

# Probability and Random Variables

## Assignment 4

Yash R Ramteke (bt21btech11006)

May 31, 2022

# Outline

1 Problem

2 Solution

# Problem

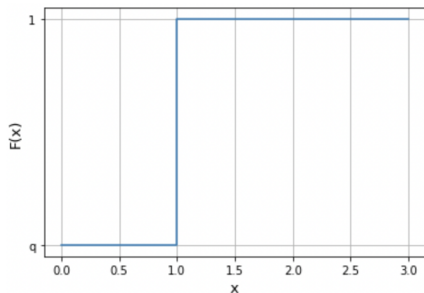
In the coin-tossing experiment, the probability of heads equals  $p$  and the probability of tails equals  $q$ . We define the random variable  $x$  such that  $x(h)=1$ ,  $x(t)=0$

We shall find it's distribution function  $F(x)$  for every  $x'$  from  $-\infty$  to  $\infty$ .

If  $x \geq 1$ , then  $x(h)=1$  and  $x(t)=0 \leq x$ .

Hence  $F(x)=P\{x \leq x'\} = P(h,t)=1$ ,  $x \geq 1$

# Solution



If  $0 \leq x \leq 1$ , then  $x(h)=1$  and  $x(t)=0 \leq x$ . Hence

$$F(x)=P\{x \leq x\} = P\{t\}=q, \quad 0 \leq x \leq 1.$$

If  $x < 0$ , then  $x(h)=1 > x$  and  $x(t)=0 > x$ . Hence,

$$F(x)=P\{x \leq x\}=P\{\emptyset\} = 0, \quad x < 0$$