

前面4个月， 目标: single variable
calculus, multivariable calculus,
linear algebra for economics and
engineering

1007 single variable calculus

Course Contents – List of Topics:

Review of Basic Concepts
Function Notation
Parent Functions and Transformations
Domain and Range
Trigonometry
Inverse Trigonometric Functions
Log Laws
Piecewise Functions
Odd and Even Functions
Limit Notation & Graphical Representations
Evaluating Limit Expressions Using Limit Laws
Continuity and Intermediate Value Theorem
Limits Involving Squeeze Theorem
Limits Involving Infinity
Instantaneous Rates of Change & Average Rate of Change
Derivative Definition
Derivatives Rules using Constant Rule, Power Rule, and Sum Rule
Derivatives Rules using Product Rule, Quotient Rule, and Chain Rule
Derivatives of Trigonometric Functions, Exponential Functions, and Inverse Functions
Implicit Differentiation
Logarithmic Differentiation
Linearization
Critical Points
Absolute and Local Extrema
First Derivative Test
Concavity & Inflection Points
Second Derivative Test
Curve Sketching
L'Hopitals Rule ($\frac{0}{0}$ and $\frac{\infty}{\infty}$)
L'Hopitals Rule (1^∞ and $(\infty)^0$ and 0^0)
Antiderivatives
Definite and Indefinite Integrals
Fundamental Theorem of Calculus
Area Under Curves & Area Contained Between Curves

single variable calculus (2007)

Topics

Indeterminate Forms and L'Hôpital's rule (Section 4.4)
The Substitution Rule (Section 5.5)
Integration by Parts (Section 7.1)
Trigonometric Integrals (Section 7.2)
Trigonometric Substitution (Section 7.3)
Integration of Rational Functions by Partial Fractions (Section 7.4)
Improper Integrals (Section 7.8)
Curves Defined by Parametric Equations (Section 10.1)
Calculus with Parametric Curves (Section 10.2)

Polar Coordinates (Section 10.3)
Calculus in Polar Coordinates (Section 10.4)
Sequences (Section 11.1)
Series (Section 11.2)
The Integral Test and Estimates of Sums (Section 11.3)
The Comparison Tests (Section 11.4)
Alternating Series and Absolute Convergence (Section 11.5)
The Ratio and Root Tests (Section 11.6)
Power Series (Section 11.8)
Representations of Functions as Power Series (Section 11.9)
Taylor and Maclaurin Series (Section 11.10)

linear algebra 2107

| week # | DATES | TESTS | SECTIONS | TOPICS |
|--------|-------|-------|---------------------|--|
| 1 | | | 1-3 | |
| 2 | | | 4.1 | Vector Spaces and Subspaces. |
| 3 | | | 4.2, 4.3 | Null Spaces, Column Spaces, Row Space and Linear Transformations. Linearly Independent Sets, Bases. |
| 4 | | | 4.4, 4.5 | Coordinate Systems. The Dimension of a Vector Space. |
| 5 | | | 4.5, 4.6 | Rank. Change of Basis. |
| 6 | | | 5.1, 5.2 | Eigenvectors and Eigenvalues. The Characteristic Equation. |
| 7 | | | 5.3, 5.4 | Diagonalization. Eigenvectors and Linear Transformations. |
| 8 | | | 5.5 | Complex Eigenvalues. |
| | | | | |
| 9 | | | 6.1, 6.2 | Inner Product, Length and Orthogonality. Orthogonal Sets. |
| 10 | | | 6.3, 6.4 | Orthogonal Projections. The Gram-Schmidt Process. |
| 11 | | | 6.5, 6.6 | Least-Squares Problems. Least-Squares Lines. Least-Squares Fitting of Other Curves. |
| 12 | | | 6.7 | Inner product Spaces. |
| 13 | | | 7.1, 7.2 | Diagonalization of Symmetric Matrices. The Spectral Theorem for Symmetric Matrices. Quadratic Forms. |
| 14 | | | 7.2 (cont.), 7.3 | The Principal Axes Theorem. Constrained Optimization. |

The above weekly schedule is subject to change depending on the progress of the course.

multi variable calculus (2008)

Topics:

12.1 Three-Dimensional Coordinate Systems

12.2 Vectors

12.3 The Dot Product

12.4 The Cross Product

12.5 Equations of Lines and planes

12.6 Cylinders and Quadric Surfaces

13.1 Vector Functions and Space Curves

13.2 Derivatives and Integrals of Vector Functions

13.3 Arc Length and Curvature

13.4 Motion in Space: Velocity and Acceleration

14.1 Functions of Several Variables

14.2 Limits and Continuity

14.3 Partial Derivatives

14.4 Linear Approximations

14.5 The Chain Rule

14.6 Directional Derivatives and the Gradient Vector

14.7 Maximum and Minimum Values

14.8 Lagrange Multipliers

15.1 Double Integrals over Rectangles

15.2 Double Integrals over General Regions

15.3 Double Integrals in Polar Coordinates

15.4 Applications of Double Integrals

15.6 Triple Integrals

15.7 Triple Integrals in Cylindrical Coordinates

15.8 Triple Integrals in Spherical Coordinates

15.9 Change of Variables

16.1 Vector Fields

16.2 Line Integrals

16.3 Fundamental Theorem for Line Integrals

16.4 Green's Theorem

Tentative Lecture Schedule

| Week | Dates | Sections |
|------|------------------|---------------------|
| 0 | Sept. 8 | 12.1, 12.2 |
| 1 | Sept. 13 - 15 | 12.3, 12.4 |
| 2 | Sept. 20 - 22 | 12.5, 12.6 |
| 3 | Sept. 27 - 29 | 13.1, 13.2 |
| 4 | Oct. 4 - 6 | 13.3, 13.4 |
| 5 | Oct. 13 | 14.1, 14.2 |
| 6 | Oct. 18 - 20 | 14.3, 14.4 |
| | | Reading week |
| 7 | Nov. 1 - 3 | 14.5, 14.6 |
| 8 | Nov. 8 - 10 | 14.7, 14.8 |
| 9 | Nov. 12 - 16 | 15.1, 15.2, 15.3 |
| 10 | Nov. 15 - 17 | 15.4, 15.6 |
| 11 | Nov. 22 - 24 | 15.7, 15.8 |
| 12 | Nov. 29 - Dec. 1 | 15.9, 16.1 |
| 13 | Dec. 6 - 8 | 16.2, 16.3 |
| 14 | Dec. 10 | 16.4 |

后面4个月:

1152 的 1, 2, 3.1-3.4, 4.1.1,
4.1.2

2152 的 4, 3.5 , 5

以及 2000 multivariable
calculus

mathematical analysis 1052-2052

| week # | DATES | TESTS | book ch. | TOPICS |
|--------|-------|-------|-----------|--------|
| 1 | | | 3-5 | |
| 2 | | | 7-9 | |
| 3 | | | 9-10 | |
| 4 | | | 11 14 | |
| 5 | | | 17-18 | |
| 6 | | | 19-20 | |
| 7 | | | 28-29 | |
| 8 | | | 30 | |
| 9 | | | 32 33 | |
| 10 | | | 34 36 | |
| 11 | | | 15 23 | |
| 12 | | | 37 24 | |
| 13 | | | 25 26 | |
| 14 | | | 31 | |

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multivariable calculus 2000

| week # | DATES | TESTS | lectures | TOPICS |
|--------|-------|-------|----------|--------|
| 1 | | | 1-2 | |
| 2 | | | 3 | |
| 3 | | | 4 | |
| 4 | | | 5 | |
| 5 | | | 6 | |
| 6 | | | 7 | |
| 7 | | | 8 | |
| 8 | | | 9 | |
| 9 | | | 10 | |
| 10 | | | 11 | |
| 11 | | | 12 | |
| 12 | | | 13 | |
| 13 | | | 14 | |
| 14 | | | 15 | |

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