

# END TERM EXAMINATION

FIFTH SEMESTER [B.TECH.] DECEMBER 2017

Paper Code: IT-301

Subject: Theory of Computation

Time: 3 Hours

Maximum Marks: 60

Note: Attempt any five questions including Q.No 1 which is compulsory. Select one question from each unit.

- Q1 Answer the following questions: (2x10=20)
- (a) State Kleene's theorem. What is a regular expression.
  - (b) Define top down parsing and LL(1) grammar.
  - (c) Write your comment on "Can a machine produce itself?"
  - (d) Define PSPACE and NSPACE complexity classes.
  - (e) Prove that language  $L = \{a^n b^n | n > 0\}$  is not regular.
  - (f) State Pumping lemma for context free language.
  - (g) What is a parse tree
  - (h) Differentiate between polynomial time reduction and Logarithmic space reduction
  - (i) Define Pushdown automata. Give example.

## UNIT-I

- Q2 Prove that regular languages are closed under union and intersection. Let  $M_1$  and  $M_2$  be the two Finite automata's accepting the language  $L_1$  and  $L_2$  respectively. Design automaton to recognize the language. (10)
- (a)  $L_1 \cup L_2$
  - (b)  $L_1 - L_2$
  - (c)  $L_1 \cap L_2$
- Where  $L_1 = \{\text{No. of a's in the string defined over a, b is even}\}$   
And  $L_2 = \{\text{no of b's in the string defined over a, b is odd}\}$

- Q3 Define Nondeterministic automata. Explain the mechanism to convert NFA into DFA. (10)

## UNIT-II

- Q4 Define Pushdown automata. What is instantaneous descriptor. Design a pushdown automata to recognize the language  $L = \{a^n b 2^n | n > 1\}$  (10)
- Q5 Prove that context free languages are closed under union and concatenation. Also prove that intersection of a Context free language and regular language will be a context free language. (10)

## UNIT-III

- Q6 What is Un-decidability problem? Prove that Halting Problem is Undecidable. (10)
- Q7 Prove that Multitape Multithead Turing is computationally equivalent to a Standard Turing Machine. Design a Turing Machine to accept the language  $L = \{a^n b^n | n > 0\}$ . (10)

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**UNIT-IV**

- Q8 Write your views on the following "Every P-class problem is an NP-class problem". Also Prove that clique problem is NP complete. (10)
- Q9 Prove that a problem solvable in the space of  $O(f(n))$  requires worst case time of the order of  $O(2^{f(n)})$  [Make necessary assumptions]. State and Prove Savich theorem. (10)

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# END TERM EXAMINATION

FIFTH SEMESTER [B.TECH.] DECEMBER 2017

Paper Code: IT-301

Time: 3 Hours

Subject: Theory of Computation

Maximum Marks: 75

Note: Attempt any five questions including Q.No 1 which is compulsory. Select one question from each unit.

- Q1 Answer the following questions: (2.5x10=25)
- (a) State Kleene's theorem. What is a regular expression.
  - (b) Define top down parsing and LL(1) grammar.
  - (c) Write your comment on "Can a machine produce itself?"
  - (d) Define PSPACE and NSPACE complexity classes.
  - (e) Prove that language  $L = \{a^n b^n | n > 0\}$  is not regular.
  - (f) State Pumping lemma for context free language.
  - (g) What is a parse tree?
  - (h) Differentiate between polynomial time reduction and Logarithmic space reduction.
  - (i) Define Pushdown automata. Give example.

## UNIT-I

- Q2 Prove that regular languages are closed under union and intersection. Let  $M_1$  and  $M_2$  be the two Finite automata's accepting the language  $L_1$  and  $L_2$  respectively. Design automaton to recognize the language. (12.5)

(a)  $L_1 \cup L_2$

(b)  $L_1 - L_2$

(c)  $L_1 \cap L_2$

Where  $L_1 = \{\text{No. of a's in the string defined over a, b is even}\}$   
And  $L_2 = \{\text{no of b's in the string defined over a, b is odd}\}$

- Q3 Define Nondeterministic automata. Explain the mechanism to convert NDFA into DFA. (12.5)

## UNIT-II

- Q4 Define Pushdown automata. What is instantaneous descriptor. Design a pushdown automata to recognize the language  $L = \{a^n b 2^n | n > 1\}$  (12.5)
- Q5 Prove that context free languages are closed under union and concatenation. Also prove that intersection of a Context free language and regular language will be a context free language. (12.5)

## UNIT-III

- Q6 What is Un-decidability problem? Prove that Halting Problem is Un-decidable. (12.5)
- Q7 Prove that Multitape Multithead Turing is computationally equivalent to a Standard Turing Machine. Design a Turing Machine to accept the language  $L = \{a^n b^n | n > 0\}$ . (12.5)

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**UNIT-IV**

- Q8 Write your views on the following "Every P-class problem is an NP-class problem". Also Prove that clique problem is NP complete. (12.5)
- Q9 Prove that a problem solvable in the space of  $O(f(n))$  requires worst case time of the order of  $O(2^{f(n)})$  [Make necessary assumptions]. State and Prove Savich theorem. (12.5)

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