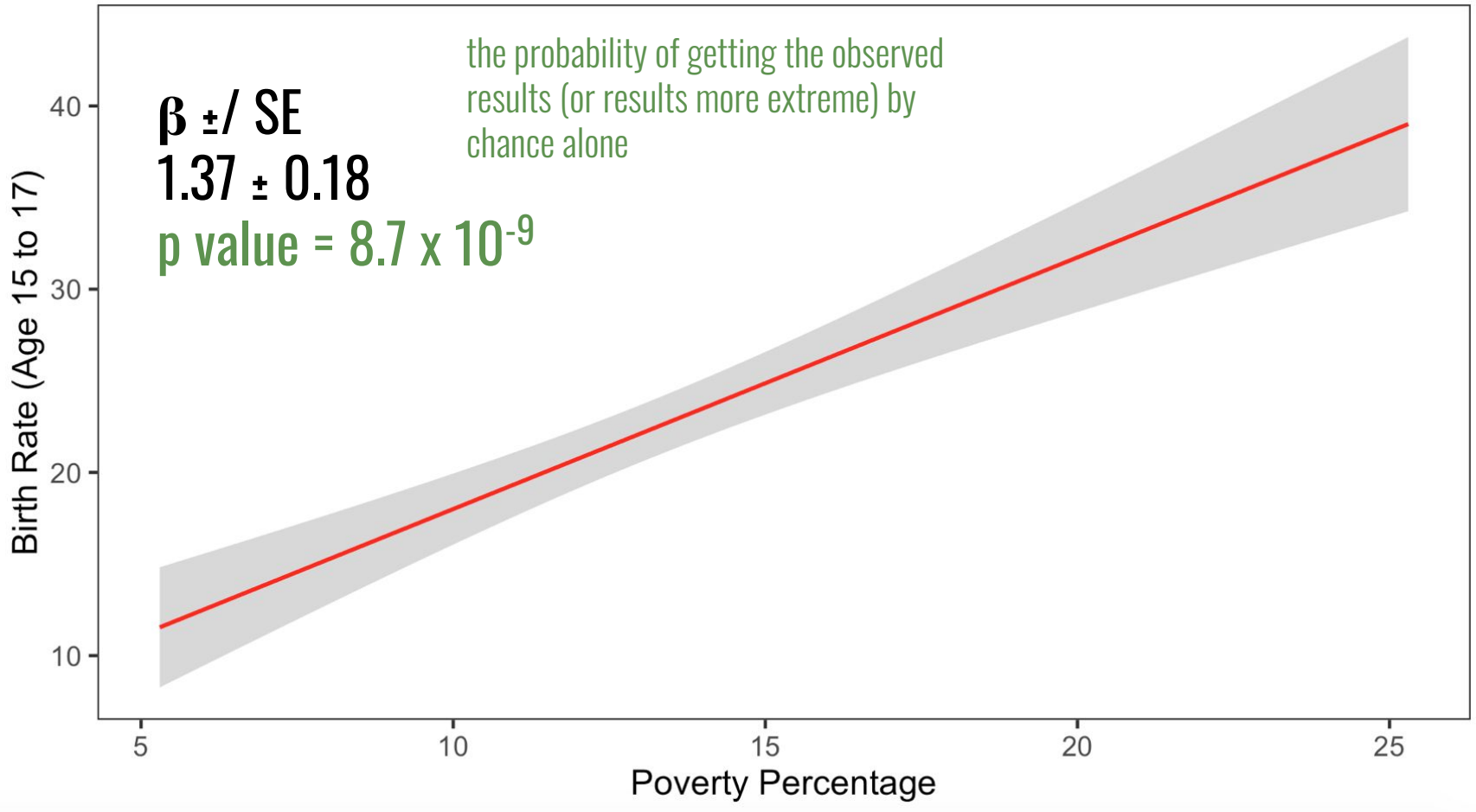

0.4
0.3
0.2
0.1
0.0
proportion
0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
number of heads
p-value : the probability of getting the observed results (or results more extreme) by chance alone
What if you observed 16 heads??



What would be the p-value of you flipping 16 heads?

A
< 0.13

B
> 0.13


β ±/ SE
1.37 ± 0.18
p value = 8.7 x 10-9
the probability of getting the observed results (or results more extreme) by chance alone
Birth Rate (Age 15 to 17)
40
30
20
10
5
10
15
20
25
Poverty Percentage

Takes into account the effect size (β) and the SE

p-value : the probability of getting the observed results (or results more extreme) by chance alone