

Q.1) Five terminals on an on-line computer system are attached to a communication line to the central computer system. The probability that any terminal is ready to transmit is 0.95. Let X denote the number of ready terminals.

(a) Find the probability of getting exactly 3 ready terminals.

Ans `>dbinom(x = 3, size = 5, prob = 0.95)`

[1] 0.02143438

(b) Find all the probabilities.

Ans `>x <- 0:5`

`>dbinom(x, size = 5, prob = 0.95)`

[1] 0.0000003125

[2] 0.0000296875

[3] 0.0011281250

[4] 0.0214343750

[5] 0.2036265625

[6] 0.7737809375

Q.2) It is known that 20% of integrated circuit chips on a production line are defective. To maintain and monitor the quality of the chips, a sample of twenty chips is selected at regular intervals for inspection. Let X denote the number of defectives found in the sample. Find the probability of different number of defective found in the sample?

`>x <- 0:20`

`>dbinom(x, size = 20, prob = 0.2)`

[1] 1.152922e-02

[2] 5.764608e-02

[3] 1.369094e-01

[4] 2.053641e-01

[5] 2.181994e-01

[6] 1.745595e-01

[7] 1.090997e-01

[8] 5.454985e-02

[9] 2.216088e-02

[10] 7.386959e-03

[11] 2.031414e-03

[12] 4.616849e-04

```
[13]8.656592e-05
[14]1.331783e-05
[15]1.664729e-06
[16] 1.664729e-07
[17]1.300570e-08
[18]7.650410e-10
[19]3.187671e-11
[20]8.388608e-13
[21] 1.048576e-14
```

Q.3) It is known that 1% of bits transmitted through a digital transmission are received in error. One hundred bits are transmitted each day. Find the probability of different number of bits found in error each day.?

Ans

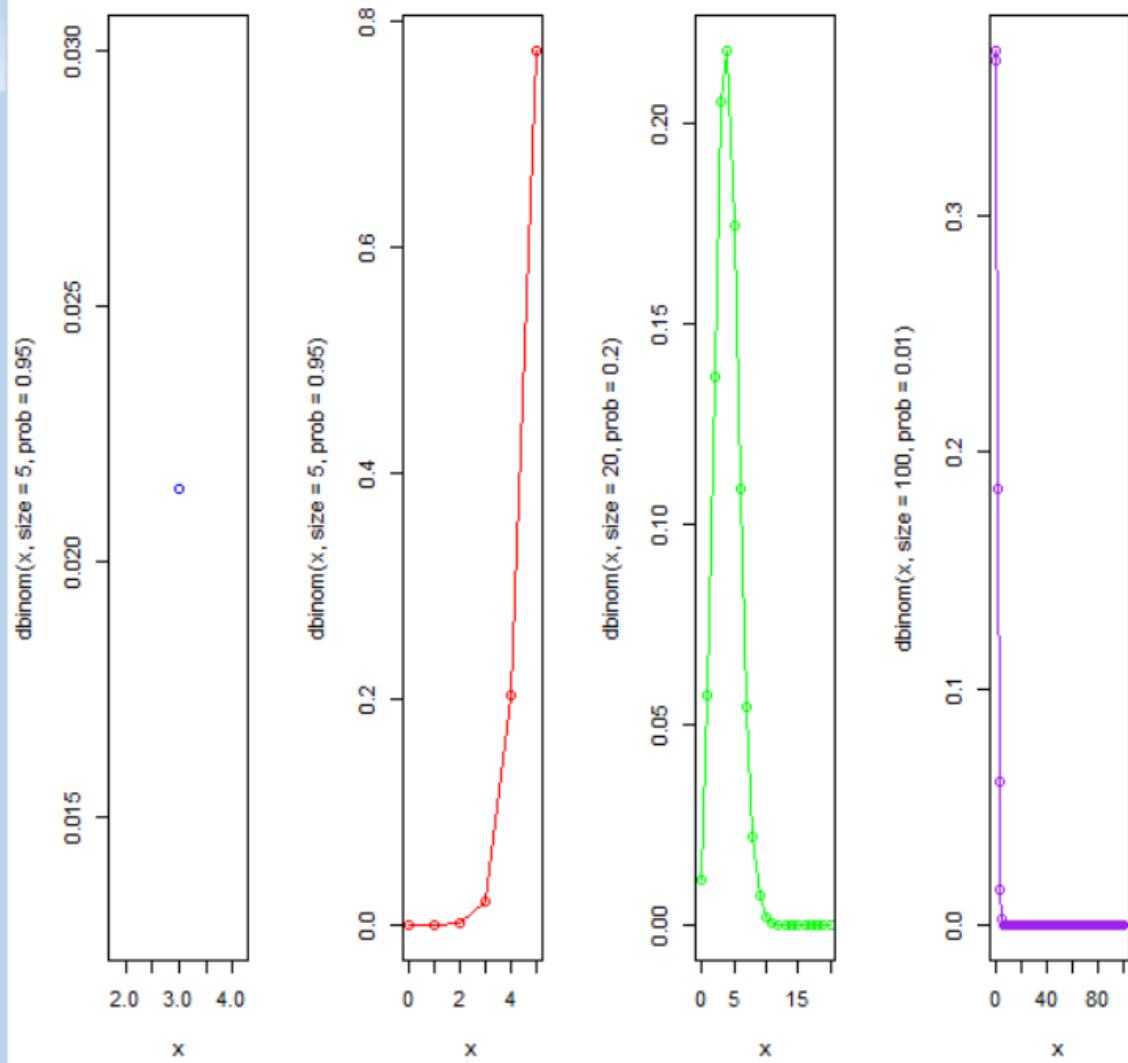
```
>x <- 0:100
>dbinom(x, size = 100, prob = 0.01)
[1] 3.660323e-01 3.697296e-01 1.848648e-01 6.099917e-02
1.494171e-02
[6] 2.897787e-03 4.634508e-04 6.286346e-05 7.381694e-06
7.621951e-07
[11] 7.006036e-08 5.790112e-09 4.337710e-10 2.965956e-11
1.861747e-12
[16] 1.078184e-13 5.785707e-15 2.887697e-16 1.344999e-17
5.863367e-19
[21] 2.398650e-20 9.230014e-22 3.347893e-23 1.146841e-24
3.716614e-26
[26] 1.141263e-27 3.325359e-29 9.206008e-31 2.424382e-32
6.079954e-34
[31] 1.453457e-35 3.315151e-37 7.220499e-39 1.502889e-40
2.991491e-42
[36] 5.698078e-44 1.039212e-45 1.815713e-47 3.040667e-49
4.882708e-51
[41] 7.521343e-53 1.111802e-54 1.577594e-56 2.149411e-58
2.812590e-60
[46] 3.535467e-62 4.269888e-64 4.955382e-66 5.526836e-68
5.924459e-70
[51] 6.103988e-72 6.044749e-74 5.753549e-76 5.263395e-78
4.627377e-80
[56] 3.909263e-82 3.173103e-84 2.474154e-86 1.852815e-88
1.332276e-90
```

[61] 9.195842e-93 6.090970e-95 3.870118e-97 2.357936e-99
 1.376951e-101
 [66] 7.703225e-104 4.126306e-106 2.115098e-108 1.036813e-110
 4.856976e-113
 [71] 2.172673e-115 9.273039e-118 3.772701e-120 1.461680e-122
 5.387028e-125
 [76] 1.886367e-127 6.267832e-130 1.973343e-132 5.877609e-135
 1.653336e-137
 [81] 4.383845e-140 1.093365e-142 2.558996e-145 5.605686e-148
 1.145943e-150
 [86] 2.178859e-153 3.838722e-156 6.239651e-159 9.310773e-162
 1.268066e-164
 [91] 1.565513e-167 1.737722e-170 1.717116e-173 1.492009e-176
 1.122294e-179
 [96] 7.159768e-183 3.766713e-186 1.568973e-189 4.851495e-193
 9.900000e-197
 [101] 1.000000e-200

Q.4) Plot all of the above problems in a single window for random variable and respective Probabilitydistribution.

```

>par(mfrow = c(1,4))
>x = 3
>plot(x,dbinom(x, size = 5, prob = 0.95),type = 'o', col = 'blue')
>x <- 0:5
>plot(x,dbinom(x, size = 5, prob = 0.95),type = 'o', col = 'red')
>x <- 0:20
>plot(x,dbinom(x, size = 20, prob = 0.2),type = 'o', col = 'green')
>x <- 0:100
>plot(x,dbinom(x, size = 100, prob = 0.01),type = 'o', col = 'purple')
  
```



Q.5) For Q.No. 1 Find $P(X = 3)$ and $P(X > 3)$. For Q. No. 2 Find $P(X = 4)$ and $P(X > 4)$. Find all the cumulative probabilities and round to 4 decimal places.

```
>y <- 1-pbinom(3, 5, 0.95)
>y
[1] 0.9774075
>a <- dbinom(x = 4, size = 20, prob = 0.2)
>a
[1] 0.2181994
>round(a,4)
[1] 0.2182
>g <- 4
>q <- 1- pbinom(g, size = 20, prob = 0.2)
>q
[1] 0.3703517
>round(q,4)
[1] 0.3704
```

Q.6) The probability that a patient recover from a rare blood disease is 0.4. If 15 people are known to have contracted this disease, what is the probability that

(a) at least 10 survive,

```
>f = 9
>c <- 1 - pbinom(f, size = 15, prob = 0.4)
>c
[1] 0.0338333
```

(b) from 3 to 8 survive,

```
>j = 8
>g = 3
>n <- pbinom(j, size = 15, prob = 0.4)
>n
[1] 0.9049526
>m <- n - pbinom(g, size = 15, prob = 0.4)
>m
[1] 0.8144507
```

(c) exactly 5 survive?

```
>i=5
```

```
>c <- 1 - pbinom(i, size = 15, prob = 0.4)
```

```
>c
```

```
[1] 0.5967844
```