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**Subject:** Design and analysis of algorithm

**Practical:** Experiment on Strassen's matrix multiplication

**Theory:**

$$\begin{aligned}p1 &= a(f - h) & p2 &= (a + b)h \\p3 &= (c + d)e & p4 &= d(g - e) \\p5 &= (a + d)(e + h) & p6 &= (b - d)(g + h) \\p7 &= (a - c)(e + f)\end{aligned}$$

The A x B can be calculated using above seven multiplications.  
Following are values of four sub-matrices of result C

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \times \begin{bmatrix} e & f \\ g & h \end{bmatrix} = \begin{bmatrix} p5 + p4 - p2 + p6 & p1 + p2 \\ p3 + p4 & p1 + p5 - p3 - p7 \end{bmatrix}$$

A                      B                      C

A, B and C are square matrices of size N x N  
a, b, c and d are submatrices of A, of size N/2 x N/2  
e, f, g and h are submatrices of B, of size N/2 x N/2  
p1, p2, p3, p4, p5, p6 and p7 are submatrices of size N/2 x N/2

**Procedures:**

Divide a matrix of order of 2\*2 recursively till we get the matrix of 2\*2.

Use the previous set of formulas to carry out 2\*2 matrix multiplication.

In this eight multiplication and four additions, subtraction are performed.

Combine the result of two matrixes to find the final product or final matrix.

**Algorithm:**

1. Take inputs as matrix1 and matrix2
2. elements of matrix 1: a11, a12, a13, a14  
elements of matrix 2: b11, b12, b13, b14
3. perform following addition:  
 $D1 = (a11 + a22) * (b11 + b22)$   
 $D2 = (a21 + a22)*b11$   
 $D3 = (b12 - b22)*a11$   
 $D4 = (b21 - b11)*a22$   
 $D5 = (a11 + a12)*b22$

$$D6 = (a_{21} - a_{11}) * (b_{11} + b_{12})$$

$$D7 = (a_{12} - a_{22}) * (b_{21} + b_{22})$$

$$C_{00} = d_1 + d_4 - d_5 + d_7$$

$$C_{01} = d_3 + d_5$$

$$C_{10} = d_2 + d_4$$

$$C_{11} = d_1 + d_3 - d_2 - d_6$$

4. print the resultant matrix

### Program:

```
#include<stdio.h>
int main()
{
    int i,j,array1[2][2],array2[2][2];
    printf ("first matrix\n");
    for (i=0;i<2;i++)
    {
        for (j=0;j<2;j++)
        {
            scanf ("%d",&array1[i][j]);
        }
    }

    for (i=0;i<2;i++)
    {
        for (j=0;j<2;j++)
        {
            printf ("%d\t",array1[i][j]);
        }
        printf ("\n");
    }

    printf ("second matrix\n");

    for (i=0;i<2;i++)
    {
```

```

        for (j=0;j<2;j++)
        {
            scanf ("%d",&array2[i][j]);
        }

    }

    for (i=0;i<2;i++)
    {
        for (j=0;j<2;j++)
        {
            printf ("%d\t",array2[i][j]);
        }
        printf ("\n");
    }

/*printf ("%d\n",array1[0][0]);
printf ("%d\n",array1[0][1]);
printf ("%d\n",array1[1][0]);
printf ("%d\n",array1[1][1]);

printf ("%d\n",array2[0][0]);
printf ("%d\n",array2[0][1]);
printf ("%d\n",array2[1][0]);
printf ("%d\n",array2[1][1]);*/

int s1[1],s2[1],s3[1],s4[1],s5[1],s6[1],s7[1],s8[1],s9[1],s10[1];
s1[0] = array2[0][1] - array2[1][1];
s2[0] = array1[0][0] + array1[0][1];
s3[0] = array1[1][0] + array1[1][1];
s4[0] = array2[1][0] - array2[0][0];
s5[0] = array1[0][0] + array1[1][1];
s6[0] = array2[0][0] + array2[1][1];
s7[0] = array1[0][1] - array1[1][1];
s8[0] = array2[1][0] + array2[1][1];
s9[0] = array1[0][0] - array1[1][0];
s10[0] = array2[0][0] + array2[0][1];

int p1[1], p2[1], p3[1], p4[1], p5[1], p6[1], p7[1];
p1[0] = array1[0][0] * s1[0];
p2[0] = s2[0] * array2[1][1];
p3[0] = s3[0] * array2[0][0];
p4[0] = array1[1][1] * s4[0];

```

```

p5[0] = s5[0] * s6[0];
p6[0] = s7[0] * s8[0];
p7[0] = s9[0] * s10[0];

int c11[1], c12[1], c21[1], c22[1];
printf ("\nMultiplication of two metrices\n");
c11[0] = p5[0] + p4[0] - p2[0] + p6[0];
c12[0] = p1[0] + p2[0];
c21[0] = p3[0] + p4[0];
c22[0] = p5[0] + p1[0] - p3[0] - p7[0];
printf ("%d\t",c11[0]);
printf ("%d\n",c12[0]);
printf ("%d\t",c21[0]);
printf ("%d\n",c22[0]);
    return 0;
}

```

### Output:

```

first matrix
10 20
30 40
10      20
30      40
second matrix
20 40
60 80
20      40
60      80

Multiplication of two metrices
1400      2000
3000      4400

...Program finished with exit code 0
Press ENTER to exit console.

```

### Observation:

Strassen's matrix multiplication reduces the number of multiplication as it takes more time complexity than the addition and subtraction. So, operations are replaced by addition. For the big metrics, this method is very useful and fast.

Time complexity of Strassen's Matrix multiplication:

$$T(n) = 7T(n/2) + O(n^2) = O(n^{\log(7)}).$$

**Conclusion:**

In this practical, I performed the Strassen's Matrix multiplication where I multiplied  $2 \times 2$  matrix using above mentioned method. In this method, number of multiplication operations get reduced and reduces the time taken by the algorithm, number of operations also reduces.