

## SORTING

→ Arranging elements of an array in ascending order.

- Classification;
  - 1) Number of Comparisons
  - 2) No. of Swaps
  - 3) Memory Usage
  - 4) Recursion
  - 5) Stability & Adaptability

→ Internal Sort (In-Sort)

(use main memory exclusively)

→ External Sort (Out-Sort)

(uses external memory)

### 1) BUBBLE SORT (sinking sort)

→ Traverse through the list in adjacent manner one by one if wrongly placed swaps them. Performs traversing till each element is placed correctly at end after one looping.

Time Complexity:  $O(n^2)$  (Best) (Worst Case)

Space " :  $O(1)$  auxiliary

## Implementation;

```
void bubbleSort ( int a[], int size)
{
    for ( int step = 0; step < size-1; step++)
    {
        for (int j = 0; j < size-step-1; j++)
        {
            if ( a[j] > a[j+1])
            {
                // swap; ( swaps element )
            }
        }
    }
}
```

\* In improved version best case can be resolved to  $O(n)$  by adding a variable swapped if false, <sup>inner</sup> loop will not execute further

```
→ void bubbleSort (int a[], int size) {
    int i, j, swapped = 1, temp;
    for (i = size-1; i > 0 && swapped; i--) {
        swapped = 0;
        for (j = 0; j < i-1; j++) {
            if ( a[j] > a[j+1] ) {
                swap;
                swapped = 1;
            }
        }
    }
}
```

} if cond. executes on one looping the swapped = 1 else the list is sorted



- SELECTION SORT;  $\rightarrow$  Takes smallest element & exchange it with first element in the list & continues
- $\rightarrow$  Similarly, takes largest element & exchange it with last element
- $\rightarrow$  Improves on bubble sort by making one exchange for every pass through the list.

### Advantages

- easy implementation
- In-place sorting (i.e. no additional space required)

### Dis-advantage

- Time  $\rightarrow O(n^2)$

### Implementation

```
void SelectionSort (int a[], int size) {
    int i, j, min, temp;
    for (i = 0; i < size - 1; i++) {
        min = i;
        for (j = i + 1; j < size; j++) {
            if (a[j] < a[min])
                min = j;
        }
        temp = a[min];
        a[min] = a[i];
        a[i] = temp;
    }
}
```

or

```
void selectionSort (int a[], int size) {
```

```
    int i, j, max, temp;
```

```
    for (i = size - 1; i >= 0; i--) {
```

```
        max = i;
```

```
        for (j = sizei-1; j >= 0; j--) {
```

```
            if (a[j] > a[max])
```

```
                max = j;
```

```
        }  
        temp = a[max];
```

```
        a[max] = a[i];
```

```
        a[i] = temp;
```

```
    }
```

INSERTION SORT; picks element 1-by-1 and places it  
to right position where it belongs  
in sorted list.

- Simple & efficient comparison sort.
- Each iteration removes an element from I/P list and inserts it into sorted sublist.
- In-place - requires a constant amount  $O(1)$  of additional memory.



## Implementation,

```
void insertionSort (int a[], int size) {  
    for (int i = 1; i <= size - 1; i++) {  
        int key = a[i]; j = i;  
        for while (a[j-1] > key && j >= 1) {  
            a[j] = a[j-1];  
            j--;  
        }  
        a[j] = key; }  
}
```

example;

1 191 1029

4	9	11	45	27
		↑		↑
		(Sorted Sublist)		(inserted to sorted Sublist)

→ 4 9 11 45 45 (27 < 45 copy 45 at A[4])

→ 4 9 11 45 45 (next is 11, 27 > 11, so

→ 4 9 11 27 45 (copy 27 at A[3])

(2)

$\rightarrow i=1$  (3 8 4 2 9 1)

$j=1$

(3 > 8)  $\times \rightarrow$  (3 8 4 2 9 1)

$i=2=j$

key=4 { (8 > 4)  $\rightarrow$  (3 8 8 2 9 1) (copy 8 at a[2])  
 $j=1$   
(3 > 4)  $\times \rightarrow$  (3 4 8 2 9 1) (insert 4 at a[1])

key=2 {  $i=3=j$   
(8 > 2)  $\rightarrow$  (3 4 8 8 9 1) (copy 8 at a[3])  
 $j=2$   
(4 > 2)  $\rightarrow$  (3 4 4 8 9 1) (copy 4 at a[2])  
 $j=1$   
(3 > 2)  $\rightarrow$  (3 3 4 8 9 1) (copy 3 at a[1])  
 $j=0$   $\rightarrow$  (2 3 4 8 9 1) (insert 2 at a[0])

$i=4=j$   
key=9 (8 > 9)  $\times$  (2 3 4 8 9 1)

key=1 {  $i=5=j$   
(9 > 1) (2 3 4 8 9 9) (copy 9 at a[5])  
 $j=4$   
(8 > 1) (2 3 4 8 8 9) (copy 8 at a[4])  
 $j=3$   
(4 > 1) (2 3 4 4 8 9) (copy 4 at a[3])  
 $j=2$   
(3 > 1) (2 3 3 4 8 9) (copy 3 at a[2])  
 $j=1$   
(2 > 1) (2 2 3 4 8 9) (copy 2 at a[1])  
 $j=0$

(1 2 3 4 8 9) (inserts 9 at a[0])



- Insertion sort is used when data is nearly sorted or when  $\Delta p$  size is small and due to its stability (low overhead)

→ Time Complexity  $\rightarrow T(n) = \theta(1) + \theta(2) + \dots + \theta(n-1)$   

$$T(n) = \theta\left(\frac{n(n-1)}{2}\right)$$

$T(n) = \theta(n^2)$  [Best/Worst Case]

→ Space Complexity  $\rightarrow \theta(n^2)$  total,  $\theta(1)$  auxiliary

- Shell Sort; (Diminishing increment sort)  
 $\hookrightarrow$   $n$ -gap insertion sort

- Shell sort makes several passes & uses various gaps b/w adjacent elements, variation in shell sort is to avoid comparing <sup>adjacent</sup> elements until last step, so effectively performs insertion sort.

- let the gap be of  $\frac{\text{size}}{2}$  & decrement of  $\frac{1}{2}$  by every looping.

- Swap the values

- at gap=1, shell sort will perform insertion sort

Example;

gap = 3

34 1 42 8 23 6

34 ————— 8 (Sort 8 & 34)

1 ————— 23

42 ————— 6 (Sort 42 & 6)

gap = 1

perform

insertion

sort

→ 8 1 6 34 23 42

→ 8 8 6 34 23 42

→ ① 8 8 34 23 42

→ 1 ⑥ 8 34 23 42

→ 1 6 8 34 34 42

→ 1 6 8 ② 34 42 (Sorted)

Complexity;

Space;

$O(1)$  auxiliary

Time;

$O(n \log^2 n)$  (best case)

$O(n^2)$  (worst case)

- Also known as inse n-gap insertion sort.



## • Merge Sort;

### Implementation:

```
void ShellSort (int a[], int size) {
```

```
    int i, j, h, v;
```

```
    for (h = 1; h < size; h = 3 * h + 1;
```

```
        while (h < size / 3)
```

```
            h = 3 * h + 1;
```

} used to calculate gap  
b/w elements

```
    for (; h > 0; h = (h - 1) / 3) {
```

```
        for (i = h; i < size; i++) {
```

```
            v = a[i]; j = i;
```

```
            while (a[j - h] > v && j > h - 1) {
```

```
                a[j] = a[j - h];
```

```
                j -= h;
```

```
            a[j] = v;
```

```
        }
```

```
    }
```

Performing Insertion  
sort at h gap in  
given array

- In place algorithm.

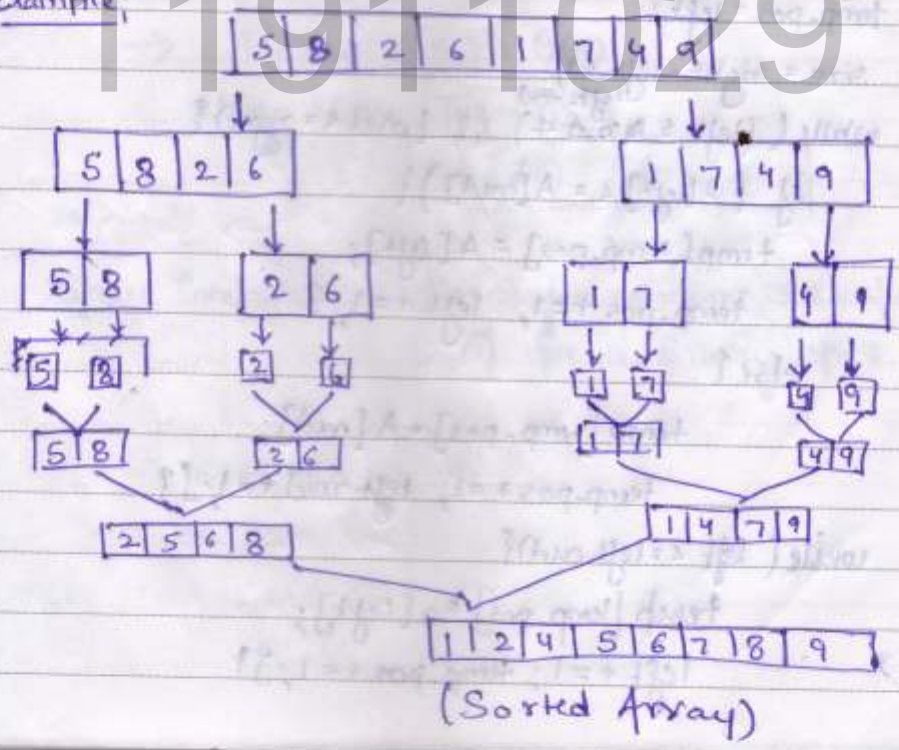
- Average Complexity;  $O(n^2 \log^2 n)$  or  $O(n^{3/2})$   
for best case;  $O(n)$

• MERGE SORT; is an example of divide & conquer strategy.

- Divides the array into equal halves & then combine them in sorted way.

- Recursive algo that splits array into  $\frac{1}{2}$ .

Example;





Implementation: void Mergesort(int a[], int temp[], int left, int right)

```

{
    int mid;
    if (right > left) {
        mid = (right + left) / 2;
        Mergesort(A, temp, left, mid);
        Mergesort(A, temp, mid + 1, right);
        Merge(A, temp, left, mid + 1, right);
    }
}

void Merge(int a[], int temp[], int left, int mid, int right) {
    int i, size, temp_pos;
    int left_end = mid - 1;
    temp_pos = left;
    size = right - left + 1;
    while (left <= left_end && mid <= right) {
        if (A[left] <= A[mid]) {
            temp[temp_pos] = A[left];
            temp_pos++; left++;
        }
        else {
            temp[temp_pos] = A[mid];
            temp_pos++; left = mid++;
        }
    }
    while (left <= left_end) {
        temp[temp_pos] = A[left];
        left++; temp_pos++;
    }
    while (mid <= right) {
        temp[temp_pos] = A[mid];
        mid++; temp_pos++;
    }
}

```

while (mid <= right) {

temp[temp\_pos] = a[mid];

mid += 1; temp\_pos += 1; }

for (i = 0; i < size; i++) {

a[right] = temp[right];

right = right - 1;

Yash Jain

— Out-place algorithm as it needs temp array to assign sorted values.

→  $T(n) = 2T\left(\frac{n}{2}\right) + O(n)$

Using Master Theorem;

$$T(n) = O(n \log n)$$

Space Complexity;  $O(\log n)$  for runtime stack space  
 $O(n)$  for auxiliary space.



## Quick Sort

- famous comparison based algorithm.
- sorts using divide & conquer strategy.
- No additional storage required as it is in-place algorithm like mergeSort.

- The only disadvantage is worst-case time complexity is  $O(n^2)$ .

→ Divide & Conquer Strategy:

- first select the first element of list as pivot value.

- The pivot value roles to assist the splitting of list into 2-sublists.

- After sorting, the pivot value position is referred as partition point.

- All the elements in first sublist must be smaller than pivot value &

- In 2<sup>nd</sup> list must be greater than pivot value

Conquer: The two sublist sorted by recursive calls & then to quick sort

## ALGO. IMPLEMENTATION;

```
void quickSort (int A[], int low, int high) {
```

```
    int pivot;
```

```
    if (high > low) {
```

```
        pivot = partition (A, low, high);
```

```
        quickSort (A, low, pivot-1);
```

```
        quickSort (A, pivot+1, high);
```

```
    }
```

```
int partition (int A[], int low, int high) {
```

```
    int left, right, pivot_value = A[low];
```

```
    left = low;
```

```
    right = high;
```

```
    while (left < right) {
```

```
        while (A[left] <= pivot_value)
```

```
            left++;
```

```
        while (A[right] > pivot_value)
```

```
            right--;
```

```
        if (left < right)
```

```
            swap (A[left], A[right]);
```

```
    } A[low] = A[right]; // Swapping the pivot-value to
```

```
    A[right] = pivot_value; // partition point
```

```
    return right;
```



Example;

→ 50 17 76 9 18 63 5  
↑ pivot ↑ left ↑ right

(Moves) → 50 17 76 9 18 63 5  
(left++) ↑ pivot ↑ left ↑ right  
(left will stop)

(right will move if  $50 < 18$ ) → 50 17 76 9 18 63 5

Swaps (76, 5) ↑ pivot ↑ left ↑ right

(50 > 5) → 50 17 5 9 18 63 76  
left++ ↑ pivot ↑ left ↑ right

50 > 9 → 50 17 5 9 18 63 76  
left++ ↑ pivot ↑ left ↑ right

50 > 18 → 60 17 5 9 18 63 76  
left++ ↑ pivot ↑ left ↑ right

50 < 63 → 50 17 5 9 18 63 76  
left will stop ↑ pivot ↑ left ↑ right

(right (50 > 76) X)  
(right --) ↑ pivot ↑ left ↑ right

## BINARY SEARCH TREES; (BST)

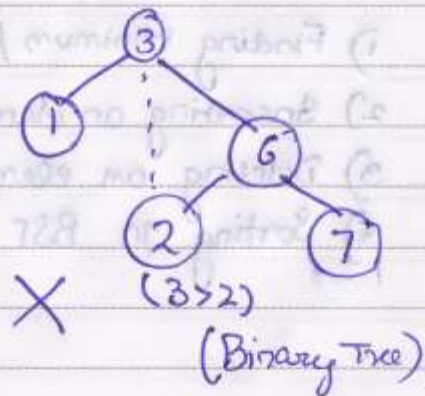
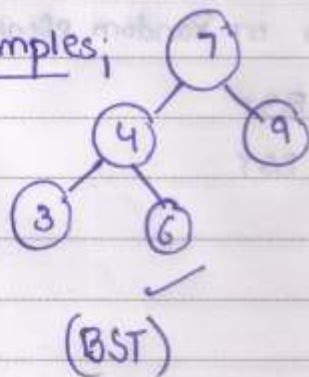
- In Binary Trees there is no node restrictions i.e. why worst case complexity of search is  $O(n)$ .
- whereas in BST imposing some restrictions on node we make worst case complexity of search  $O(\log n)$ .

- BST Property, follows that left subtree data should be less than root data.

- & right subtree data should be greater than root data.

- Implies on all nodes in BST.

Examples;





## • BST Declaration;

```
struct BST {
```

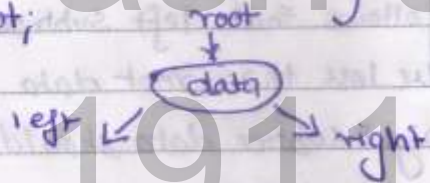
```
    int data;
```

```
    struct BST * left;
```

```
    struct BST * right;
```

```
} *root;
```

Structure of  
BST



## • Operations on BST;

- 1) Finding Minimum / Maximum or Random element in BST.
- 2) Inserting an element in BST
- 3) Deleting an element in BST
- 4) Sorting in BST