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Subject: Design and analysis of algorithm

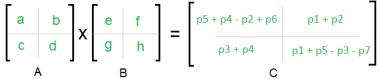
Practical: Experiment on Strassens matrix multiplication

Theory:

$$p1 = a(f - h)$$
 $p2 = (a + b)h$
 $p3 = (c + d)e$ $p4 = d(g - e)$
 $p5 = (a + d)(e + h)$ $p6 = (b - d)(g + h)$
 $p7 = (a - c)(e + f)$

The A \times B can be calculated using above seven multiplications.

Following are values of four sub-matrices of result C



A, B and C are square metrices of size N x N

a, b, c and d are submatrices of A, of size N/2 x N/2 $\,$

e, f, g and h are submatrices of B, of size N/2 x N/2 $\,$

p1, p2, p3, p4, p5, p6 and p7 are submatrices of size N/2 x N/2 $\,$

Procedures:

Divide a matrix of order of 2*2 recursively till we get the matrix of 2*2.

Use the previous set of formulas to carry out 2*2 matrix multiplication.

In this eight multiplication and four additions, subtraction are performed.

Combine the result of two matrixes to find the final product or final matrix.

Algorithm:

- 1. Take inputs as matrix1 and matrix2
- 2. elements of matrix 1: a11, a12, a13, a14

elements of matrix 2: b11, b12, b13, b14

3. perform following addition:

$$D1 = (a11 + a22) * (b11 + b22)$$

$$D2 = (a21 + a22)*b11$$

$$D3 = (b12 - b22)*a11$$

$$D4 = (b21 - b11)*a22$$

$$D5 = (a11 + a12)*b22$$

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D6 = (a21 - a11) * (b11 + b12)

D7 = (a12 - a22) * (b21 + b22)

C00= d1 + d4 - d5 + d7

C01 = d3 + d5

C10 = d2 + d4

C11 = d1 + d3 - d2 - d6

4. print the reasultant matrix
```

Program:

```
#include<stdio.h>
int main()
  int i,j,array1[2][2],array2[2][2];
  printf ("first matrix\n");
  for (i=0;i<2;i++)
     for (j=0;j<2;j++)
       scanf ("%d",&array1[i][j]);
   for (i=0;i<2;i++)
     for (j=0;j<2;j++)
       printf ("%d \t",array1[i][j]);
  printf ("\n");
  printf ("second matrix\n");
  for (i=0;i<2;i++)
```

```
for (j=0;j<2;j++)
       scanf ("%d",&array2[i][j]);
   for (i=0;i<2;i++)
     for (j=0;j<2;j++)
       printf ("%d \t",array2[i][j]);
  printf ("\n");
 *printf ("%d\n",array1[0][0]);
printf ("%d\n",array1[0][1]);
printf ("%d\n",array1[1][0]);
printf ("%d\n",array1[1][1]);
printf ("%d\n",array2[0][0]);
printf ("%d\n",array2[0][1]);
printf ("%d\n",array2[1][0]);
printf ("%d\n",array2[1][1]);*/
int s1[1],s2[1],s3[1],s4[1],s5[1],s6[1],s7[1],s8[1],s9[1],s10[1];
s1[0] = array2[0][1] - array2[1][1];
s2[0] = array1[0][0] + array1[0][1];
s3[0] = array1[1][0] + array1[1][1];
s4[0] = array2[1][0] - array2[0][0];
s5[0] = array1[0][0] + array1[1][1];
s6[0] = array2[0][0] + array2[1][1];
s7[0] = array1[0][1] - array1[1][1];
s8[0] = array2[1][0] + array2[1][1];
s9[0] = array1[0][0] - array1[1][0];
s10[0] = array2[0][0] + array2[0][1];
int p1[1], p2[1], p3[1], p4[1], p5[1], p6[1], p7[1];
p1[0] = array1[0][0] * s1[0];
p2[0] = s2[0] * array2[1][1];
p3[0] = s3[0] * array2[0][0];
p4[0] = array1[1][1] * s4[0];
```

```
p5[0] = s5[0] * s6[0];

p6[0] = s7[0] * s8[0];

p7[0] = s9[0] * s10[0];

int c11[1], c12[1], c21[1], c22[1];

printf ("\nMultiplication of two metrices\n");

c11[0] = p5[0] + p4[0] - p2[0] + p6[0];

c12[0] = p1[0] + p2[0];

c21[0] = p3[0] + p4[0];

c22[0] = p5[0] + p1[0] - p3[0] - p7[0];

printf ("%d\t",c11[0]);

printf ("%d\n",c12[0]);

printf ("%d\n",c22[0]);

return 0;

}
```

Output:

```
first matrix
10 20
30 40
10 20
30 40
second matrix
20 40
60 80
20 40
60 80
Multiplication of two metrices
1400 2000
3000 4400

...Program finished with exit code 0
Press ENTER to exit console.
```

Observation:

Srassens matrix multiplication reduces the number of multiplication as it takes more time complexity than the addition and subtraction. So, operations are replaced by addition. For the big metrics, this method is very useful and fast.

Time complexity of Srassen's Matrix multiplication:

$$T(n) = 7T(n/2) + O(n^2) = O(n^{\log(7)}).$$

Conclusion:

In this practical, I performed the Strassen's Matrix multiplication where I multiplied 2X2 matrix using above mentioned method. In this method, number of multiplication operations get reduced and reduces the time taken by the algorithm, number of operations also reduces.