

END TERM EXAMINATION

SEVENTH SEMESTER [B.TECH./M.TECH.] - DECEMBER 2010

Paper Code: IT401

Subject: Digital Signal Processing

Paper ID: 15401

Time : 3 Hours

Maximum Marks : 60

Note: Attempt five questions including Q.1 which is compulsory.

- Q1 (a) Discuss minimum phase and maximum phase transfer function. (5)
 (b) A linear time invariant system is characterized by system function

$$H(z) = \frac{3 - 4z^{-1}}{1 - 3.5z^{-1} + 1.5z^{-2}}$$
. Determine $h(n)$. (5)
 (c) Check if the system is LTI or not (i) $y(n) = \sum_{k=-\infty}^n x(k)$ (ii) $y(n) = x(-n)$. (5)
 (d) Derive the relationship between DFT (i) Z-transform (ii) Fourier series. (5)
- Q2 (a) Compute the convolution $y(n) = x(n) * h(n)$, $x(n) = \begin{cases} 1 & n = -2, 0, 1 \\ 2 & n = -1 \\ 0 & \text{elsewhere} \end{cases}$,
 $h(n) = \delta(n) - \delta(n-1) + \delta(n-4) + \delta(n-5)$. (8)
 (b) Determine whether the signals are energy or power signal and also compute its value (i) $x(n) = e^{2n}u(n)$ (ii) $x(n) = (1/3)^n u(n)$. (2)
- Q3 (a) Check if the following signals are causal or not:- (3)
 (i) $y(n) = x(n) + x^2(n-1)$
 (ii) $y(n) = x(2n)$
 (iii) $y(n) = \sum_{k=-\infty}^{n+1} x(k)$
 (b) Discuss sampling theory in frequency domain. (2)
 (c) Find the cross correlation of two finite length sequences $x(n) = \{1, 2, 1, 1\}$ and $y(n) = \{1, 1, 2, 1\}$. Also, show that $r_{xy}(l) = x(l) * y(-l)$. (5)
- Q4 (a) Given the sequences $x_1(n) = \{1, 2, 3, 4\}$, $x_2(n) = \{1, 1, 2, 2\}$. Compute- (8)
 (i) $x_3(n) = x_1(n) \cdot x_2(n)$.
 (ii) Linear convolution using circular convolution.
 (b) Derive the Parseval's theorem. (2)
- Q5 (a) Determine the causal signal $x(n)$ having Z-transform

$$X(Z) = \frac{1}{(1 - 2z^{-1})(1 - z^{-1})^2}$$
. (6)
 (b) Prove the following property of DFT where $X(K)$ is the N point DFT of $x(n)$. If $x(n)$ is real and even then $X(K)$ is real and even. (4)
- Q6 Find the DFT of a sequence $x(n) = \{1, 2, 3, 4, 4, 3, 2, 1\}$ using OIT algorithm. Draw the structure and also show bit reversal. (10)
- Q7 Find the IDFT of the sequence $X(K) = \{4, 1 - j2.414, 0, 1 - j0.414, 0, 1 + j0.414, 0, 1 + j2.414\}$ using DIF algorithm. (10)

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- Q8 Draw the direct form II, cascade and parallel structure for the system described by the difference equation

$$y(n) = \frac{3}{4}y(n-1) - \frac{1}{8}y(n-2) + x(n) + \frac{1}{3}x(n-1). \quad (10)$$

- Q9 (a) Explain the design of IIR filter using (i) impulse invariance method (ii) Bilinear transformation method. (4)

- (b) Realize the following system function using minimum no. of multipliers:- (6)

(i) $H(z) = 1 + \frac{1}{3}z^{-1} + \frac{1}{4}z^{-2} + \frac{1}{4}z^{-3} + \frac{1}{3}z^{-4} + z^{-5}$

(ii) $H(z) = (1 + z^{-1}) \left(1 + \frac{1}{2}z^{-1} + \frac{1}{2}z^{-2} + z^{-3} \right)$
