

ADAPT Modeling Framework (AMF) Manual

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1. Setup and preparation

The framework can be installed by running the `setup` function in the AMF root directory. This will add the AMF package and ODEMEX toolbox to the MATLAB search path, allowing these to be used from any location, and will attempt to start a parallel pool to enable computation using multiple cores (see `help matlabpool`). Any sub-directories will also be included in the search path.

1.1 Required knowledge

Basic knowledge of MATLAB functions and data types is assumed. The following link explains the different data types supported by MATLAB:

http://nl.mathworks.com/help/matlab/data-types_data-types.html

While knowledge of object-oriented programming is not required for basic use, advanced configurations require some basic knowledge of how to use objects in MATLAB. Objects can be interpreted as structures with incorporated methods:

<http://nl.mathworks.com/company/newsletters/articles/introduction-to-object-oriented-programming-in-matlab.html>

Basic knowledge of the estimation of parameter trajectories using the ADAPT algorithm is required.¹ In addition, the examples used in this manual make use of the toy model developed by Natal van Riel et al.²

1.2 Preparing the ODEMEX toolbox

The AMF package uses the ODEMEX toolbox to enable MEX compilation for computational files in order to improve computation times. This toolbox requires configuration in order to be used. Instructions on how to configure the ODEMEX toolbox can be found in the **Instructions.pdf** file located in the **odemex** folder.

1.3 Setting up a new project

It is recommended to create a new directory for each new AMF project. A project generally contains the following files:

- A model function;
- A dataset function;
- A mat-file containing the experimental data values;
- A run file;
- Custom functions (optional).

It is recommended to use unique names for these files to prevent naming conflicts that may occur when adding multiple projects to the MATLAB search path.

2. Setting up the model

A dynamical model is defined in a model file. This file contains a single function that returns a structure containing the specification of all components that are included in the model. This structure contains the following fields:

DESCRIPTION	The model description.
PREDICTOR	Specification of the model predictor.
[CONSTANTS]	Specification of model constants (optional).
[INPUTS]	Specification of model inputs (optional).
PARAMETERS	Specification of model parameters.
STATES	Specification of model states.
[REACTIONS]	Specification of model reactions (optional).

Start by defining the model function and adding a description for the model.

```
% toyModel.m
function MODEL = toyModel()

MODEL.DESCRPTION = 'Toy model created by N.A.W van Riel.';
```

The remaining fields of the model structure are used to specify the model components. Components are grouped by type (i.e. predictor, constant, input, parameter, state and reaction) and are defined using cell matrices. Each type requires a single specification cell matrix of which one row defines a single model component. The columns of a specification matrix represent properties that can be used to customize components. While properties are specific to component types, the first and last property of components of all types correspond to the component name and the optional meta-data respectively.

Shared properties

name	char	Unique component identifier.
meta-data	cell (array)	Optional meta-data used for visualization of model results. meta-data should either be an empty cell array {} or an array containing the component's unit type, unit and plotting label: {'unitType' 'unit' 'label'}.

2.1 The model predictor

Properties

interval	double (vector)	Vector containing the start and end values of the (time) interval.
----------	-----------------	--------------------------------------------------------------------

The model predictor is used to define the independent variable of the model (usually time). The (time) interval defined is used for simulation and the computation of trajectories.

```
MODEL.PREDICTOR = {  
%   name   interval   meta-data  
    't'     [0 10]     {'time' 'days' 'Time'}  
};
```

2.2 Model constants

Properties

value	double OR char	Constant value (double) OR name of a data component (char).
-------	----------------	-------------------------------------------------------------

Model constants can be defined as static values by using a number for the `value` property. In addition, constant values can be obtained from the dataset by using the name of the data component for the `value` property.

```
MODEL.CONSTANTS = {  
%   name   value   meta-data  
    'mBW'  'BW'     {'mass'  'kg'  'body weight'}  
};
```

In this example, the mean body weight of the subject group is defined in the dataset as 'BW'. By using this syntax, the model constant 'mBW' obtains this value for use in the model ODE. The advantage of obtaining constant values from data is that these values are automatically updated when switching between datasets or subject groups.

2.3 Model inputs

Properties

type	char	Input type: 'data' for data inputs; 'function' for function inputs.
args	cell (array)	Array of input arguments.
method	char	Interpolation method: 'linear' for linear interpolation; 'spline' for cubic spline interpolation.

Dynamic model inputs can be obtained directly from data, or defined as a function of model parameters. Constant inputs are treated identical model constants, and should therefore be defined as model constants (2.2). The `method` property specifies the interpolation method to be used in the ODE solver.

2.3.1 Data inputs

For data inputs, `args` should contain a single element: the name of the data component.

```
MODEL.INPUTS = {  
%   name      type   args      method  meta-data  
    'Insulin' 'Data' {'Insulin'} 'Linear' {'conc.' 'uU/ml' 'Insulin'}  
};
```

In this example, the insulin concentration for the current subject group is obtained from the dataset to be used as a model input.

2.3.2 Function inputs

For function inputs, the first element of `args` should contain the time interval. Additional elements need to be added for each time point in this interval, containing the names of the model parameters that compose the dynamic input.

```
MODEL.INPUTS = {  
%   name  type      args      method  meta-data  
    'u1'  'Function' {[0 3 5 10], 'p1', 'p2', 'p3', 'p4'} 'Linear' {}  
};
```



```

MODEL.PARAMETERS = {
%   name fit value bnd meta-data
    'p1' 1   1   [] {}
    'p2' 1   1   [] {}
    'p3' 1   1   [] {}
    'p4' 1   1   [] {}
};

```

This example demonstrates the definition of a piece-wise linear interpolated input function composed of 4 model parameters that should be fitted when optimizing the model.

2.4 Model parameters

Properties

fit	double (bool)	Indicator for fitting: 1 for fit parameters; 0 for constant parameters.
value	double	Initial parameter value.
bnd	double	Lower and upper boundary of the estimated value. Will default to [0 inf] if left empty.

Model parameters can be defined as constant parameters, or parameters that should be fitted during model optimization using `fit`. The boundary conditions for parameter estimation are specified in the `bnd` property.

2.5 Model states

Properties

init	double	Initial state value.
ode	char	The ODE describing the state time derivative.

Model states define the initial model state, as well as the model ODE that describes the state time derivatives. The `ode` property contains the equation for the state time derivative (ODE), and specifies a function of other model components (constants, inputs, parameters, states and reactions).

```

MODEL.STATES = {
%   name init ode      meta-data
    's1' 0   'v1 - v3 - v4' {}
    's2' 0   '-v1 + v2'  {}
    's3' 0   'v1 - v2'   {}
    's4' 0   'v4 - v5'   {}
};

```

In this example, the state time derivatives are defined as functions of model reactions (fluxes in this case).

2.6 Model reactions

Properties

expr	char	The expression describing the reaction as a function of other components.
------	------	---------------------------------------------------------------------------

Model reactions are abstract model components that can represent any mathematical functions of other components (similar to state time derivatives). Generally, they are used to define intermediary component functions (i.e. fluxes or other physiological entities) which are in turn used to compose the model ODE (2.5).

```

MODEL.STATES = {
%   name init ode      meta-data
    's1' 0   'v1 - v3 - v4' {}
    's2' 0   '-v1 + v2'  {}
    's3' 0   'v1 - v2'   {}
    's4' 0   'v4 - v5'   {}
};

MODEL.REACTIONS = {
%   name expr      meta-data
    'v1' 'k1 * u1 * s2' {}
    'v2' 'k2 * u2 * s3' {}
    'v3' 'k3 * s1'      {}
    'v4' 'k4 * s1'      {}
    'v5' 'k5 * s4'      {}
};

```

In this example, reactions are used to define fluxes, which are in turn used to define the model ODE in the model states.

2.6.1 Using reactions to define model outputs

Model reactions can be used to define any function of model components, even if they are not used to compose the model ODE. This can be useful since the framework will automatically compute and visualize any defined reaction, providing an easy way to analyze desired model outputs.

```
MODEL.REACTIONS = {  
%   name  expr          meta-data  
    'v1'  'k1 * u1 * s2' {}  
    'v2'  'k2 * u2 * s3' {}  
    'v3'  'k3 * s1'      {}  
    'v4'  'k4 * s1'      {}  
    'v5'  'k5 * s4'      {}  
  
    'y1'  'v1 + v2'      {}  
    'y2'  's1 * 10^6'    {}  
};
```

In this example, 2 model outputs are defined as additional model reactions. One computes the sum of fluxes v1 and v2, and the other performs a unit conversion on state s1.

2.6.2 Conditional if-statements

The use of conditional if-statements is supported in reaction expressions using a specific syntax and is compatible with MEX compilation.

```
MODEL.REACTIONS = {  
%   name  expr          meta-data  
    'posG' 'if((G > 0), G, 0)' {} % single condition  
    'posS' 'if((G > 0) && (S > 0), 1, 0)' {} % multiple conditions  
};
```

In this example, S and G represent other model components (i.e. states). Reaction posG will have the value of G if $G > 0$, and 0 otherwise. Reaction posS will have a value of 1 if both $G > 0$ and $S > 0$, and 0 otherwise.

2.7 Restrictions

Several restrictions apply to the definition of model components:

- **All component names must be unique, even for components of different types;**
- **Only reaction expressions can contain conditional if-statements (2.6.2).**

To ensure compatibility with MEX compilation, several additional restrictions apply to component functions in reaction expressions (2.5) and state time derivatives (2.5):

- **MATLAB functions cannot be used in component functions;**
- **Powers should be defined using `pow(A,B)` or `A^B`. Exponent notation (i.e. `1e6`) is not allowed;**

If these last conditions are not met, computational algorithms can still be executed without the optimized performance provided by MEX compilation.

2. Preparing experimental data

Experimental data has to be provided using a nested data structure that is restricted to a specific format. This structure needs to be prepared and saved only once, before defining the dataset.

On the first level, the data structure contains the names of the separate subject groups (group names can be chosen arbitrarily). The second level contains the measurement times, means and standard deviations of the data fields (i.e. metabolite concentrations). The data structure used in the following examples represents a dataset of two subject groups `toy` and `toy2` containing the measured means and standard deviations of metabolite concentrations `s1 s2 s3 s4`.

```
data =  
  
    toy: [1x1 struct]  
    toy2: [1x1 struct]  
  
data.toy =  
  
    t: [5x1 double]  
    s1_mean: [5x1 double]  
    s1_std: [5x1 double]  
    s2_mean: [5x1 double]  
    s2_std: [5x1 double]  
    s3_mean: [5x1 double]  
    s3_std: [5x1 double]  
    s4_mean: [5x1 double]  
    s4_std: [5x1 double]
```

The measurement times for all measured metabolites must be included in the dataset. In this case, all measurements were done on the same time interval τ . If data of multiple subject groups is available (as is the case here) the data field names must be identical between groups: `toy2` must have the same field names for the measurement times, means and standard deviations of `s1 s2 s3` and `s4`. Note that the data values do not have to be identical: these generally depend on the experiment and may be different between subject groups.

Once the data structure has been created, it should be saved in the project root directory.

```
save('toyData.mat', '-struct', 'data');
```

3. Setting up the dataset

A dataset is defined in a dataset function. This function returns a structure containing the data specification (similar to the definition of models). This structure contains the following fields:

DESCRIPTION	The dataset description.
FILE	The name of the MAT file to which the experimental data structure is saved.
GROUPS	Subject group names.
FIELDS	Data fields.

Start by defining the dataset function and adding a description for the dataset.

```
% toyData.m
function DATASET = toyData()

DATASET.DESCRPTION = 'Toy test data.';

DATASET.FILE = 'toyData'; % toyData.mat
```

This dataset parses the data structure located in 'toyData.mat'.

3.1 Groups

The GROUPS field specifies the names of the subject groups that may be used for model optimization. All of the specified subject groups must be available in the specified data structure.

```
DATASET.GROUPS = {
    'toy'
    'toy2'
};
```

3.2 Data fields

Properties

name	char	Field name.
obs	double (bool)	Observable indicator. 1 for observables; 0 for regular data.
timeField	char	Name of the corresponding time field in the data structure.
meanField	char	Name of the corresponding mean value field in the data structure.
stdField	char	Name of the corresponding standard deviation field in the data structure.
unitConv	double	Unit conversion factor.
smooth	double	Smoothing parameter for the generation of random cubic smoothing splines (see <code>help csaps</code> for information on how this parameter affects the spline).

Data fields can be defined to parse the experimental data values located in the supplied data structure. The `obs` property specifies whether or not the data should be considered observable. Observable data fields must have a name equal to the corresponding model state or reaction, and are automatically used to compute the model error during model optimization. The `timeField`, `meanField` and `stdField` specify the names of the corresponding fields in the data structure. Note that if the data field contains a single value (static data), the `timeField` property is not required and should be empty `[]`.

```
DATASET.FIELDS = {  
%   name obs timeField meanField stdField unitConv smooth  
    's1' 1   't'       's1_mean' 's1_std' 1      []  
    's2' 1   't'       's2_mean' 's2_std' 1      []  
    's3' 1   't'       's3_mean' 's3_std' 1      []  
    's4' 1   't'       's4_mean' 's4_std' 1      []  
};
```

Following the previous examples, the values for data fields `s1` `s2` `s3` `s4` are loaded from ‘`toyData.mat`’ upon loading a subject group (i.e. `toy`). In this dataset, data is available for all model states (2.5), therefore all defined data fields are observable.

Unit conversions can be specified using the `unitConv` property. Data values will be multiplied by this factor upon loading. In addition, the smoothing parameter for the generation of random cubic smoothing splines (i.e. for the ADAPT algorithm) can be specified using the `smooth` property.

4. Setting up the run file

Once the model and dataset are defined, the model and dataset objects need to be created and configured in order to perform computational algorithms (i.e. model simulation, optimization or calculation of parameter trajectories using ADAPT). In order to provide a clear workflow, it is recommended to centralize these operations in a single run file for each separate task.

Start by importing the AMF package for easy access to its classes and methods.

```
% runToy.m  
import AMF.*
```

4.1 Creating the model and dataset objects

The model and dataset objects can be created directly from their respective specification files.

```
model = Model('toyModel'); % toyModel.m  
data = DataSet('toyData'); % toyData.m
```

4.2 Coupling the dataset to the model

Data values need to be loaded by loading a subject group. If no group is loaded explicitly, the first defined subject group is loaded automatically. Therefore, explicit loading of a subject group is not required if only one group is defined. The dataset is then ready to be coupled to the model.

```
loadGroup(data, 'toy');  
initiateExperiment(model, data);
```

4.3 Configuring the model

The model can be configured by customizing the model options. These options control which files should be compiled and serve as parameters for computational algorithms. An overview of available model options is provided in chapter 5.


```

model.options.useMex      = 1;
model.options.odeTol      = [1e-12 1e-12 100];
model.options.numIter     = 50;
model.options.numTimeSteps = 100;
model.options.parScale    = [2 -2];
model.options.seed        = 1;
model.options.SSTime      = 1000;
model.options.lab1        = .1;

```

This example configures the model for the execution of the ADAPT algorithm to compute 50 trajectories over 100 time steps, with MEX compilation enabled to drastically improve computation times.

The model needs to be parsed to resolve all interactions and dependencies between data and model components and compiled to generate the necessary computation files.

```

parseAll(model);
compileAll(model);

```

4.4 Computation

Once the model is configured, computational algorithms can be performed. In the previous examples, the model was set up for the ADAPT algorithm, which can now be executed.

```

result = runADAPT(model);

```

The `runADAPT` method executes the ADAPT algorithm and returns a result object containing the computed trajectories and corresponding model errors.

Alternatively, this segment of the run file can contain other algorithms. The AMF package currently supports the following algorithms:

simulate	Simulate the model by computing the states (and all other components) for the time range of the current predictor.
fit	Fit the model using dataset and simulate the model using the optimized parameters.
runADAPT	Run ADAPT on the model to compute possible parameter trajectories.

4.5 Results analysis

Once the computational algorithm has been executed, the returned result object can be used to visualize the computed trajectories.

```
plotAll(result, 'parameters', 'traj');  
plotAll(result, 'states', 'traj');
```

In this example, we plot the estimated parameter trajectories as well as the state trajectories. This will output 2 figures. Note that the meta-data provided to model components is automatically used for the visualization of results. In addition, any observable model component will automatically include its data (mean and standard deviations).

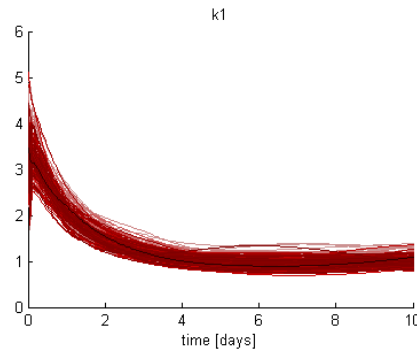


FIGURE 1: ESTIMATED PARAMETER TRAJECTORIES

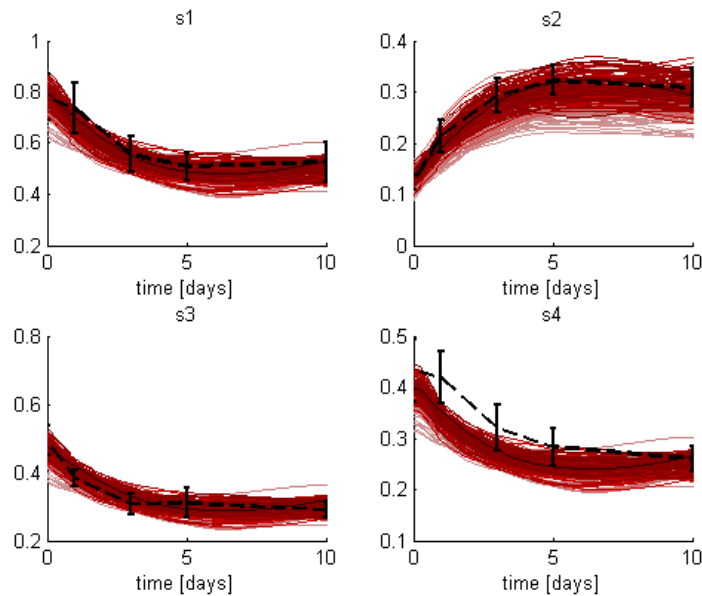


FIGURE 2: ESTIMATED STATE TRAJECTORIES

5. Model options

Several options for computational algorithms can be configured on the model:

General options

optimset	struct	Optimization OPTIONS structure used by the optimization algorithm (<code>lsqnonlin</code>). See <code>help optimset</code> for more information.
useMex	double (bool)	Indicator that specifies whether or not the MEX compilation should be used to improve computation times (recommended).
timeSteps	double	The number of time steps used for simulation or trajectory estimation (ADAPT).

ADAPT options

parScale	double	2-element vector containing the upper and lower boundaries for the generation of random parameters during the ADAPT algorithm.
numIter	double	The number of iterations (trajectories) to be calculated during the ADAPT algorithm.
lab1	double	The regularization factor used during the ADAPT algorithm.
seed	double	The initial random seed (can be any arbitrary number). Using the same initial random seed will always generate identical trajectories during the ADAPT algorithm. Note that the generation of identical trajectories fails when parallel computing is enabled (parallel computing causes trajectory calculations in random order).
sSTime	double	The time used to fit the initial steady state. The specified value for <code>sSTime</code> will be prefixed to the current time vector prior to fitting the initial time step.
savePrefix	Char	A string that is used as prefix when saving model results. This option is used to prevent the automatic overwriting of result files.

Note that since the model options are stored in a dynamic structure, any custom options can be defined for use in custom regularization functions (chapter 6). For example, a custom regularization function might require additional regularization factors:

```
model.options.labC = [.1 .01 .01];
```

6. Advanced configuration

Advanced configurations can be achieved by customizing several functions that are used during the execution of computational algorithms. However, using custom functions requires some knowledge of the internal workings of the framework, in particular of how model component and data field objects can be accessed to obtain their computed values.

6.1 Accessing model components

Once a model object is created from a specification file (4.1), there are several interfaces available on the object to access the individual components.

6.1.1 By reference

A model object has a `ref` property that contains a structure in which references to all component objects are stored by name. Following the previous examples, state `s1` can be accessed using this structure.

```
model.ref.s1
```

```
ans =
```

```
AMF.ModelState handle
Package: AMF

Properties:
  derivedODE: []
  compiledODE: []
    index: 1
    name: 's1'
    expr: 'v1 - v3 - v4'
    data: [1x1 AMF.DataField]
    time: []
    init: 0
    prev: 0
    curr: 0
    val: []
  unitType: []
    unit: []
    label: []
```

While the properties of the component objects are different for each type, all components have identical properties for storing computed values, which can be used to create alternative error and regularization functions (6.3-6.5):

Component object properties that store computed values

init	The initial value.
curr	The current value. This value updates after fitting each time step during ADAPT.
prev	The previous value. Equals curr of the previous time step.
val	Values of the resulting trajectory.
data	Only used for observable components: contains a reference to the corresponding data object.

6.1.2 By type

Additionally, components are grouped by type and stored in properties of the model object as arrays. The following component arrays are available.

Model properties containing component arrays

constants	Model constants.
inputs	Model inputs.
parameters	Model parameters.
fitParameters	Fit parameters (subset of parameters).
states	Model states.

reactions	Model reactions.
-----------	------------------

These component arrays can be used to access multiple values simultaneously. For example, a single statement can retrieve the current values for parameters:

```
pcurr = [model.parameters.curr]
```

```
pcurr =  
1.0000    1.0000    0.1000    0.5000    1.0000
```

6.2 Accessing observable data

For observable model components, the data property contains a reference to the corresponding data object (6.1).

```
s1 = model.ref.s1;  
s1.data
```

```
ans =  
  
AMF.DataField handle  
Package: AMF  
  
Properties:  
    name: 's1'  
    obs: 1  
    index: 1  
timeField: 't'  
valField: 's1_mean'  
stdField: 's1_std'  
unitConv: 1  
    smooth: []  
    source: [1x1 struct]  
        time: [5x1 double]  
        val: [5x1 double]  
        std: [5x1 double]  
    options: []  
    fitIdx: [5x1 double]
```

The following properties of a data object contain computed values.

Data object properties that store computed values

time	Time interval used for interpolation.
val	Interpolated values.
std	Interpolated standard deviations.
source.time	Measurement time of the experimental data values.
source.val	Measured experimental values.
source.std	Measured experimental standard deviations.
fitIdx	The indices of the source.time locations in the complete fit time interval.

For regular model optimization, the framework simulates the model only on the time points for which observable data is available. Since different observables can have different measurement times, the indices of the bigger fit time interval that correspond to the measurement times are stored in the `fitIdx` property.

6.3 Customizable functions

The functions that are used for computational tasks are stored in the `functions` property of the model object. By default, this property contains a structure with function handles to the relevant functions.

```
model.functions
```

```
ans =
```

```
ODE: @C_toyModel_ODE
ODEMex: @C_toyModel_ODEMEX
ODEC: @C_toyModel_ODEC
```

```

reactions: @C_toyModel_REACTIONS
inputs: @C_toyModel_INPUTS
reg: @AMF.regFun
err: @AMF.errFun
errStep: @AMF.errFunStep

```

To realize advanced configurations for computational algorithms, these functions are fully customizable and can be replaced with alternative custom functions in the run file. However, it is advisable to only change the functions that are not automatically generated when compiling the model.

Compiled model functions

ODE	The compiled ODE function used by the solver algorithm to compute the dynamic model states.
ODEMex	The compiled function that is used as input to the ODEMEX toolbox in order to compile the MEX function (this function contains a syntax specific to the toolbox and cannot be run directly).
ODEC	The compiled MEX ODE function. This function will only be compiled when MEX compilation is enabled in the model options (<code>useMex</code>).
reactions	The reactions function that computes the dynamic reactions for any given time.
inputs	The inputs function that computes (interpolates) the dynamic inputs for any given time.

Customizable model functions

reg	The regularization function. This function is used for ADAPT regularization, but can be used to define any additional model errors (penalties) that should be considered during optimization.
err	The error function used for 'regular' fitting in the objective function to compute the error of observable model components.
errStep	The error function used for fitting a single time step in the objective function to compute the error of observable model components (used for parameter estimation in each time step by the ADAPT algorithm).

6.4 Error functions

Two separate error functions are used for the computation of model errors: a regular error function used in regular optimization algorithms, and a step error function that calculates the model error in a single time step, used in ADAPT. During optimization, error functions are called on each individual observable model component.

6.4.1 Regular error function

The default regular error function is `AMF.errFun`. This function calculates the error of a single observable component, weighted by the standard deviation of the data. During regular optimization, the `curr` property of model components is a vector that contains the computed values that correspond to the fit time interval. The `fitIdx` property of the data object is used to retrieve only the simulated values that correspond to the data measurement times.

```
% AMF.errFun
function err = errFun(comp)

idx = comp.data.fitIdx;
err = (comp.data.source.val(:)-comp.curr(idx))./comp.data.source.std(:);
```

Any custom error function must return an error vector. For example, consider an error function `customErrFun` that does not incorporate weighing using the standard deviation of the data.

```
% customErrFun.m
% un-weighted error
function err = customErrFun(comp)

idx = comp.data.fitIdx;
err = comp.data.source.val(:)-comp.curr(idx);
```

To use this custom error function instead of the default, assign it to the model.

```
model.functions.err = @customErrFun;
```

6.4.2 Step error function (ADAPT)

The default step error function is `AMF.errFunStep`. This function calculates the error of an observable component in a single time step. During ADAPT, the `curr` and `prev` properties of model components contain a single value corresponding to the current and previous time step.

```
% AMF.errFunStep
function err = errFunStep(comp, ts)

err = (comp.data.val(ts)-comp.curr)./comp.data.std(ts);
```

The `ts` argument corresponds to the index of the current time step, and is used to obtain the current interpolated data value. Similar to 6.2.1, a custom function can be used by assigning one to the model.

```
model.functions.errStep = @customErrFunStep;
```

6.5 Regularization

The regularization function is used to define any additional errors that should be considered during model optimization. The complete model object is passed to this function, allowing the use of any model or data components for the computation of errors. Model components can be accessed using the methods described in 6.1. Data components can be accessed by using the `dataset` model property, which contains a reference to the current dataset.

```
model.dataset
```

```
ans =
```

```
AMF.DataSet handle
Package: AMF

Properties:
    name: 'toyData'
  description: 'Toy test data.'
specification: [1x1 struct]
      data: [1x1 struct]
    groups: {'toy'}
activeGroup: 'toy'
      fields: [1x4 AMF.DataField]
    functions: []
        ref: [1x1 struct]
        list: {4x1 cell}
```

A dataset object contains a `ref` property that can be used to access individual data objects, similar to the `ref` property of the model. Generally, only observable data is used which can be accessed directly from the observable model components (6.2).

6.5.1 Defining additional penalties

The regularization function can be used during regular optimization to define additional errors or penalties. For example, if the AUC of a metabolite concentration is to be remained constant, a penalty can be defined in a custom regularization function:

```
% minGlucReg.m
% Regularization function of the minimal
% glucose model by Dalla Man et al.
function E = minGlucReg(model)

Ra = model.ref.Ra_g;
Gtot = model.ref.Gtot;

E = AUC(Ra) - Gtot.val;
```

In this example, total glucose intake `Gtot` (grams) is a model constant and is believed to be equal to the area under the curve (AUC) of the glucose rate of appearance in grams `Ra_g`. The AUC of `Ra_g` is approximated using cumulative trapezoidal numerical integration:

```
% AUC.m
% Approximates the area under curve (AUC)
% using cumulative trapezoidal numerical
% integration.
function val = AUC(comp)

tmp = cumtrapz(comp.time, comp.curr);
val = tmp(end);
```

To use this regularization function, it needs to be assigned to the model.

```
model.functions.reg = @minGlucReg;
```

6.5.2 ADAPT regularization

When executing the ADAPT algorithm, a default regularization function is used that penalizes erratic changes in parameter values, controlled by model option `lab1`:

```
% AMF.regFun
function reg = regFun(model)

t = getTime(model);
p = model.fitParameters;

lab1 = model.options.lab1;

dt = t(end) - t(1);

if t(end) == 0
    reg = 0;
else
    reg = ([p.curr] - [p.prev]) ./ [p.init] ./ dt * lab1;
end
```

As seen in the default regularization function, any of the model object functions and properties can be used to compute additional errors. This allows for the creation of complex custom regularization functions that use any model or data components.

Note that if a custom regularization function is assigned to the model, this overwrites the default ADAPT regularization function. If standard ADAPT regularization is required, it is advisable to copy `AMF.regFun` to the project directory and extend it with additional regularization terms.

7. Saving and loading results

After running the ADAPT algorithm on the model, the resulting trajectories are automatically saved in the 'results' sub-directory of the project root. Results are saved in the following format:

```
{options.savePrefix}_{name}_{options.numIter}_{options.numTimeSteps}.mat
```

Note that `options.savePrefix` should be set in the run file to prevent overwriting of existing result files (a suggestion would be to use the current date as prefix). An example results file might look like this:

```
13112015_toyModel_100_50.mat
```

For other computational algorithms, results can be saved manually:

```
% fit the model
fit(model);

% save result structure in the results directory
saveResult(model);
```

7.1 Loading results

Previously saved results can be loaded into a model result object.

```
resultStruct = load('13112015_toyModel_100_50.mat');

% create the ModelResult object
result = AMF.ModelResult(resultStruct);
```

After the results are loaded in the model result object, it can be used to visualize trajectories. Several options for visualization include:

```
% parameter trajectories
plotAll(result, 'parameters', 'traj');

% parameter trajectory histogram
plotAll(result, 'parameters', 'hist');

% state trajectories
plotAll(result, 'states', 'traj');
```

8. References

1. Tiemann, C. A. *et al.* Parameter Trajectory Analysis to Identify Treatment Effects of Pharmacological Interventions. *PLoS Comput Biol* **9**, e1003166 (2013).
2. Riel, N. A. W. van, Tiemann, C. A., Vanlier, J. & Hilbers, P. A. J. Applications of analysis of dynamic adaptations in parameter trajectories. *Interface Focus* **3**, 20120084 (2013).