



Introduction to Bayesian methods

Quiz, 10 questions



Congratulations! You passed!

Next Item



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point

1.

$p(x|\theta)p(\theta)$ is a distribution over:



x



(x, θ)



Correct

$p(x|\theta)p(\theta) = p(x, \theta)$ which is a distribution over vector (x, θ)



θ



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2.

Choose correct statements:



$$p(a | b) = \int p(a, c | b)dc$$



Correct

The sum rule.



$$p(a, b | c) = p(a | b, c)p(b | c)$$



Correct



$$p(a | b) = \int p(a | b, c)dc$$



Un-selected is correct



$$p(a | b) = \int p(a | b, c)p(c)dc, \text{ when } b \text{ and } c \text{ are independent}$$



Correct

$$p(c | b) = p(c) \text{ when } c \text{ and } b \text{ are independent}$$



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3.

Choose correct statements:

 $p(a | b, c) = p(a | b)p(a | c)$ when b and c are independent

Un-selected is correct



$$p(a | b, c) = \frac{p(b | a, c)p(a | c)}{\int p(b | a', c)p(a' | c)da'}$$



Correct



$$p(a | b) = \frac{p(a, c | b)}{p(c | a, b)}$$



Correct

Apply Bayes rule to $p(c | a, b)$ 

$$p(a | b)p(b) + p(a | \bar{b})p(b) = p(a), \text{ for binary } b$$



Correct

The law of total probability



$$p(a | b) + p(a | \bar{b}) = p(a), \text{ for binary } b$$



Un-selected is correct



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4.

Let joint probability over random variables a, b, c be $p(a, b, c) = p(a|b)p(b|c)p(c)$. Are random variables a and c independent?

Yes



No



Correct

Let's marginalize joint probability by b and we get $\int p(a, b, c)db = \int p(a|b)p(b|c)p(c)db = p(c) \int p(a|b)p(b|c)db$. Unfortunately, integral contain inside both a and c and it can't be decomposed into two integrals $\int f(a, b)db$ and $\int g(c, b)db$, so a and c is dependent.



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5.

Let joint probability over random variables a, b, c, d be $p(a, b, c, d) = p(a|b)p(b)p(c|d)p(d)$. Are random variables a and c independent?

Yes

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Correct

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Let's marginalize joint probability by b and d , so we get $\int p(a, b, c, d) db dd = \int p(a|b)p(b)p(c|d)p(d) db dd = (\int p(a|b)p(b) db) (\int p(c|d)p(d) dd)$. So we decomposed it into two integrals $\int f(a, b)db$ and $\int g(c, d)dd$, so a and c is independent.

☐ No



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6. Recall the probabilistic regression setting. In the lecture, we have proved that solving the least-squares problem with L2 regularizer $L(w) = \sum_{i=1}^n (w^T x_i - y_i)^2 + C \sum_{i=1}^N w_i^2$ is equivalent to finding the MAP estimate for w with prior distribution $\mathcal{N}(w | 0, \gamma I)$. Let us now choose a prior distribution to be Laplace distribution: $p(w|0, b) = \frac{1}{(2b)^n} \prod_{i=1}^n \exp\left(-\frac{|w_i|}{b}\right)$ instead of Normal. Adding which of the following regularizers to the least-squares problem is equivalent to finding a MAP-estimate for such a model?

☐ $\sum_{i=1}^N w_i^{\frac{1}{2}}$

☒ $\sum_{i=1}^N |w_i|$

Correct

Let's get minus logarithm of Laplace distribution and we will get $C \sum_{i=1}^n |w_i| + D$, where C and D are some constants. We can forget about D constant because it's not important when we will minimize loss function.

☐ $\sum_{i=1}^N \frac{1}{|w_i|}$

☐ $\sum_{i=1}^N w_i$



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7. For linear regression with loss function $L(w) = \sum_{i=1}^n (w^T x_i - y_i)^2 + C \sum_{i=1}^N w_i^2$ prior distribution for weights w was Normal distribution $\mathcal{N}(w|0, \gamma I)$. Which prior distribution on weights is right for loss function $L(w) = \sum_{i=1}^N (w^T x_i - y_i)^2$ if each component of weights should be in some predefined range: $w_i \in [l, r]$?

☒ Uniform distribution with the same limits for each component.

$$p(w | a, b) = \begin{cases} \frac{1}{(b-a)^n}, & \text{if } \forall w_i \in [l, r] \\ 0, & \text{else} \end{cases}$$

Correct

We can formulate question using equivalent loss function $L(w) = \sum_{i=1}^N (w^T x_i - y_i)^2 + \sum_{i=1}^N r(w_i)$ without limits on weights component but function $r(w_i) = \begin{cases} C, & \text{if } w_i \in [l, r] \\ +\infty, & \text{else} \end{cases}$. The same regularisation we will have if we find minus logarithm of Uniform distribution.

☐ Laplace distribution with zero mean and the same divergence for each component.

$$p(w | 0, b) = \frac{1}{(2b)^n} \prod_{i=1}^n \exp\left(-\frac{|w_i|}{b}\right)$$



Gamma distribution with the same parameters for each component.

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$$p(w|\alpha, \beta) = \frac{\Gamma(\alpha)^n}{\Gamma(\alpha)^n} \prod_i x_i^{\alpha-1} \exp^{-\beta w_i}$$



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8.

For the **remaining** problems we will use the following story:

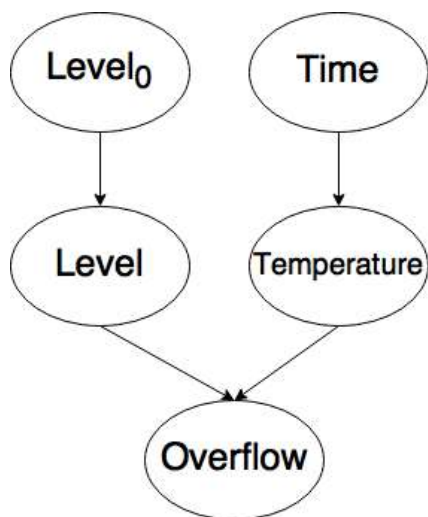
You have a kettle that boils water. You pour water up to level L_0 and turn the kettle on. Over time, temperature $Temp$ starts to increase. At time T , level of water is L . Since water is boiling, water level slightly oscillates and so can be considered random. You also know that the height of a kettle is limited. If at some point water level exceeds this value, water will split on a table. We will denote this event as a binary random variable O (overflow). Our goal is to determine the maximum allowed initial water level L_{max} so that we can write it down in a kettle manual. Normally we would like to find L_{max} for which, for example, $P(O | L_0 = L_{max}) = 0.001$: if you pour this amount of water, overflow will occur with a fairly low probability.

In these tasks we will construct a Bayesian network and select probability distributions needed for the model.

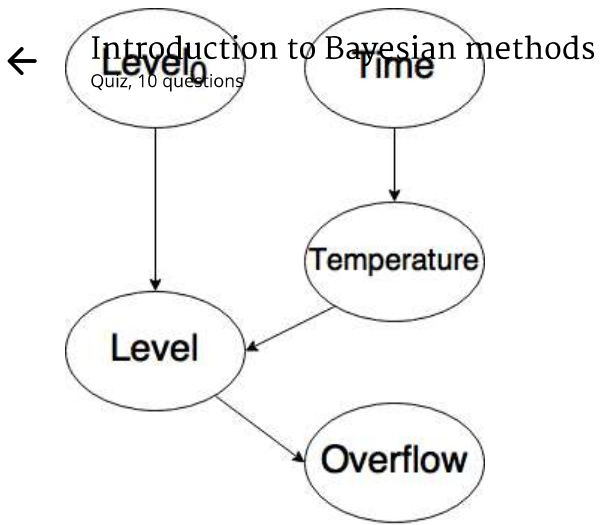
Our first step is to choose the correct Bayesian network.



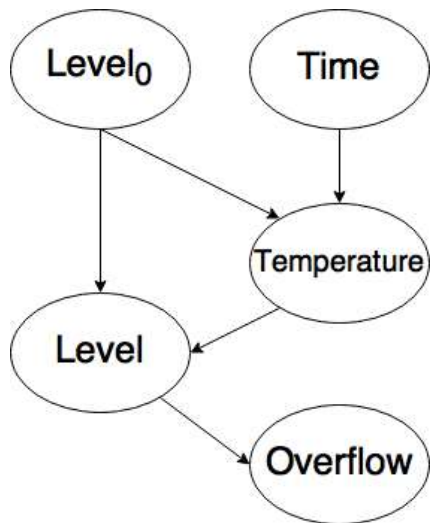
a)



b)

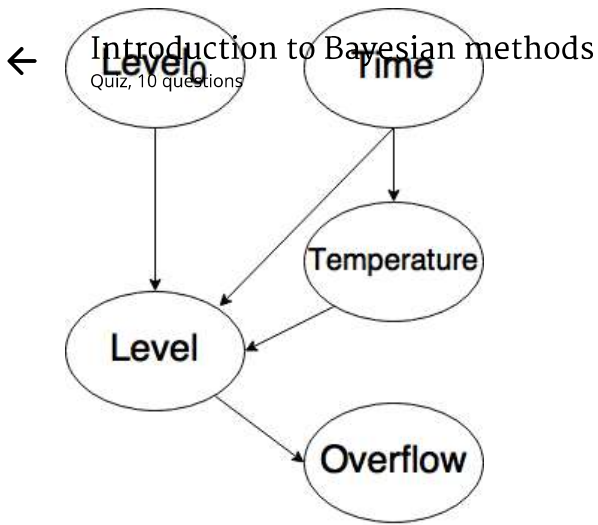


☒ c)



▲
Correct
Correct!

☐ d)



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9.

Write joint distribution for this situation.

☐ $p(L_0|L, Temp)p(T|Temp)p(Temp|L)p(L|O)p(O)$

☒ $p(O|L)p(L|L_0, Temp)p(Temp|L_0, T)p(L_0)p(T)$



Correct

☐ $p(L|O)p(Temp|L_0, L)p(Temp|L_0, T)p(L_0)p(T)$

☐ $p(O|L)p(L|L_0, Temp)p(L_0, T|Temp)p(Temp)$



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10.

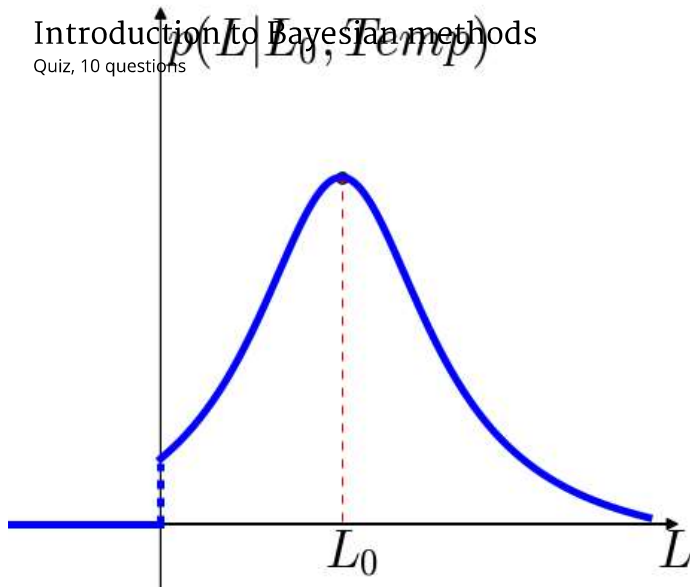
Which distribution can you use for $p(L|L_0, Temp)$?

☒ a)



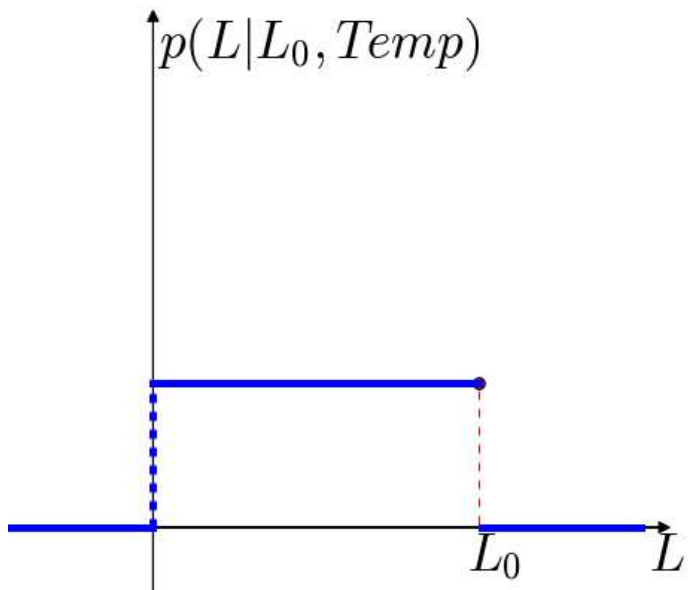
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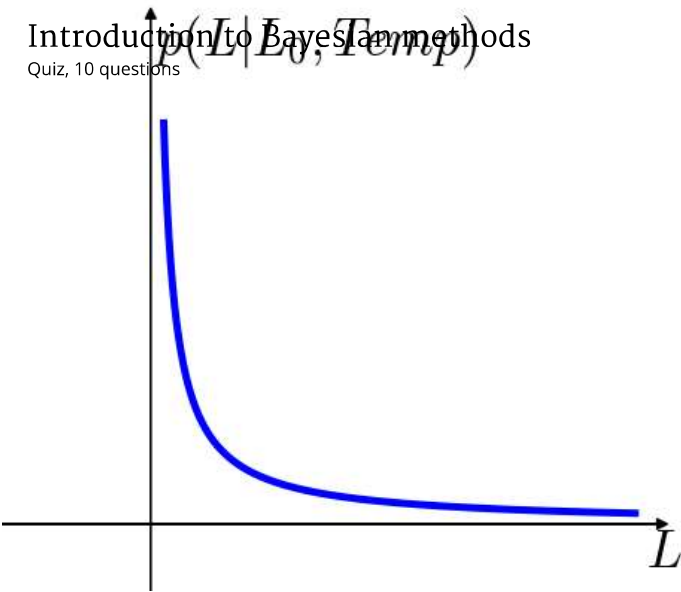


Correct

☐ b)



☐ c)



☐ d)

