

Previous Year Questions 2024

Q1: What should be added from the polynomial $x^2 - 5x + 4$, so that 3 is the zero of the resulting polynomial? (2024)

- (a) 1
- (b) 2
- (c) 4
- (d) 5

Ans: (b)

$$\text{Let, } f(x) = x^2 - 5x + 4$$

Let p should be added to f(x) then 3 becomes zero of polynomial.

$$\text{So, } f(3) + p = 0$$

$$\Rightarrow 3^2 - 5 \times 3 + 4 + p = 0$$

$$\Rightarrow 9 + 4 - 15 + p = 0$$

$$\Rightarrow -2 + p = 0$$

$$\Rightarrow p = 2$$

So, 2 should be added.

Q2: Find the zeroes of the quadratic polynomial $x^2 - 15$ and verify the relationship between the zeroes and the coefficients of the polynomial. (2024)

Ans:

$$x^2 - 15 = 0$$

$$x^2 = 15$$

$$x = \pm \sqrt{15}$$

Zeroes will be $\alpha = \sqrt{15}$, $\beta = -\sqrt{15}$

Verification: Given polynomial is $x^2 - 15$

On comparing above polynomial with

$ax^2 + bx + c$, we have

$$a = 1, b = 0, c = -15$$

sum of zeros = $\alpha + \beta$

$$= \sqrt{15} - \sqrt{15} = \frac{0}{1} = \frac{-b}{a}$$

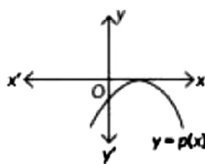
Product of zeros = $\alpha\beta$

$$\sqrt{15} \times -(\sqrt{15}) = \frac{-15}{1} = \frac{c}{a}$$

Hence, verified.

Previous Year Questions 2023

Q3: The graph of $y = p(x)$ is given, for a polynomial $p(x)$. The number of zeroes of $p(x)$ from the graph is (2023)



- (a) 3
- (b) 1
- (c) 2
- (d) 0

Ans: (b)

Here, $y = p(x)$ touches the x-axis at one point

So, number of zeros is one.

Q4: If α, β are the zeroes of a polynomial $p(x) = x^2 + x - 1$, then $1/\alpha + 1/\beta$ equals to (2023)

- (a) 1
- (b) 2
- (c) -1
- (d) -1/2

Ans: (a)

The polynomial is $p(x) = x^2 + x - 1$.

Step 1: The relationships between the zeroes and coefficients:

Sum of zeroes ($\alpha + \beta$): $-\frac{b}{a} = -\frac{1}{1} = -1$

Product of zeroes ($\alpha\beta$): $\frac{c}{a} = \frac{-1}{1} = -1$

Step 2: Simplify $\frac{1}{\alpha} + \frac{1}{\beta}$:

$$\frac{1}{\alpha} + \frac{1}{\beta} = \frac{\alpha + \beta}{\alpha\beta}$$

Substitute the values:

$$\frac{\alpha + \beta}{\alpha\beta} = \frac{-1}{-1} = 1$$

Final Answer: (a) 1

Q5: If α, β are the zeroes of a polynomial $p(x) = x^2 - 1$, then the value of $(\alpha + \beta)$ is (2023)

- (a) 1
- (b) 2
- (c) -1
- (d) 0

Ans: (d)

The polynomial is $p(x) = x^2 - 1$.

Step 1: Sum of zeroes $(\alpha + \beta)$: $-\frac{b}{a} = -\frac{0}{1}$

Step 2: Simplify:

$$\frac{0}{1} = 0$$

Final Answer: (d) 0

Q6: If α, β are the zeroes of a polynomial $p(x) = 4x^2 - 3x - 7$, then $(1/\alpha + 1/\beta)$ is equal to (2023)

- (a) $7/3$
- (b) $-7/3$
- (c) $3/7$
- (d) $-3/7$

Ans: (d)

The polynomial is $p(x) = 4x^2 - 3x - 7$.

Step 1: calculating sum and product of zeroes

Sum of zeroes $(\alpha + \beta)$: $-\frac{b}{a} = -\frac{(-3)}{4} = \frac{3}{4}$

Product of zeroes $(\alpha\beta)$: $\frac{c}{a} = \frac{-7}{4}$

Step 2: Simplify $\frac{1}{\alpha} + \frac{1}{\beta}$:

$$\frac{\alpha + \beta}{\alpha\beta} = \frac{\frac{3}{4}}{\frac{-7}{4}} = \frac{-3}{7}$$

Final Answer: (d) $-\frac{3}{7}$

Q7: If one zero of the polynomial $p(x) = 6x^2 + 37x - (k - 2)$ is reciprocal of the other, then find the value of k . (CBSE 2023)

Ans: We have,

The polynomial is $p(x) = 6x^2 + 37x - (k - 2)$.

Step 1: The relationship between the product of zeroes and coefficients:

$$\text{Product of zeroes } (\alpha\beta): \frac{c}{a} = \frac{-(k-2)}{6}$$

It is given that $\alpha\beta = 1$. Substitute this:

$$\frac{-(k-2)}{6} = 1$$

Step 2: Solve for k :

Multiply both sides by 6:

$$-(k-2) = 6$$

Simplify:

$$k - 2 = -6$$

$$k = -4$$

Final Answer: $k = -4$

Previous Year Questions 2022

Q8: If one of the zeroes of a quadratic polynomial $(k - 1)x^2 + kx + 1$ is -3 , then the value of k is (2022)

(a) $4/3$

(b) $-4/3$

(c) $2/3$

(d) $-2/3$

Ans: (a)

Given, -3 is a zero of quadratic polynomial $(k - 1)x^2 + kx + 1$.

$$\therefore (k - 1)(-3)^2 + k(-3) + 1 = 0$$

$$\Rightarrow 9k - 9 - 3k + 1 = 0 \Rightarrow 6k - 8 = 0$$

$$\Rightarrow k = 8/6$$

$$\Rightarrow k = 4/3$$

Q9: If the path traced by the car has zeroes at -1 and 2, then it is given by (2022)

- (a) $x^2 + x + 2$
- (b) $x^2 - x + 2$
- (c) $x^2 - x - 2$
- (d) $x^2 + x - 2$

Ans: (c)

The zeroes of the polynomial are **-1** and **2**.

Step 1: The polynomial with given zeroes is:

$$p(x) = a(x - \alpha)(x - \beta)$$

Substitute the zeroes $\alpha = -1$ and $\beta = 2$:

$$p(x) = a(x - (-1))(x - 2) = p(x) = a(x + 1)(x - 2)$$

Step 2: Expand the polynomial:

$$p(x) = a[(x)(x) + (x)(-2) + (1)(x) + (1)(-2)]$$

$$p(x) = a[x^2 - x - 2]$$

Step 3: Assuming $a = 1$:

$$p(x) = x^2 - x - 2$$

Final Answer: (c) $x^2 - x - 2$

Q10: The number of zeroes of the polynomial representing the whole curve, is (2022)

- (a) 4
- (b) 3
- (c) 2
- (d) 1

Ans: (a)

Given curve cuts the x-axis at four distinct points.

So, number of zeroes will be 4.

Q11: The distance between C and G is (2022)

- (a) 4 units
- (b) 6 units
- (c) 8 units
- (d) 7 units

Ans: (b)

Q12: The quadratic polynomial, the sum of whose zeroes is -5 and their product is 6.

(2022)

(a) $x^2 + 5x + 6$

(b) $x^2 - 5x + 6$

(c) $x^2 - 5x - 6$

(d) $-x^2 + 5x + 6$

Ans: (a)

Let α, β be the zeroes of required polynomial $p(x)$.

Given, $\alpha + \beta = -5$ and $\alpha\beta = 6$

$$\therefore p(x) = k[x^2 - (-5)x + 6] = k[x^2 + 5x + 6]$$

Thus, one of the polynomial which satisfy the given condition is $x^2 + 5x + 6$

Previous Year Questions 2021

Q13: If one zero of the quadratic polynomial $x^2 + 3x + k$ is 2 then find the value of k .

(2021)

Ans: Given, polynomial is $f(x) = x^2 + 3x + k$

Since, 2 is zero of the polynomial $f(x)$.

$$\therefore f(2) = 0$$

$$\Rightarrow f(2) = (2)^2 + 3 \times 2 + k$$

$$\Rightarrow 4 + 6 + k = 0$$

$$\Rightarrow k = -10$$

Previous Year Questions 2020

Q14: The degree of polynomial having zeroes -3 and 4 only is (2020)

(a) 2

(b) 1

(c) more than 3

(d) 3

Ans: (a)

Since, the polynomial has two zeroes only. So. the degree of the polynomial is 2.

Q15: If one of the zeroes of the quadratic polynomial $x^2 + 3x + k$ is 2. then the value of k is (2020)

- (a) 10
- (b) - 10
- (c) -7
- (d) -2

Ans: (b)

Given, 2 is a zero of the polynomial

$$p(x) = x^2 + 3x + k$$

$$\therefore p(2) = 0$$

$$\Rightarrow (2)^2 + 3(2) + k = 0$$

$$\Rightarrow 4 + 6 + k = 0 =$$

$$\Rightarrow 10 + k = 0$$

$$\Rightarrow k = -10$$

Q16: The quadratic polynomial, the sum of whose zeroes is -5 and their product is 6 _____ is (2020)

- (a) $x^2 + 5x + 6$
- (b) $x^2 - 5x + 6$
- (c) $x^2 - 5x - 6$
- (d) $-x^2 + 5x + 6$

Ans: (a)

Let α, β be the zeroes of required polynomial $p(x)$

Given, $\alpha + \beta = -5$ and $\alpha\beta = 6$

$$p(x) = k[x^2 - (-5)x + 6]$$

$$= k[x^2 + 5x + 6]$$

Thus, one of the polynomial which satisfy the given condition is $x^2 + 5x + 6$.

Q17: Form a quadratic polynomial, the sum and product of whose zeroes are (-3) and 2 respectively. (CBSE 2020)

Ans: Let α, β be the zeroes of required polynomial Given, $\alpha + \beta = -3$ and $\alpha\beta = 2$

$$\therefore p(x) = k[x^2 - (-3)x + 2] = k(x^2 + 3x + 2)$$

$$\text{For } k = 1, p(x) = x^2 + 3x + 2$$

Hence, one of the polynomial which satisfy the given condition is $x^2 + 3x + 2$.

Q18: The zeroes of the polynomial $x^2 - 3x - m(m + 3)$ are:

- (a) $m, m + 3$
- (b) $-m, m + 3$
- (c) $m, -(m + 3)$
- (d) $-m, -(m + 3)$ (CBSE 2020)

Ans: (b)

Given:

$$x^2 - 3x - m(m + 3) = 0$$

Let's find the zeroes by applying the quadratic formula:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Substitute into the formula:

$$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4 \cdot 1 \cdot (-m(m + 3))}}{2 \cdot 1}$$
$$x = \frac{3 \pm \sqrt{9 + 4m(m + 3)}}{2}$$

Simplify under the square root:

$$x = \frac{3 \pm \sqrt{9 + 4m^2 + 12m}}{2}$$
$$x = \frac{3 \pm \sqrt{(2m + 3)^2}}{2}$$

Taking the square root:

$$x = \frac{3 \pm (2m + 3)}{2}$$

So, the zeroes are $-m$ and $m + 3$.

Thus, the correct answer is (b) $-m, m + 3$.

Previous Year Questions 2019

Q19: Find the value of k such that the polynomial $x^2 - (k + 6)x + 2(2k - 1)$ has sum of its zeroes equal to half of their product. [Year 2019, 3 Marks]

Ans: 7

The given polynomial is $x^2 - (k + 6)x + 2(2k - 1)$

According to the question

Sum of zeroes = $1/2$ (Product of Zeroes):

$$\Rightarrow k + 6 = 1/2 \times 2(2k - 1)$$

$$\Rightarrow k + 6 = 2k - 1$$

$$\Rightarrow k = 7$$