4.3-1.

Show that the solution of T(n) = T(n-1) + n is $O(n^2)$.

Answer.

$$\begin{split} T\left(n\right) &= T\left(n-1\right) + n \\ &= T\left(n-2\right) + \left(n-1\right) + n \\ &= T\left(n-3\right) + \left(n-2\right) + \left(n-1\right) + n \\ &= \cdots \\ &= T\left(0\right) + 1 + 2 + \cdots + \left(n-1\right) + n \\ &= T\left(0\right) + \frac{n\left(n+1\right)}{2} \\ &= O\left(n^2\right) \end{split}$$

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