

SCHRÖDINGER'S TIME DEPENDENT EQN : (SDE)

* We know :

$$\frac{1}{u^2} \frac{\partial^2 y}{\partial t^2} = \frac{\partial^2 y}{\partial x^2}, \text{ where } f = f(x, t)$$

ODE : ordinary diff. eqn

PDE : partial DE

* Goal : We have to find differential eqn (ODE/PDE), which will describe the micro level or quantum level description of the particle.

* Wave eqn : $f(x, t) = Ae^{i(\omega t - Kx)}$

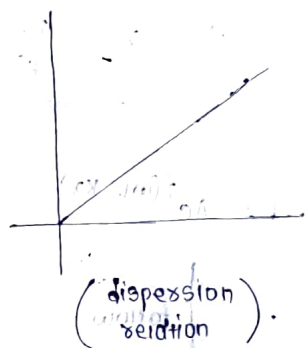
$$\frac{\partial f}{\partial t} = i\omega f, \quad \frac{\partial f}{\partial x} = -iKf$$

$$\frac{\partial^2 f}{\partial t^2} = (i\omega)^2 f, \quad \frac{\partial^2 f}{\partial x^2} = (-iK)^2 f$$

putting above eqn

$$\frac{\omega^2}{u^2} = K^2 \quad (\text{or}) \quad \omega = Ku$$

$K = \frac{\omega}{c}$ → module-1



* For Quantum level :

$$E = \frac{p^2}{2m}$$

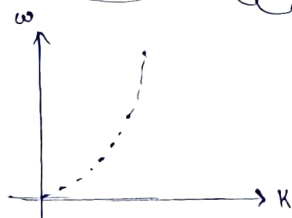
if $V(x) = 0$

$$p = \hbar K$$

$$\hbar = \frac{h}{2\pi}$$

$$\Rightarrow \hbar \omega = \frac{\hbar^2 K^2}{2m}$$

$$\Rightarrow \omega \propto K^2$$



* If we have to satisfy this dispersion relation, what is the governing ODE/PDE ?

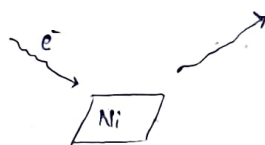
$$E = \frac{hc}{\lambda} = h\nu = 2\pi\hbar \left(\frac{\omega}{2\pi} \right) = \hbar\omega$$

~~P = mv~~
de-Broglie

$$\lambda = \frac{h}{p} \Rightarrow p = \frac{h}{\lambda} \Rightarrow p = \frac{h\nu}{c} \Rightarrow p = \frac{h}{2\pi} \left(\frac{\omega}{c} \right) = \frac{\hbar K}{2\pi} = \hbar K$$

DAIRSSON GERMER : (WAVE NATURE OF PARTICLE)

Wave Nature	Particle Nature
Bragg's Theory	de-Broglie
λ_{Bragg}	$\lambda_{\text{de-brog}}$



$$\lambda_{\text{Bragg}} = \lambda_{\text{debrog}}$$

$$2d \sin \theta = n\lambda$$

HEISENBERG UNCERTAINTY THEORY :

$$* \Delta p_x \cdot \Delta x \geq \hbar/2 = \frac{h}{4\pi}$$

$$\Delta p_y \cdot \Delta y \geq \hbar/2$$

$$\Delta p_z \cdot \Delta z \geq \hbar/2$$

$$* \Delta E \cdot \Delta t \geq \hbar/2$$

$$* \Delta J \cdot \Delta \phi \geq \hbar/2$$

$J \rightarrow$ angular momentum

$\phi \rightarrow$ angle

WAVE FUNCTION :

$$* \text{Notation} \rightarrow \Psi = \Psi(\vec{r}, t) \quad \text{Psi}$$

$$\psi = \psi(\vec{r})$$

psi

* Ψ is in general complex.

* $|\Psi|^2$ has meaning, it represents the probability density of

$|\Psi|^2 \cdot dx$ is the probability of finding the object (e^- , proton, etc)

b/w x & $x+dx$.