

# Accelerating Conv2D and DepthwiseConv2D Tensor Operations for TensorFlow Lite on Embedded FPGA with Hybrid Custom Floating-Point Approximation

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**Abstract**—Convolutional neural networks (CNNs) have become ubiquitous in the field of image processing, computer vision, and artificial intelligence (AI). Given the high computational demands of CNNs, dedicated hardware accelerators have been implemented to improve compute performance in FPGAs and ASICs. However, most commercial general-purpose deep learning processing units (DPUs) struggle with support for low-power, resource-limited embedded devices. In this paper, we present a tensor processor (TP) as a dedicated hardware accelerator for TensorFlow (TF) Lite on embedded FPGA. We accelerate Conv2D and DepthwiseConv2D tensor operations with fixed-point and floating-point. The proposed compute optimization performs vector dot-product with hybrid custom floating-point and logarithmic approximation. This approach accelerates computation, reduces energy consumption and resource utilization. To demonstrate the potential of the proposed architecture, we address a design exploration with four compute engines: (1) fixed-point, (2) Xilinx floating-point LogiCORE IP, (3) hybrid custom floating-point approximation, and (4) hybrid logarithmic approximation. The hardware design is implemented with high-level synthesis (HLS). A single TP running at 150 MHz on a Xilinx Zynq-7020 achieves 45X runtime acceleration and 951X power reduction on Conv2D tensor operation compared with ARM Cortex-A9 at 666MHz, and 4.59X compared with the equivalent implementation with floating-point LogiCORE IP. The entire hardware design and the implemented TF Lite software extensions are available as an open-source project.

**Index Terms**—Artificial intelligence, convolutional neural networks, depthwise separable convolution, hardware accelerator, TensorFlow Lite, embedded systems, FPGA, custom floating-point, logarithmic computation, approximate computing

## I. INTRODUCTION

THE constant research and the rapid evolution of artificial neural networks (ANNs) are driving the transition to smarter and more powerful AI applications, where CNN-based models represent the essential building blocks of deep learning algorithms in computer vision tasks [1]. Applications such as smart surveillance, medical imaging, natural language processing, robotics, and autonomous navigation have been powered by CNN-based models in industry and academia [2]. Nonetheless, dedicated hardware is often required to accelerate execution due to the high computational demands of CNNs. In terms of pure computational throughput, graphics processing units (GPUs)

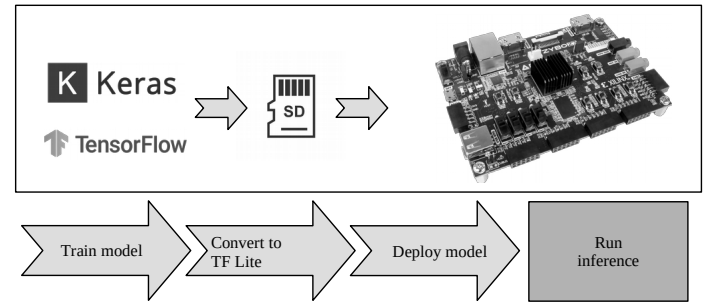


Fig. 1. Deployment workflow.

offer the best performance. In terms of power consumption, FPGA solutions are well known to be more energy efficient (than GPUs) [3]. As a result, numerous FPGA accelerators have been proposed, targeting both high performance computing (HPC) for data-centers and embedded systems applications [4]–[6]. However, most commercial deep learning processing units (DPUs) are not designed for low-power, resource-limited embedded FPGAs.

In this paper, we present a tensor processor compatible with TensorFlow Lite to accelerate *Conv2D* and *DepthwiseConv2D* operations on embedded FPGA. This implementation is integrated in a hardware/software co-design framework to accelerate tensor operations on FPGAs. This framework integrates TensorFlow Lite library and implements delegate interfaces [7] as bridge between the TF Lite runtime and the proposed architecture. To control resource utilization and energy consumption, we implement the tensor operations as hardware engines, where they are optionally instantiated in the FPGA fabric as needed. Further on, to accelerate floating-point computation, we adopt the hybrid custom floating-point and logarithmic dot-product approximation technique [8].

To operate the proposed system, the user would train a custom CNN model on TensorFlow or Keras, then this is converted into a TensorFlow Lite model (8-bit quantization and standard floating-point formats are supported), then the model is stored in a micro SD card along with the embedded software

and configuration bitstream. See **Fig. 1**.

Our main contributions are as follows:

- 1) We present a tensor processor as a dedicated hardware accelerator for TensorFlow Lite on embedded FPGA. We accelerate *Conv2D* and *DepthwiseConv2D* tensor operations with fixed-point and floating-point computation.
- 2) We develop a hardware/software co-design framework targeting low-power and resource-constrained AI applications. The parameterized and modular architecture enables design exploration with different compute hardware approaches.
- 3) We demonstrate the potential of the proposed architecture by address a design exploration with four compute engines: (1) fixed-point, (2) floating-point LogiCORE, (3) hybrid custom floating-point approximation, and (4) hybrid logarithmic approximation. We evaluate compute and accuracy performance implementing half-precision, brain floating-point, TensorFlow, and custom reduced formats for approximate processing, including logarithmic computation. Detailed performance reports are presented.

To promote the research in this field, our entire work is made available to the public as an open-source project at X.

## II. RELATED WORK

### A. Google's Edge TPU

The Edge Tensor Processing Unit (TPU) is an ASIC designed by Google that provides high performance machine learning (ML) inference for TensorFlow Lite models [9]. This implementation uses PCIe and I2C/GPIO to interface with an iMX 8M system-on-chip (SoC). The reported throughput and power efficiency are 4 TOPS and 2 TOPS per watt, respectively [10]. The Edge TPU supports 40 tensor operations including *Conv2D* and *DepthwiseConv2D* [11].

However, the Edge TPU does not support floating-point computation. The Edge TPU supports only TensorFlow Lite models that are fully 8-bit quantized and then compiled specifically for the Edge TPU [12]. As a limitation, the 8-bit quantization method requires a representative dataset that can be inaccessible. Regarding power dissipation, the Edge TPU system-on-module (SoM) requires up to 15W power supply [10], which can be inadequate for very low-power applications.

### B. Xilinx Zynq DPU

The Xilinx deep learning processing unit (DPU) is a configurable computation engine optimized for CNNs. The degree of parallelism utilized in the engine is a design parameter and can be selected according to the target device and application. The DPU IP can be implemented in the programmable logic (PL) of the selected Zynq-7000 SoC or Zynq UltraScale+ MPSoC device with direct connections to the processing system (PS) [13]. The peak theoretical performance reported on Zynq-7020 is 230 GOP/s.

However, the DPU does not support floating-point computation. The DPU requires the CNN model to be quantized, calibrated, converted into a deployable model, and then compiled into the executable format [13].

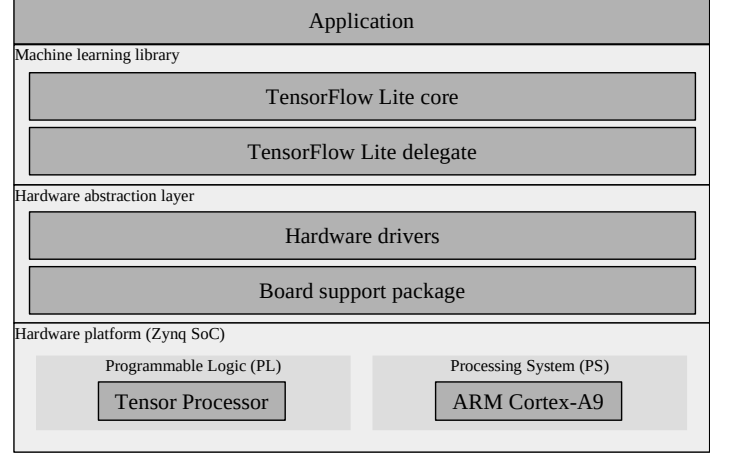


Fig. 2. System-level overview of the proposed embedded software stack.

## III. BACKGROUND

### A. Conv2D tensor operation

The *Conv2D* tensor operation is described in **Eq. (1)**. Where  $X$  represents the input feature maps,  $W$  represents the convolution kernel (known as filter) and  $b$  represents the bias for the output feature maps [14].

$$\text{Conv2D}(W, x)_{i,j,o} = \sum_{k,l,m}^{K,L,M} W_{(o,k,l,m)} \cdot x_{(i+k,j+l,m)+b_o} \quad (1)$$

### B. DepthwiseConv2D tensor operation

The *DepthwiseConv2D* tensor operation is described in **Eq. (2)**. Where  $X$  represents the input feature maps,  $W$  represents the convolution kernel (known as filter), and  $b$  represents the bias for the output feature maps.

$$\text{DConv2D}(W, x)_{i,j,n} = \sum_{k,l}^{K,L} W_{(k,l,n)} \cdot x_{(i+k,j+l,n)} + b_o \quad (2)$$

## IV. SYSTEM DESIGN

The proposed system architecture is a hardware/software framework to investigate tensor acceleration with target on Zynq devices. The SoC architecture is illustrated in **Fig. 3**. The software stack is shown in **Fig. 2**.

a) *Tensor processor*: The TP is a dedicated hardware module to compute tensor operations. The hardware architecture is described in **Fig. 4**. This architecture implements on-chip storage, high performance off-chip communication with AXI-Stream, and communication with CPU via AXI-Lite and interrupt. This hardware architecture is implemented with HLS. The tensor operators are implemented based on the C++ TF Lite micro kernels [15].

This accelerator offers two modes of operation: *configuration* and *execution*.

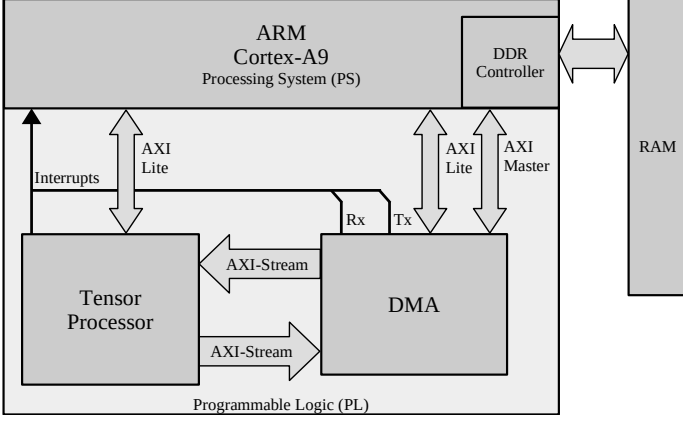


Fig. 3. System-level architecture of the proposed embedded platform.

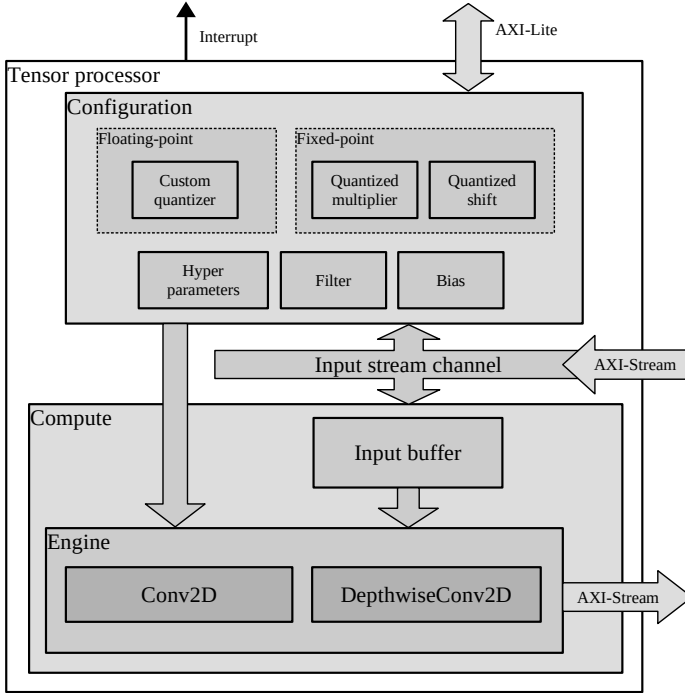


Fig. 4. Hardware architecture of the proposed tensor processor.

*b) Configuration mode:* In this mode, the TP receives the operator ID and the hyperparameters for execution: stride, dilation, padding, offset, activation, quantized activation, depth-multiplier, input shape, filter shape, bias shape, and output shape. Afterwards the accelerator receives the *filter*, *bias* and quantization vectors.

*c) Execution mode:* In this mode, the TP executes the tensor operator according to the hyperparameters given in the configuration mode. During execution, the input and output tensor buffers are moved from/to the TF Lite memory regions via direct memory access (DMA).

*d) Compatibility:* This TP is compatible with TF Lite 8-bit quantized models and standard floating-point. For this purpose, we implement the compute engines with regular integers and floating-point LogiCORE IPs.

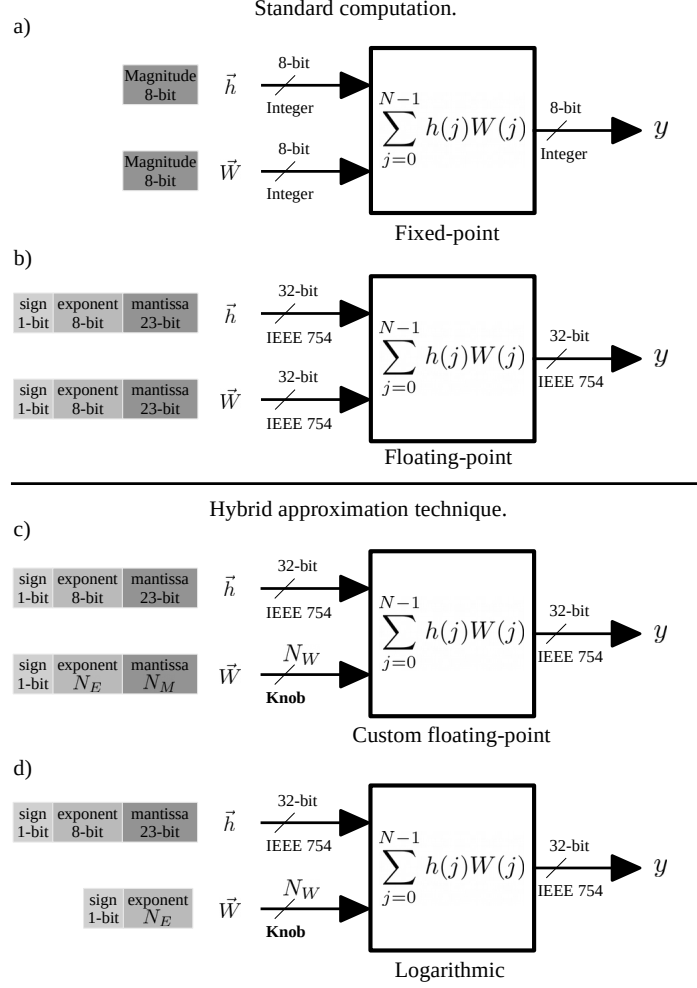


Fig. 5. Hardware alternatives for vector dot-product.

*e) Floating-point optimization:* We optimize the floating-point computation adopting the dot-product with hybrid custom floating-point and logarithmic approximation [8]. This approach: (1) denormalize input numbers, (2) executes computation in integer format for exponent and mantissa, and finally (3) normalize the result into IEEE 754 format. This design implements a pipelined vector dot-product with a latency of  $2N + II$ , where  $N$  and  $II$  are the vector length and initiation interval, respectively. This implementation achieves up to  $5\times$  latency reduction compared with a pipelined vector dot-product using Xilinx floating-point LogiCORE [8]. We implement the vector dot-product illustrated in Fig. 5.

## V. EXPERIMENTAL RESULTS

The proposed hardware/software framework is demonstrated on a Xilinx Zynq-7020 SoC (Zybo-Z7 development board). On the programmable logic (PL), we implement the proposed hardware architecture with a clock frequency at  $150MHz$ . On the processing system (PS), we execute TF Lite micro on the ARM Cortex-A9 at  $666MHz$  with NEON floating-point unit (FPU) [16].

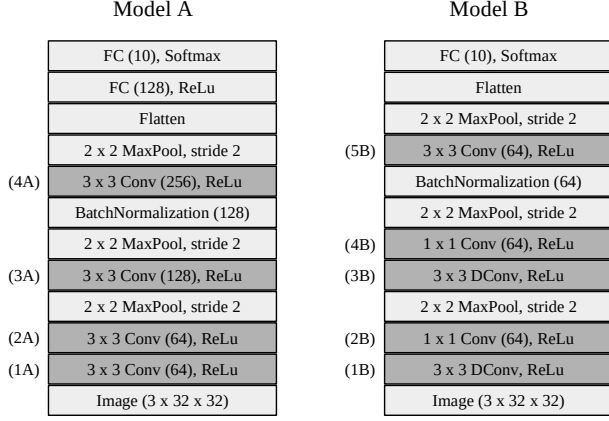


Fig. 6. CNN-based models for case study.

To evaluate the performance, we build models *A* and *B* in TensorFlow, see **Fig. 6**. To evaluate *DConv* tensor operation, model *B* incorporates depthwise separable convolution operations (a depthwise convolution followed by a pointwise convolution).

*A* and *B* are evaluated with the following hardware implementations:

- 1) Fixed-point.
- 2) Floating-point LogiCORE.
- 3) Hybrid custom floating-point approximation.
- 4) Hybrid logarithmic approximation.

*a) Fixed-point:* To evaluate the compute performance on fixed-point, we convert *A* and *B* to TF Lite models with 8-bit fixed-point quantization. The compute performance is presented in **Tab. I**. A runtime execution of *A* is illustrated in **Fig. 7**. This implementation achieves a peak acceleration of  $45.23\times$  in model *A* at the tensor operation (4A) *Conv*, see **Tab. I**.

TABLE I  
COMPUTE PERFORMANCE WITH FIXED-POINT ON MODEL *A* AND *B*.

Tensor operation		CPU	TP (fixed-point)			Accel.
Operation	MOP	t (ms)	t (ms)	MOP/s	GOP/W	
Model A						
(1A) Conv	1.769	700.22	55.19	32.06	0.23	12.69
(2A) Conv	37.748	12,666.91	297.08	127.06	0.93	42.64
(3A) Conv	18.874	6,081.01	142.99	131.99	0.97	42.53
(4A) Conv	18.874	5,543.77	122.58	153.97	1.13	45.23
Model B						
(1B) DConv	0.027	13.43	0.63	43.74	0.25	21.25
(2B) Conv	0.196	129.95	11.57	16.98	0.12	11.23
(3B) DConv	0.147	69.18	3.33	44.26	0.25	20.77
(4B) Conv	1.048	378.78	9.96	105.25	0.77	38.02
(5B) Conv	2.359	694.60	16.46	143.22	1.05	42.20

*b) Floating-point LogiCORE:* To evaluate the compute performance on floating-point models, we convert *A* and *B* to TF Lite without quantization. The compute performance is presented in **Tab. II**. This implementation achieves a peak acceleration of  $9.77\times$  in model *A* at the tensor operation (4A) *Conv*.

Model A (fixed-point)

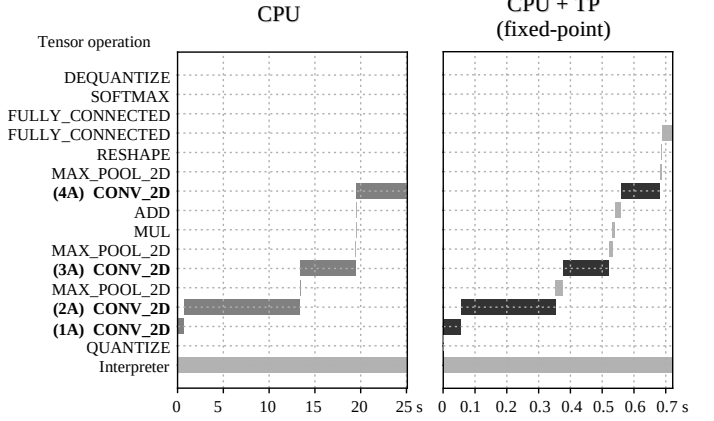


Fig. 7. Compute performance with fixed-point on model *A*.

TABLE II  
COMPUTE PERFORMANCE WITH FLOATING-POINT LOGICORE ON MODELS *A* AND *B*.

Tensor operation		CPU	TP (floating-point LogiCORE)			Accel.
Operation	MOP	t (ms)	t (ms)	MOP/s	GOP/W	
Model A						
(1A) Conv	1.769	670.95	120.07	14.73	0.21	<b>5.59</b>
(2A) Conv	37.748	12,722.13	1,328.08	28.42	0.40	<b>9.58</b>
(3A) Conv	18.874	6,094.85	636.53	29.65	0.42	<b>9.58</b>
(4A) Conv	18.874	5,564.79	569.30	33.15	0.47	<b>9.77</b>
Model B						
(1B) DConv	0.027	11.51	1.557	17.75	0.23	<b>7.39</b>
(2B) Conv	0.196	94.82	20.487	9.59	0.13	<b>4.62</b>
(3B) DConv	0.147	58.84	8.355	17.64	0.23	<b>7.04</b>
(4B) Conv	1.048	368.66	40.271	26.03	0.37	<b>9.15</b>
(5B) Conv	2.359	697.08	72.981	32.32	0.46	<b>9.55</b>

*c) Hybrid custom floating-point approximation:* This implementation presents a peak acceleration of  $44.87\times$  in model *A* at the tensor operation (4A) *Conv*. See **Tab. III**. It is expected that this implementation achieves near  $5\times$  acceleration compared with the LogiCORE-based implementation. In this case, we observe an acceleration of  $4.59\times$ .

TABLE III  
COMPUTE PERFORMANCE WITH HYBRID CUSTOM FLOATING-POINT APPROXIMATION ON MODELS *A* AND *B*.

Tensor operation		CPU	TP (hybrid custom floating-point)			Accel.
Operation	MOP	t (ms)	t (ms)	MOP/s	GOP/W	
Model A						
(1A) Conv	1.769	670.95	68.50	25.83	0.39	9.8
(2A) Conv	37.748	12,722.13	307.83	122.63	1.85	41.33
(3A) Conv	18.874	6,094.85	147.97	127.55	1.93	41.19
(4A) Conv	18.874	5,564.79	124.03	152.17	2.30	44.87
Model B						
(1B) DConv	0.027	11.51	1.41	19.63	0.27	8.17
(2B) Conv	0.196	94.82	20.34	9.43	0.14	4.66
(3B) DConv	0.147	58.84	6.58	22.41	0.31	8.94
(4B) Conv	1.048	368.66	12.75	82.23	1.24	28.91
(5B) Conv	2.359	697.08	17.14	137.68	2.08	40.68

For comparison, **Fig. 8** shows the runtime executions of model *A* with the proposed floating-point solutions. **Fig. 9**

illustrates the runtime execution of model  $B$  with  $DConv$  tensor operators.

The dot-product with hybrid custom floating-point approximation achieves better performance with larger vectors. Since  $DConv$  performs a channel-wise spatial dot-product, this implementation presents very limited acceleration compared with the LogiCORE-based implementation.

*d) Accuracy performance:* For this evaluation, we train  $A$  and  $B$  for image classification with CIFAR-10 dataset. We deploy the models with a baseline accuracy of 76.6% for  $A$ , and 68.8% for  $B$ .

We evaluate the accuracy performance of the CNN models under the effects of tensor quantization using reduced custom floating-point representation. **Tab. IV** presents the list of custom formats proposed for evaluation. In this case, the *filter* and *bias* tensors are quantized from base floating-point representation (IEEE 754) into custom reduced formats with bit-truncation and -rounding methods. This technique improves on-chip memory utilization, and enables quality configurability. The accuracy performance is presented in **Fig. 10**.

TABLE IV  
IMPLEMENTED FLOATING-POINT FORMATS FOR ACCURACY EVALUATION.

Floating-point formats				
Name	Size (bits)	Sign	Exponent	Mantissa
Logarithmic	6	1	5	0
S1-E5-M1	7	1	5	1
S1-E5-M2	8	1	5	2
S1-E5-M3	9	1	5	3
S1-E5-M4	10	1	5	4
Float16	16	1	5	10
BFloat16	16	1	8	7
Tensor Float	19	1	8	10
Float32	32	1	8	23

*e) Resource utilization and power dissipation:* The resource utilization and power dissipation of the TP is listed in **Tab. V**. The implementations with hybrid custom floating-point and logarithmic approximation are the most power efficient.

The estimated power dissipation of the CPU is 1.4W. The estimated power dissipation of the TP implementing  $Conv$  operator with hybrid custom floating-point is 66mW. This implementation achieves a peak acceleration of  $44.87\times$ . This results in a peak power efficiency improvement of  $951\times$ .

The power dissipation of the Zynq device is presented in **Fig. 11**.

## VI. CONCLUSIONS

In this paper, we present a tensor processor as a dedicated hardware accelerator for TensorFlow Lite on embedded FPGA. We accelerate  $Conv2D$  and  $DepthwiseConv2D$  tensor operations for fixed-point and floating-point computation. The proposed optimization technique performs vector dot-product with hybrid custom floating-point and logarithmic approximation. This approach accelerates computation, reduces energy consumption and resource utilization. To demonstrate the potential of the proposed architecture, we presented a design exploration with four compute engines: (1) fixed-point, (2) Xilinx floating-point

TABLE V  
RESOURCE UTILIZATION AND POWER DISSIPATION OF THE PROPOSED TP ENGINES.

TP engine	Post-implementation resource utilization				Power (W)
	LUT	FF	DSP	BRAM 18K	
1) Fixed-point					
Conv	5,677	4,238	78	70	0.136
DConv	7,232	5,565	106	70	0.171
Conv + DConv	12,684	8,015	160	70	0.248
2) Floating-point LogiCore					
Conv	4,670	3,909	59	266	0.070
DConv	6,263	5,264	82	266	0.075
Conv + DConv	10,871	7,726	123	266	0.119
3 ) Hybrid custom floating-point approximation					
Conv	6,787	4,349	56	74	0.066
DConv	8,209	5,592	79	74	0.072
Conv + DConv	14,590	8,494	117	74	0.108
4) Hybrid logarithmic approximation					
Conv	6,662	4,242	54	58	0.060
DConv	8,110	5,380	77	58	0.066
Conv + DConv	14,370	8,175	113	58	0.105

LogiCORE IP, (3) hybrid custom floating-point approximation, and (4) hybrid logarithmic approximation.

A single tensor processor running at 150 MHz on a Xilinx Zynq-7020 achieves  $45\times$  runtime acceleration and  $951\times$  power reduction on  $Conv2D$  tensor operation compared with ARM Cortex-A9 at 666MHz, and  $4.59\times$  compared with the equivalent implementation with floating-point LogiCORE IP.

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### Model A (floating-point)

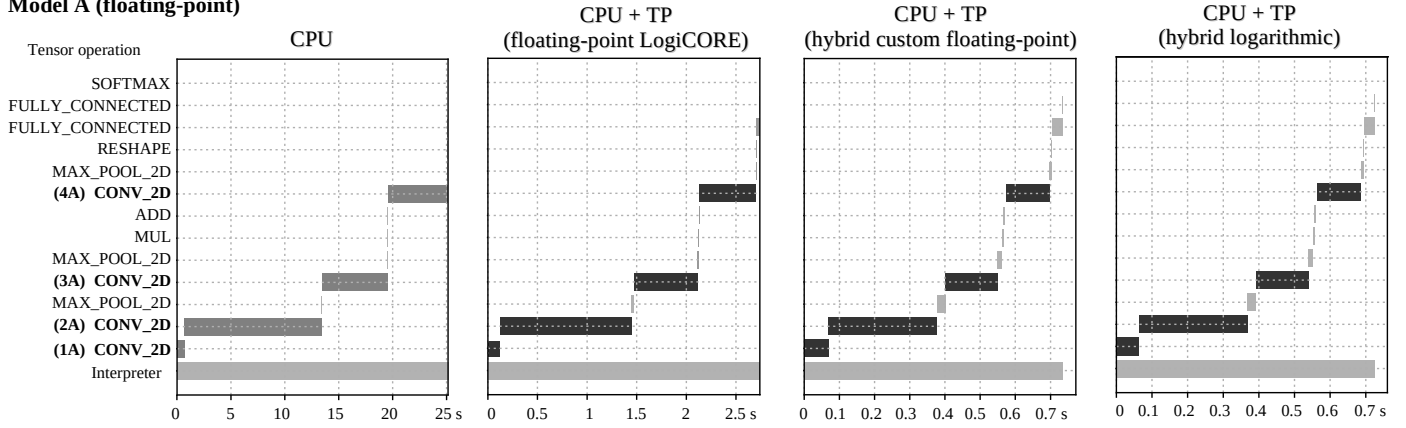


Fig. 8. Compute performance with the proposed floating-point solutions on model A.

### Model B (floating-point)

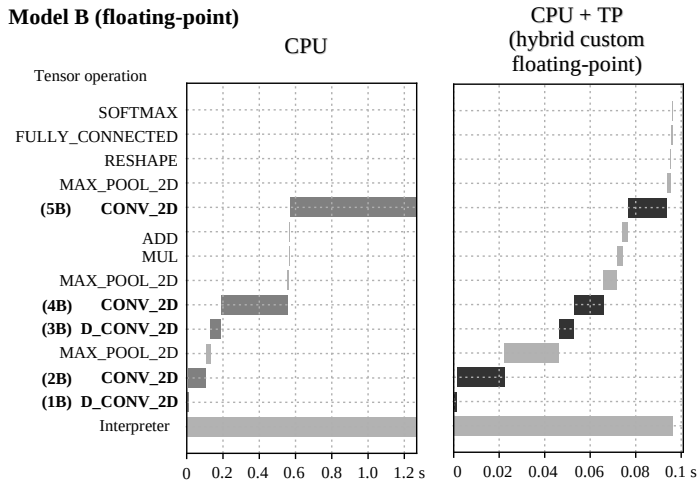


Fig. 9. Compute performance on model B (floating-point).

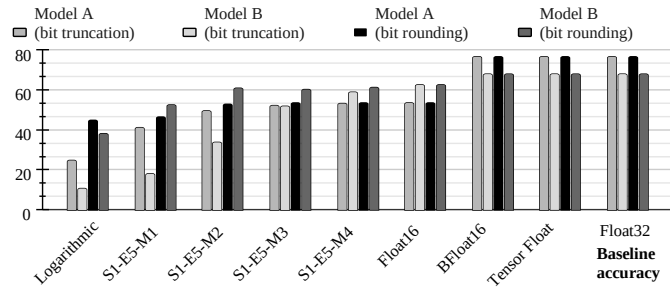


Fig. 10. Accuracy performance using hybrid custom floating-point approximation with various formats.

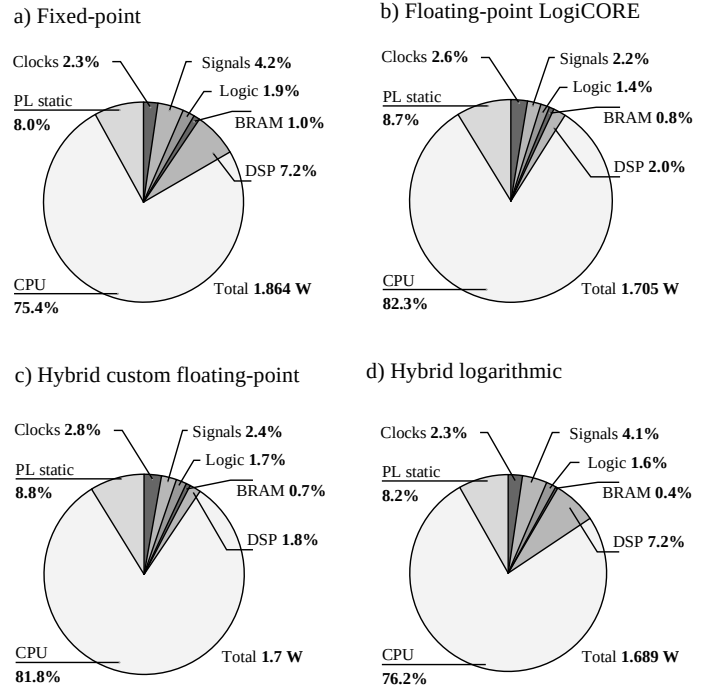


Fig. 11. Estimated power dissipation of the Zynq-7020 SoC with different TP engines.

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