

Assignment 2

Yash R Ramteke
bt21btech11006

Question: Determine the binomial distribution where mean is 9 and standard deviation is $\frac{3}{2}$. Also, find the probability of obtaining at most one success.

Solution: For binomial distribution :

Given, Mean = 9 and Standard Deviation(S.D) = $\frac{3}{2}$

$$\text{Mean} = np = 9 \quad (1)$$

$$\text{Variance} = (\text{S.D.})^2 = npq = \frac{9}{4} \quad (2)$$

By substituting equation(1) in equation(2):

$$q = \frac{1}{4} \quad (3)$$

Since, $p = 1 - q$

$$p = 1 - \frac{1}{4} = \frac{3}{4} \quad (4)$$

Using equation (4) in equation (1):

$$n = \frac{9}{p} = \frac{4 \times 9}{3} = 12 \quad (5)$$

Thus Binomial distribution is:

$$\sum_{x=0}^n P(x) = \sum_{x=0}^n \binom{n}{x} p^x (1-p)^{n-x} \quad (6)$$

$$P(x=r) = {}^{12}C_r (p)^r (q)^{12-r} \quad (7)$$

$$P(x=r) = {}^{12}C_r \left(\frac{3}{4}\right)^r \left(\frac{1}{4}\right)^{12-r} \quad (8)$$

$$r = 0, 1, 2, 3, \dots$$

$P(\text{at most one success}) = P(x=0) + P(x=1)$

$$= {}^{12}C_0 \left(\frac{3}{4}\right)^0 \left(\frac{1}{4}\right)^{12} + {}^{12}C_1 \left(\frac{3}{4}\right)^1 \left(\frac{1}{4}\right)^{11} \quad (9)$$

$$= \left(\frac{1}{4}\right)^{12} + 36 \left(\frac{1}{4}\right)^{12} = \frac{37}{4^{12}} \quad (10)$$