Accelerator Framework for Mapping Floating-Point CNN on Low-Power Resource-Limited FPGAs

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Abstract—Convolutional neural networks (CNNs) have become ubiquitous in the field of image processing, computer vision, and artificial intelligence (AI). Given the high computational demands of CNNs, dedicated hardware accelerators have been implemented to improve compute performance in FPGAs and ASICs. However, most commercial general-purpose deep learning processing units (DPUs) struggle with support for low-power, resource-limited embedded devices. In this paper, we present a tensor processor (TP) as a dedicated hardware accelerator for TensorFlow (TF) Lite on embedded FPGA. We accelerate Conv2D and DepthwiseConv2D tensor operations with fixed-point and floating-point. The proposed compute optimization performs vector dot-product with hybrid custom floating-point and logarithmic approximation. This approach accelerates computation, reduces energy consumption and resource utilization. To demonstrate the potential of the proposed architecture, we address a design exploration with four compute engines: (1) fixed-point, (2) Xilinx floating-point LogiCORE IP, (3) hybrid custom floating-point approximation, and (4) hybrid logarithmic approximation. The hardware design is implemented with high-level synthesis (HLS). A single TP running at 150 MHz on a Xilinx Zynq-7020 achieves 45X runtime acceleration and 954X power reduction on Conv2D tensor operation compared with ARM Cortex-A9 at 666MHz, and 4.59X compared with the equivalent implementation with floating-point LogiCORE IP. The entire hardware design and the implemented TF Lite software extensions are available as an opensource project.

Index Terms—Artificial intelligence, convolutional neural networks, depthwise separable convolution, hardware accelerator, TensorFlow Lite, embedded systems, FPGA, custom floating-point, logarithmic computation, approximate computing

I. INTRODUCTION

THE constant research and the rapid evolution of artificial neural networks (ANNs) are driving the transition to smarter and more powerful AI applications, where CNN-based models represent the essential building blocks of deep learning algorithms in computer vision tasks [1]. Applications such as smart surveillance, medical imaging, natural language processing, robotics, and autonomous navigation have been powered by CNN-based models in industry and academia [2]. Nonetheless, dedicated hardware is often required to accelerate execution due to the high computational demands of CNNs. In terms of pure computational throughput, graphics processing units (GPUs) offer the best performance. In terms of power consumption, FPGA solutions are well known to be more energy efficient (than GPUs) [3]. As a result, numerous FPGA accelerators have

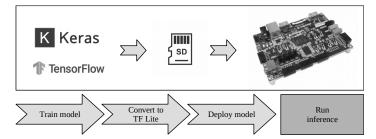


Fig. 1. Deployment workflow.

been proposed, targeting both high performance computing (HPC) for data-centers and embedded systems applications [4], [5]. However, most commercial deep learning processing units (DPUs) are not designed for low-power, resource-limited embedded FPGAs.

In this paper, we present a tensor processor compatible with TensorFlow Lite to accelerate Conv2D and DepthwiseConv2D operations on embedded FPGA. This implementation is integrated in a hardware/software co-design framework to accelerate tensor operations on FPGAs. This framework integrates TensorFlow Lite library and implements delegate interfaces [6] as bridge between the TF Lite runtime and the proposed hardware architecture. To control resource utilization and energy consumption, we implement the tensor operations as individual hardware engines, where they are optionally instantiated in the FPGA fabric as needed. Further on, to accelerate floating-point computation, we adopt the hybrid custom floating-point and logarithmic dot-product approximation technique [7], which exploits the intrinsic error-resilience of neural networks [8]. This approach can efficiently trade off quality-of-result (QoR) and resource utilization.

To operate the proposed system, the user would train a custom CNN model using TensorFlow or Keras, then this is converted into a TensorFlow Lite model, then the model is stored in a micro SD card along with the embedded software and configuration bitstream. See **Fig.** 1.

Our main contributions are as follows:

1) We present a tensor processor as a dedicated hardware accelerator for TensorFlow Lite on embedded FPGA. We accelerate *Conv2D* and *DepthwiseConv2D* tensor operations with fixed-point and floating-point computation.

- 2) We develop a hardware/software co-design framework targeting low-power and resource-constrained AI applications. The parameterized and modular architecture enables design exploration with different compute hardware approaches.
- 3) We demonstrate the potential of the proposed architecture by address a design exploration of *Conv2D* and *DepthwiseConv2D* operations with four compute engines: (1) fixed-point, (2) floating-point LogiCORE, (3) hybrid custom floating-point approximation, and (4) hybrid logarithmic approximation. We evaluate compute performance and classification accuracy implementing half-precision, brain floating-point, TensorFloat, and custom reduced formats for approximate processing, including logarithmic computation. Detailed performance reports are presented.

To promote the research in this field, our entire work is made available to the public as an open-source project at X.

II. RELATED WORK

A. Google's Edge TPU

The Edge Tensor Processing Unit (TPU) is an ASIC designed by Google that provides high performance machine learning (ML) inference for TensorFlow Lite models [9]. This implementation uses PCIe and I2C/GPIO to interface with an iMX 8M system-on-chip (SoC). The reported throughput and power efficiency are 4 TOPS and 2 TOPS per watt, respectively [10]. The Edge TPU supports 40 tensor operations including *Conv2D* and *DepthwiseConv2D*.

However, the Edge TPU does not support floating-point computation. The Edge TPU supports only TensorFlow Lite models that are 8-bit quantized and then compiled specifically for the Edge TPU [11]. Regarding power dissipation, the Edge TPU system-on-module (SoM) requires up to 15W power supply [10], which can be inadequate for very low-power applications.

B. Xilinx Zynq DPU

The Xilinx deep learning processing unit (DPU) is a configurable computation engine optimized for CNNs. The degree of parallelism utilized in the engine is a design parameter and can be selected according to the target device and application. The DPU IP can be implemented in the programmable logic (PL) of the selected Zynq-7000 SoC or Zynq UltraScale+ MPSoC device with direct connections to the processing system (PS) [12]. The peak theoretical performance reported on Zynq-7020 is 230 GOP/s.

However, the DPU does not support floating-point computation. The DPU requires the CNN model to be quantized, calibrated, converted into a deployable model, and then compiled into the executable format [12].

III. BACKGROUND

A. Conv2D tensor operation

The Conv2D tensor operation is described in **Eq.** (1), where X represents the input feature maps, W represents the convolution kernel (known as filter) and b represents the bias for the output feature maps [13]. We denote Conv as Conv2D operator.

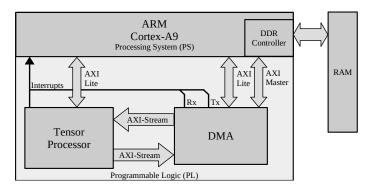


Fig. 2. Base embedded system architecture.

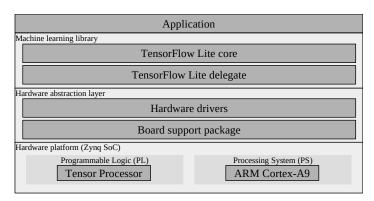


Fig. 3. Base embedded software architecture.

$$Conv(W,X)_{i,j,o} = \sum_{k,l,m}^{K,L,M} W_{(o,k,l,m)} \cdot X_{(i+k,j+l,m)} + b_o \quad (1)$$

B. DepthwiseConv2D tensor operation

The DepthwiseConv2D tensor operation is described in **Eq.** (2), where X represents the input feature maps, W represents the convolution kernel (known as filter), and b represents the bias for the output feature maps. We denote DConv as DepthwiseConv2D operator.

$$DConv\left(W,X\right)_{i,j,n} = \sum_{k,l}^{K,L} W_{(k,l,n)} \cdot X_{(i+k,j+l,n)} + b_{n} \quad (2)$$

IV. SYSTEM DESIGN

The proposed system architecture is a hardware/software codesign framework to investigate tensor acceleration targeting embedded FPGAs. In this paper, we focus on the base embedded system architecture with a single TP. The software and hardware architectures are shown in **Fig.** 2 and **Fig.** 3, respectively.

a) **Tensor processor**: The TP is a dedicated hardware module to compute tensor operations. The hardware architecture is described in **Fig.** 5. This architecture implements high performance off-chip communication with AXI-Stream, direct CPU communication with AXI-Lite, and on-chip storage utilizing BRAM. This hardware architecture is implemented

with HLS. The tensor operations are implemented based on the C++ TF Lite micro kernels [14].

$$TP_M = Input_M + Filter_M + Bias_M + Var_M$$
 (3)

$$Input_M = K_H W_I C_I Bit Size_I \tag{4}$$

$$Filter_M = C_I K_W K_H C_O Bit Size_F$$

$$Bias_M = C_O Bit Size_B$$
 (6)

(5)

$$C_O = \frac{TP_M - Var_M - K_H W_I C_I Bit Size_I}{C_I K_W K_H Bit Size_F + Bit Size_B}$$
 (7)

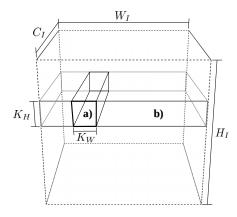


Fig. 4. Convolution of input tensor, with (a) filter tensor, and (b) input buffer.

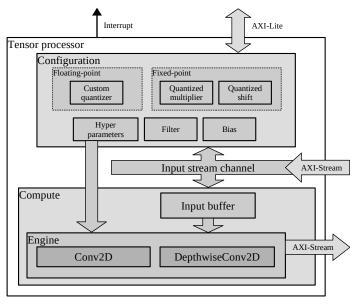


Fig. 5. Hardware architecture of the proposed tensor processor.

b) **Modes of operation**: This accelerator offers two modes of operation: configuration and execution.

In *configuration* mode, the TP receives the operation ID and hyperparameters: stride, dilation, padding, offset, activation, quantized activation, depth-multiplier, input shape, filter shape, bias shape, and output shape. Afterwards, the TP receives filter and bias tensors to be locally stored.

In *execution* mode, the TP executes the tensor operator according to the hyperparameters given in the configuration mode. During execution, the input and output tensor-buffers are moved from/to the TF Lite memory regions via direct memory access (DMA).

- c) Compatibility: This TP is compatible with TF Lite 8-bit quantized models and standard floating-point. For this purpose, we implement the compute engines with regular fixed-point and floating-point LogiCORE IPs. Vivado HLS accomplishes floating-point arithmetic operations by mapping them onto Xilinx LogiCORE IP in the resultant RTL [15].
- d) Dot-product with floating-point optimization: We optimize the floating-point computation adopting the dot-product with hybrid custom floating-point and logarithmic approximation [7]. This approach: (1) denormalizes input numbers, (2) executes computation with integer format for exponent and mantissa, and finally, (3) it normalizes the result into IEEE 754 format. This design implements a pipelined vector dot-product with a latency of 2N + II (clock cycles), where N and II are the vector length and initiation interval, respectively. This implementation achieves up to 5× latency reduction compared with a pipelined vector dot-product using Xilinx floating-point LogiCORE [7]. The hardware dot-product is illustrated in Fig. 6. As a design parameter, the mantissa bit-width of the weight vector provides a tunable knob to trade-off between resource-efficiency and QoR [16]. Since the lower-order bits have smaller significance than the higher-order bits, truncating them may have only a minor impact on QoR [17].

V. EXPERIMENTAL RESULTS

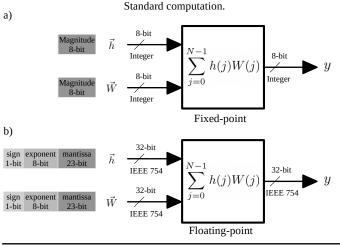
The proposed hardware/software co-design framework is demonstrated on a Xilinx Zynq-7020 SoC (Zybo-Z7 development board). On the PL, we implement the proposed hardware architecture with a clock frequency at 150MHz. On the PS, we execute the bare-metal software TF Lite Micro on the ARM Cortex-A9 at 666MHz equipped with NEON floating-point unit (FPU) [18].

To demonstrate compliance of the proposed design, we build models A and B in TensorFlow. Model B incorporates depthwise separable convolution operations (a depthwise convolution followed by a pointwise convolution). See **Fig.** 7.

To demonstrate hardware feasibility, A and B are evaluated by addressing a design exploration with the following implementations: (1) fixed-point, (2) floating-point LogiCORE, (3) hybrid custom floating-point approximation, and (4) hybrid logarithmic approximation.

A. Hardware design exploration

1) **Fixed-point**: To evaluate the compute performance on fixed-point, we convert A and B to TF Lite models with 8-



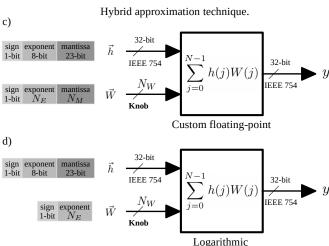


Fig. 6. Hardware alternatives for vector dot-product.

	Model A		Model B		
	FC (10), Softmax		FC (10), Softmax		
	FC (128), ReLu		Flatten		
	Flatten		2 x 2 MaxPool, stride 2		
	2 x 2 MaxPool, stride 2	(5B)	3 x 3 Conv (64), ReLu		
(4A)	3 x 3 Conv (256), ReLu		BatchNormalization (64)		
	BatchNormalization (128)		2 x 2 MaxPool, stride 2		
	2 x 2 MaxPool, stride 2	(4B)	1 x 1 Conv (64), ReLu		
(3A)	3 x 3 Conv (128), ReLu	(3B)	3 x 3 DConv, ReLu		
	2 x 2 MaxPool, stride 2		2 x 2 MaxPool, stride 2		
(2A)	3 x 3 Conv (64), ReLu	(2B)	1 x 1 Conv (64), ReLu		
(1A)	3 x 3 Conv (64), ReLu	(1B)	3 x 3 DConv, ReLu		
	Image (3 x 32 x 32)		Image (3 x 32 x 32)		

Fig. 7. CNN-based models for case study.

bit fixed-point quantization. The compute performance is presented in **Tab.** I. A runtime execution of A is illustrated in **Fig.** 8. This implementation achieves a peak runtime acceleration of $45.23 \times$ in model A at the tensor operation (4A) Conv, see **Tab.** I.

2) **Floating-point LogiCORE**: To evaluate the compute performance on floating-point models, we convert *A* and *B* to

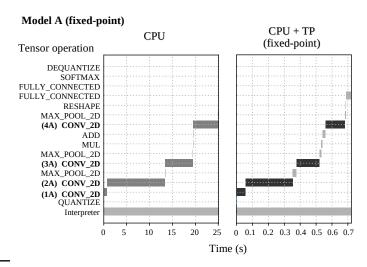


Fig. 8. Compute performance with fixed-point on model A.

TF Lite without quantization. The compute performance is presented in **Tab.** II. This implementation achieves a peak acceleration of $9.77\times$ in model A at the tensor operation (4A) Conv.

- 3) Hybrid custom floating-point approximation: This implementation presents a peak acceleration of $44.87 \times$ in model A at the tensor operation (4A) Conv. See Tab. III. This implementation achieves a $4.59 \times$ acceleration over the LogiCORE floating-point implementation. The runtime execution of model B with DConv tensor operations is illustrated in Fig. 10.
- 4) **Hybrid logarithmic approximation**: This implementation is presented for comparison in **Fig.** 9, which shows the runtime executions of model *A* with the proposed floating-point solutions including hybrid logarithmic approximation.

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Tensor operation Operation MMAC		CPU	U TP (fixed-point)			Accel.
		t (ms)	t (ms)	MMAC/s	GMAC/W	
Model	A					
(1A) Conv	1.769	700.22	55.19	32.06	0.23	12.69
(2A) Conv	37.748	12,666.91	297.08	127.06	0.93	42.64
(3A) Conv	18.874	6,081.01	142.99	131.99	0.97	42.53
(4A) Conv	18.874	5,543.77	122.58	153.97	1.13	45.23
Model	B					
(1B) DConv	0.027	13.43	0.63	43.74	0.25	21.25
(2B) Conv	0.196	129.95	11.57	16.98	0.12	11.23
(3B) DConv	0.147	69.18	3.33	44.26	0.25	20.77
(4B) Conv	1.048	378.78	9.96	105.25	0.77	38.02
(5B) Conv	2.359	694.60	16.46	143.22	1.05	42.20

B. Classification accuracy

We evaluate the classification accuracy of the CNN models under the effects of custom floating and logarithmic quantization. **Tab.** IV presents the list of custom formats proposed for evaluation. In this case, the *filter* and *bias* tensors are quantized from base floating-point representation (IEEE 754) into custom

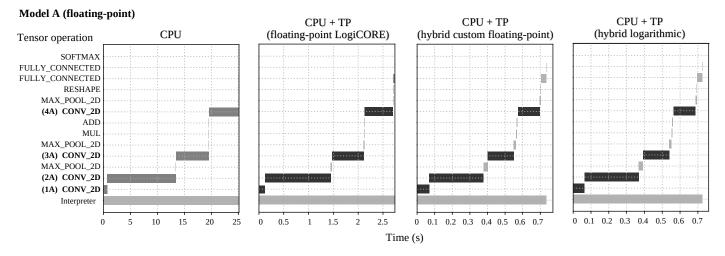


Fig. 9. Compute performance with the proposed floating-point solutions on model A.

TABLE II COMPUTE PERFORMANCE WITH FLOATING-POINT LOGICORE ON MODELS ${\cal A}$ and ${\cal B}.$

Tensor operation		CPU	TP (floa	Accel.		
Operation	MMAC	t (ms)	t (ms)	MMAC/s	GMAC/W	
Mode	l A					
(1A) Conv	1.769	670.95	120.07	14.73	0.21	5.59
(2A) Conv	37.748	12,722.13	1,328.08	28.42	0.40	9.58
(3A) Conv	18.874	6,094.85	636.53	29.65	0.42	9.58
(4A) Conv	18.874	5,564.79	569.30	33.15	0.47	9.77
Model	l B					
(1B) DConv	0.027	11.51	1.557	17.75	0.23	7.39
(2B) Conv	0.196	94.82	20.487	9.59	0.13	4.62
(3B) DConv	0.147	58.84	8.355	17.64	0.23	7.04
(4B) Conv	1.048	368.66	40.271	26.03	0.37	9.15
(5B) Conv	2.359	697.08	72.981	32.32	0.46	9.55

TABLE III COMPUTE PERFORMANCE WITH HYBRID CUSTOM FLOATING-POINT APPROXIMATION ON MODELS A AND B.

Tensor operation		CPU	TP (H	. custom floa	ting-point)	Accel.	
Operation MMAC		t (ms)	t (ms)	MMAC/s	GMAC/W		
Model A							IM
(1A) Conv	1.769	670.95	68.50	25.83	0.39	9.8	1 101
(2A) Conv	37.748	12,722.13	307.83	122.63	1.85	41.33	
(3A) Conv	18.874	6,094.85	147.97	127.55	1.93	41.19	
(4A) Conv	18.874	5,564.79	124.03	152.17	2.30	44.87	
Model	В						
(1B) DConv	0.027	11.51	1.41	19.63	0.27	8.17	
(2B) Conv	0.196	94.82	20.34	9.43	0.14	4.66	
(3B) DConv	0.147	58.84	6.58	22.41	0.31	8.94	
(4B) Conv	1.048	368.66	12.75	82.23	1.24	28.91	
(5B) Conv	2.359	697.08	17.14	137.68	2.08	40.68	

reduced formats with bit-truncation and -rounding methods. For this evaluation, we train A an B for image classification with CIFAR-10 dataset. We deploy the models with a baseline accuracy of 76.6% for A, and 68.8% for B. See **Fig.** 11.

C. Resource utilization and power dissipation

The resource utilization and power dissipation of the TP is listed in **Tab.** V. The power dissipation of the Zyng device is

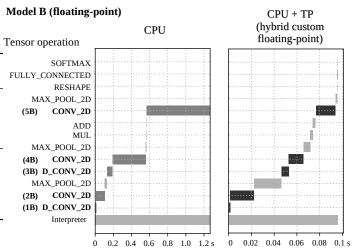


Fig. 10. Compute performance on model ${\cal B}$ (floating-point).

Time (s)

TABLE IV
IMPLEMENTED FLOATING-POINT FORMATS FOR ACCURACY EVALUATION.

Floating-point formats								
Name	Size (bits)	Sign	Exponent	Mantissa				
Logarithmic	6	1	5	0				
S1-E5-M1	7	1	5	1				
S1-E5-M2	8	1	5	2				
S1-E5-M3	9	1	5	3				
S1-E5-M4	10	1	5	4				
Float16	16	1	5	10				
BFloat16	16	1	8	7				
Tensor Float	19	1	8	10				
Float32	32	1	8	23				

presented in Fig. 12.

D. Discussion

1) **Energy consumption**: The implementations with hybrid custom floating-point and logarithmic approximation are the most efficient with energy reduction of $954 \times$ and

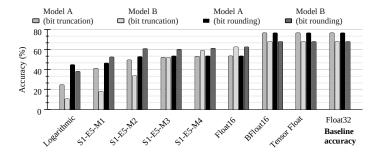


Fig. 11. Accuracy performance using hybrid custom floating-point approximation with various formats. Samples: CIFAR-10 test dataset (10,000 images).

TABLE V RESOURCE UTILIZATION AND POWER DISSIPATION OF THE PROPOSED TP ENGINES.

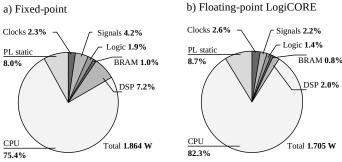
	Power (W)							
TP engine	LUT	FF	DSP	BRAM 18K				
1) Fixed-point								
Conv	5,677	4,238	78	70	0.136			
DConv	7,232	5,565	106	70	0.171			
Conv + DConv	12,684	8,015	160	70	0.248			
2) Floating-poin	t LogiCore	e						
Conv	4,670	3,909	59	266	0.070			
DConv	6,263	5,264	82	266	0.075			
Conv + DConv	10,871	7,726	123	266	0.119			
3) Hybrid custo	om floating	g-point ap	proxima	ition				
Conv	6,787	4,349	56	74	0.066			
DConv	8,209	5,592	79	74	0.072			
Conv + DConv	14,590	8,494	117	74	0.108			
4) Hybrid logarithmic approximation								
Conv	6,662	4,242	54	58	0.060			
DConv	8,110	5,380	77	58	0.066			
Conv + DConv	14,370	8,175	113	58	0.105			

 $1,055\times$, respectively. **Tab.** VI presents the energy-delay product (EDP) and energy reduction in (4A) Conv operator.

TABLE VI ENERGY CONSUMPTION IN TENSOR OPERATION (4A) Conv.

Engine	t (ms)	Power (W)	EDP (J)	Reduction
CPU	5,564.79	1.404	7,812.97	1.00
Fixed-point	122.58	0.136	16.67	468.66
Floating-point LogiCORE	569.30	0.070	39.85	196.05
Hybrid custom floating-point	124.03	0.066	8.19	954.43
Hybrid logarithmic	123.32	0.060	7.40	1,055.92

- Resource utilization: The fixed-point implementation presents the highest DSP utilization. Hence, this TP presents the highest power dissipation.
- 3) **Accuracy**: The hybrid custom floating-point approximation presents the best trade off between QoR and energy-efficiency. The bfloat16 (brain floating-point with 16-bits) achieves a comparable QoR with floating-point 32-bits, see **Fig.** 11. To improve accuracy, the CNN models would require quantization aware training methods.
- 4) **Bottleneck**: To increase performance, this implementation would require matching computational throughput with memory bandwidth using parallelization approaches.



c) Hybrid custom floating-point



Signals 4.1%

Logic **1.6%**

BRAM **0.4**%

DSP 7.2%

Total **1.689 W**

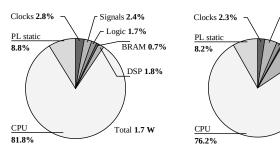


Fig. 12. Estimated power dissipation of the Zynq-7020 SoC with different TP engines.

VI. CONCLUSIONS

In this paper, we present a tensor processor as a dedicated hardware accelerator for TensorFlow Lite on embedded FPGA. We accelerate *Conv2D* and *DepthwiseConv2D* tensor operations for fixed-point and floating-point computation. The proposed optimization technique performs vector dot-product with hybrid custom floating-point and logarithmic approximation. This approach accelerates computation, reduces energy consumption and resource utilization. To demonstrate the potential of the proposed architecture, we presented a design exploration with four compute engines: (1) fixed-point, (2) Xilinx floating-point LogiCORE IP, (3) hybrid custom floating-point approximation, and (4) hybrid logarithmic approximation.

A single tensor processor running at 150 MHz on a Xilinx Zynq-7020 achieves $45\times$ runtime acceleration and $954\times$ power reduction on Conv2D tensor operation compared with ARM Cortex-A9 at 666MHz, and $4.59\times$ compared with the equivalent implementation with floating-point LogiCORE IP.

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