

# IC-260: SIGNALS & SYSTEMS

## TUTORIAL-5: SOLUTION

Please refer the book "SIGNALS & SYSTEMS" (2nd Ed.)

- A. V. OPPENHEIM, A. S. WILLSKY, S. H. NANAB. for

Q.1, Q.2 and Q.4.

Q.1 → Example 5.13.

Q.2 → Example 5.14.

Q.4 - a → Example 9.3B.

b → Similar to Example 9.4 except the  $\sin 3t$ .

$$x(t) = e^{-2t} u(t) + e^{-t} (\sin 3t) u(t)$$

$$= \left[ e^{-2t} + \frac{1}{2j} e^{(1-3j)t} - \frac{1}{2j} e^{(1+3j)t} \right] u(t)$$

Rest is similar to example 9.4.

Q.3

From the given  $x[n]$  &  $y[n]$ , we have to find  $h[n]$  &  $H(e^{j\omega})$ .

$$h[n] \xrightarrow{\mathcal{F}} H(e^{j\omega}) = \frac{Y(e^{j\omega})}{X(e^{j\omega})}$$

\* One can find easily  $Y(e^{j\omega})$  &  $X(e^{j\omega})$  by using the Fourier Transform property.

Then use partial fraction method to split  $H(e^{j\omega})$  and invert it to the time domain to find  $h[n]$ .

Q.5

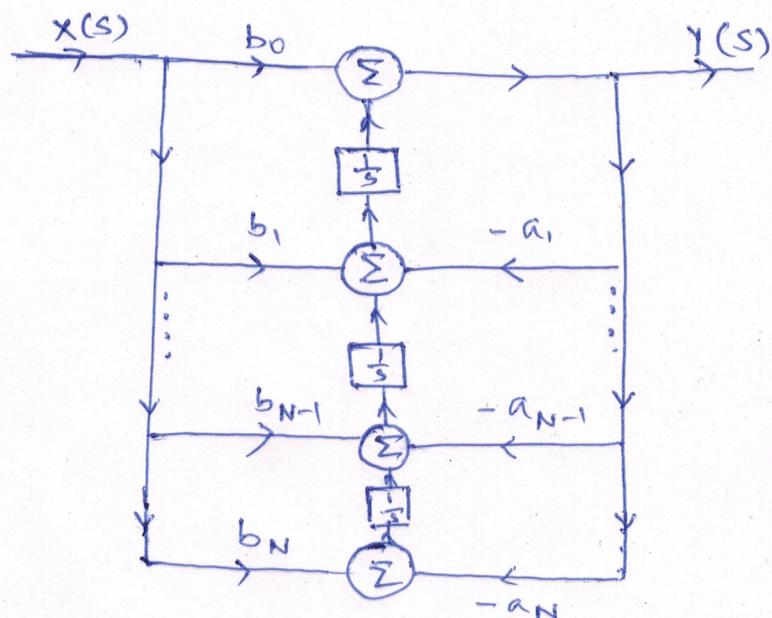
Hint:

→ Find  $y(s)$  &  $x(s)$  using L.T. properties.

→ Find  $H(s)$ , which will be of the form:

$$H(s) = \frac{b_0 s^N + b_1 s^{N-1} + \dots + b_{N-1} s + b_N}{s^N + a_1 s^{N-1} + \dots + a_{N-1} s + a_N}$$

For this block-diagram realization will be:



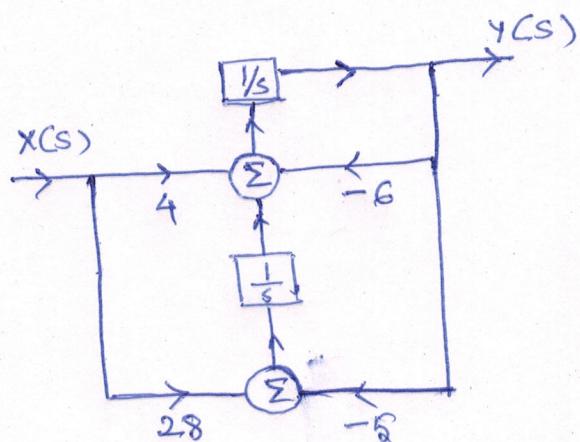
The  $H(s)$  for the problem will be

$$\frac{4s+28}{s^2+6s+5}$$

So, here  $N=2$ ;

$$b_0 = 0, b_1 = 4, b_2 = 28; a_1 = 6, a_2 = 5.$$

According to these parameters the above block diagram can be modified as:



Ans