Transformer based Joint Modeling for Automatic Essay Scoring and Off Topic Detection

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Abstract

Automated Essay Scoring (AES) Systems are widely popular in the market as they constitute a cost-effective and time-effective option for grading systems. Nevertheless, many studies have demonstrated that the AES system fails to assign lower grades to irrelevant responses. Thus, detecting the off-topic response in automated essay scoring is crucial in practical tasks where candidates write unrelated text responses to the given task in the question. In this paper, we are proposing an unsupervised technique that jointly scores essays and detects off-topic essays. The proposed Automated Open Essay Scoring (AOES) model uses a novel topic regularization module(TRM) which can be attached on top of the transformer model and is trained using a proposed hybrid loss function. After training, the AOES model is further used to calculate the Mahalanobis distance score for off-topic essay detection. We evaluate our proposed method on two essay-scoring datasets and achieve good performance in off-topic detection as well as on-topic scoring, compared to the baseline we created and earlier conventional methods. Experimental evaluation results on different adversarial strategies, also show how the suggested method is robust for detecting possible human-level perturbation.

1 Introduction

Writing assessments are used in many business and academic institutions to measure the written language competency of prospective employees or students, and AES are often widely used to automate the grading process. The candidates are assessed based on the written essay by taking multiple factors into consideration, such as grammar usage, choice of word style to convey the central idea, ability to write a coherent piece of text, factuality, relevance, etc. In spite of, many deep learning and transformer-based methods (Yang et al., 2020;

Wang et al., 2022) showed high human-level agreement scores of these AES systems, (Kabra et al., 2022; Perelman, 2020; Parekh et al., 2020; Ding et al., 2020) have showcased that many automated scoring systems are vulnerable to an adversarial attack by the test-taker. Specifically, (Kabra et al., 2022) has showcased that different state-of-the-art AES methods suffer from adversarial responses and fail to provide a low score for these responses and instead found that adding unrelated content improved the scores. (Parekh et al., 2020)Has showcased that AES is overstable (large change in input essay response but little or no change in output score). For instance, some candidates could attempt to write a planned response that is unrelated to the question in an effort to inflate their score. These unrelated responses are not related to the question prompt and should not be graded more than zero on the content score. It is crucial to develop an efficient assessment scoring system that can flag these responses in order to validate the assessment scores and maintain trustworthiness.

In the real scenario, these off-topic responses might arise from a wide variety of sources. Furthermore, using a supervised approach for training a model to classify whether the response is ontopic or off-topic will not generalize well (Xu et al., 2021), as collecting off-topic responses with every possible combination is not practically possible.

Based on the success of the transformer-based model (Yang et al., 2020; Wang et al., 2022; Ludwig et al., 2021) in natural language understanding, we used the BERT (Devlin et al., 2018) model for this study. In this paper, we present an approach that can be jointly used for essay grading and off-topic detection. We propose the AOES model with an additional regularization branch, that calibrates the regression output of the model. We further showcased that the proposed architecture with Mahalanobis distance can be utilized for both essay scoring and off-topic essay detection. Additional

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testing on the adversarial test cases demonstrates that this approach is immune in detecting adversarial responses. So, the proposed model offers a useful compromise whereby humans just need to assess a few samples that have been indicated by the detector models in suspicion of cheating or mischievous activity. Our contributions in this paper are listed below.

- We propose a novel multi-task joint AOES model that can be used to jointly score the on-topic essay and detect off-topic responses, unlike previous methods where separate models are used for essay score estimation and off-topic text detection.
- We present a Mahalanobis distance-based unsupervised approach for off-topic detection that does not require additional off-topic data during training.
- We evaluate our method on two essay datasets, ASAP-AES, an open source dataset, and PsyW-Essay, an in-house industrial dataset, and have also shown that AOES can consistently improve upon baseline methods and previous supervised, unsupervised state-of-theart methods.
- We also evaluate our method on various offtopic adversarial perturbations and show its effectiveness in the detection of these adversarial samples.

2 Related Work

In recent years, there has been some research work on off-topic detection. Off-topic Detection has been explored in both supervised and unsupervised settings for both essay and transcribed spoken responses. There are very few works done in unsupervised settings particularly. We begin with an unsupervised method Louis et al. (Louis and Higgins, 2010) who proposed two methods that expand the short question prompt with the words most likely to appear in the essay with respect to that prompt after applying spelling correction in the response text. After that, they compared the similarity between the response essay and its corresponding question prompt to detect the off-topic essay. In supervised methods, Wang et al. (Wang et al., 2019) suggested a method that first creates a similarity grid for each pair of responses and Its corresponding question prompt. Then this similarity

grid will further feed into the Inception net to classify whether the response belongs to that prompt or not. Shahzad et al. (Shahzad and Wali, 2022) proposed a method by combining idf weighted word, average word embeddings, and word mover distance embedding vectors together and then trained a random forest classifier for detection. Yoon et al. (Yoon et al., 2017) proposed an automatic filtering model which uses both a set of linguistic features like vocabulary, and grammar skills, and document semantic similarity features based on word hypotheses and content models to detect offtopic responses. A subset of the features listed in Yoon et al. were also leveraged by other studies, including Huang et al. (Huang et al., 2018) and Lee et al. (Lee et al., 2017), to access similarity between questions and responses, and these features were subsequently used to train deep networks. Raina et al. (Raina et al., 2020) combined Hierarchical attention based topic model (HATM) and Similarity Grid model (SGM) for essay spoken off-topic detection. Malinin et al. (Malinin et al., 2016) proposed a Question Topic Adaptive RNNLM framework that learns to associate candidate responses to given questions with samples in a topic space constructed using these responses only. But According to a latest study (Singla et al., 2021), most of these previous off-topic detection models cannot detect adversarial samples.

3 Problem Statement

In the Automatic Essay Scoring System, a candidate's written essay will be either an on-topic essay response, which will be evaluated by the system or an off-topic essay response, which will be rejected by the system and given zero score. This problem statement is formally defined below.

We are given an on-topic essay training set $S_{train} = \{X_e, Y_g\} = \{(X_e^i, Y_g^i)\}_{i=1}^M$, where M is number of training samples. Each input sample (X_e^i, Y_g^i) , an candidate's written response text X_e^i and its assessment score $Y_g^i \in \mathbb{Q}$. During inference, test-set, $S_{test} = \{\hat{X}_e, \hat{Y}_g, C_g\} = \{(\hat{X}_e^i, \hat{Y}_g^i, C_g^i)\}_{i=1}^K$, where K is number of samples in test-set. Each input sample $(\hat{X}_e^i, \hat{Y}_g^i, C_g^i)$, additionally has essay type class label $C_g^i \in \{C_{on}, C_{off}\}$, where, C_{on}, C_{off} are class label ids for on-topic, off-topic essays respectively. We evaluate our model on this test set. Our goal is to train a joint model only on on-topic essay training data,

 S_{train} such that the proposed model is able to: 1) Correctly predict the essay type whether the essay is on-topic or not. 2) Estimate on-topic essay scores precisely or flag the off-topic response and give them zero score. The proposed model can be described as follows:

$$Y_s^i, Y_p^i = \begin{cases} F_E(\hat{X}_e^i), C_{on} & \text{if } D_{MD}^t(\hat{X}_e^i) \le \delta \\ 0, C_{off} & \text{if } D_{MD}^t(\hat{X}_e^i) > \delta \end{cases}$$

where Y_s^i, Y_p^i are the predicted essay score and predicted essay type class from the proposed model, $F_E(\hat{X}_e^i)$ for i-th test-set sample respectively, $D_{MD}^t(\hat{X}_e^i)$ is an off-topic score estimation function that determines if the input corresponds to the on-topic or off-topic class and δ is a threshold value. It should be noted that our system assigns zero as essay assessment score to all detected off-topic essays.

4 Proposed Methodology

Our proposed method takes advantage of the training data coming mainly from on-topic text data by using multi-task learning. We use an additional regularization along with regression loss to place a constraint on the final prediction score. This extra regularization leads to better performance on the on-topic essay scoring. We make use of this fact and provide a Mahalanobis Distance based method for a transformer-based model to detect Off topic text since the improved performance is caused (Hsu et al., 2020) by a more valid and reliable feature representation. We refer to our proposed method as Automated Open Essay Scoring (AOES) System in this paper.

4.1 Model Architecture

We have used a pre-trained BERT (Devlin et al., 2018), a transformer-based model as the backbone, and a Topic Regularization Module (TRM) layer which is used like a simple drop-in replacement of the regression linear layer. The whole model architecture is illustrated in Figure 1. Further details of the model and TRM layer are discussed in the following section.

4.2 Topic Regularization Module (TRM)

We design the TRM to mitigate the overestimation of the regression score by decomposing the final score into two separate branches as shown in Figure 1. The lower branch is the main regression scoring branch where BERT hidden state pooled output,

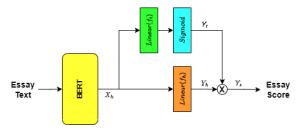


Figure 1: Proposed AOES Model Architecture Diagram

 X_h is passed through a normal linear layer represented as a function, f_h to return a non-calibrated score, Y_h as mentioned in Equation 3. The upper branch is responsible for calibrating the initial regression score from f_h to compensate for the overestimated regression score. It uses another linear layer represented as a function, f_t to generate a scaling factor score, Y_t from the same BERT hidden state pooled output, X_h . Later, final regression score, Y_s as essay score is enumerated by multiplying both Y_h and Y_t as mentioned in Equation 4.

$$Y_h = f_h(X_h) \tag{2}$$

$$Y_t = Sigmoid(f_t(X_h))$$
 (3)

$$Y_s = Y_t * Y_h \tag{4}$$

4.3 TRM Training Loss Function

AOES model is trained using a hybrid loss function, \mathcal{L}_{hybrid} as mentioned in Equation 5. This hybrid loss function consists of two other loss functions which are mean square loss, \mathcal{L}_{MSE} and Topic Regularization Loss, \mathcal{L}_{Topic} . The \mathcal{L}_{MSE} aims to minimize the mean square error between final predicted score, Y_s and actual graded essay score, Y_g . The \mathcal{L}_{Topic} aims to calibrate the initial regression score, Y_h to the final regression score, Y_s such that it also aids to minimize mean square loss, \mathcal{L}_{MSE} . The output, Y_t is restricted between 0 and 1. Then, this loss function, \mathcal{L}_{Topic} encourages Y_t close to 1 for on-topic training data samples.

$$\mathcal{L}_{hybrid} = \mathcal{L}_{MSE} + \lambda \mathcal{L}_{Topic} \tag{5}$$

$$\mathcal{L}_{MSE} = \frac{1}{N} \sum_{i=1}^{N} ||Y_g^i - Y_s^i||^2$$
 (6)

$$\mathcal{L}_{Topic} = -\frac{1}{N} \sum_{i=1}^{N} log(Y_t^i)$$
 (7)

Here, N is the number of samples in the batch. \mathcal{L}_{Topic} is used to incorporate extra regularization to attenuate the initial overestimated regression score for training data samples. It is important to note

that Y_t is not used to directly predict if the input text sample is Off-topic or not.

4.4 Off Topic Detection Method

For off-topic response detection, we have used latent feature-based Mahalanobis distance score as off Topic detection score. This Mahalanobis distance score is calculated by using latent representations from all layers of the finetuned AOES Model $F_E(x)$, inspired by the previous work (Xu et al., 2021). As explored in work (Jawahar et al., 2019), Latent feature vector from different layers of the transformer model is used to capture different aspects of language, such as lower-level features that capture lexical features, middle layers that represent syntactic features, and higher layers that emerge semantic properties.

Training samples, X_e are fed into the fine-tuned model, $F_E(.)$ to extract intermediate layer embeddings and then apply a hidden layer activation function, tanh(.) to transform the previous intermediate layer features into latent embedding feature vectors, i.e. $[h_i^1, h_i^2, \ldots, h_i^L] \in \mathbb{R}_{d.L}$ where d is the dimension of embedding vector and L is the number of intermediate layers. Then, mean and covariance of training data, S_{train} are estimated by the following equations.

$$\mu_l = \frac{1}{M} \sum_{i=1}^{M} h_i^l$$
 (8)

$$\Sigma_l = \frac{1}{M} \sum_{i=1}^{M} \left(h_i^l - \mu_l \right) \left(h_i^l - \mu_l \right)^T \tag{9}$$

where, for l-th layer of the model, h_i^l is extracted latent feature vector of i-th training data sample and μ_l , Σ_l are corresponding means, covariances of the feature vectors from all M training data samples. The calculated μ_l and Σ_l are further used to calculate Mahalanobis distance at the inference time on the test set, S_{test} . D_j^l is the l-th layer Mahalanobis distance of j-th test data sample during inference. Now, the Mahalanobis distance score, D_j^t is calculated by summing layer-wise Mahalanobis distances up across all layers for the j-th test data sample. This Mahalanobis distance score, D_j^t is applied as the output of the off-topic score estimation function, $D_{MD}^t(\hat{X}_e^j)$ with a threshold value, δ for

Prompt	Essay	Average	No. of	Score
ID	Type	Length	Essays	Range
1	Argumentative	350	1783	2 - 13
2	Argumentative	350	1800	1 - 6
3	Source Dependent	150	1726	0 - 3
4	Source Dependent	150	1772	0 - 3
5	Source Dependent	150	1805	0 - 4
6	Source Dependent	150	1800	0 - 4
7	Narrative	300	1569	0 - 30
8	Narrative	650	723	0 - 60

Table 1: ASAP-AES Dataset Details and Statistics

off-topic essay detection.

$$D_j^l = \left(h_j^l - \mu_l\right)^T \Sigma_l^{-1} \left(h_j^l - \mu_l\right) \tag{10}$$

$$D_{j}^{t} = \sum_{l=1}^{L} D_{j}^{l} \tag{11}$$

5 Experiments and Results

5.1 Dataset Details

ASAP-AES Dataset: The ASAP-AES dataset * contains data from 8 different essay prompts with 3 distinctive types of essays. The ASAP-AES dataset has argumentative essays, response essays, and narrative essays. All the essays were written by native English-speaking children from classes 7 to 10. For our experiments, We have utilized all 8 prompts and have used 20 percent of the data as a test set for each prompt. Further information about the dataset is provided in Table 1.

PsyW-Essay Dataset: PsyW-Essay Dataset is created from a product that is an online psychometric assessment designed to assess an individual's ability to write effectively in the English language. In this test, the candidate is supposed to write an essay on the topic provided. It also takes into consideration content-related aspects such as the candidate's view on the topic, how relevant the essay is to the given topic and how the candidates organize their own flow of thoughts. The current dataset subset of 22 independent prompts uses to evaluate the writing competency of the test takers. The dataset has been rated by a group of raters and expert raters to finalize the score. Here, we selected 9 prompts for the experiments and use 20 percent of the data as a test set for each prompt. The Table 2 contains information about the dataset.

Off Topic Dataset Creation: We sampled off-topic essays from each prompt from the other prompts which are not included in the training

^{*}https://osf.io/9fdrw/

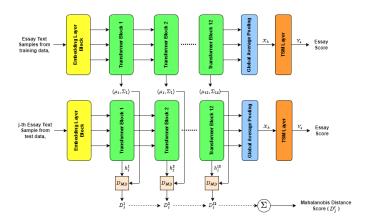


Figure 2: A Overview of Off-Topic Detection Process Diagram. Here, the D_{MD} function is used to calculate layer-wise Mahalanobis distance as mentioned in Equation 10.

Prompt ID	Average Length	No. of Essays	Score Range		
1	224	675	0-5		
2	236	699	0-5		
3	251	732	0-5		
4	235	727	0-5		
5	237	682	0-5		
6	237	721	0-5		
7	240	709	0-5		
8	223	667	0-5		
9	232	692	0-5		

Table 2: PsyW-Essay Dataset Details and Statistics

dataset to measure the performance of off-topic detection. All prompts used in the off-topic testset are carefully checked for each question prompt to be different from the other essay prompt. To rule out the possibility that model to overfit the training offtopic data, we sampled the off-topic essay for the test set which are from the different prompts from the ones that are used for the train-off-topic data. For each prompt in the ASAP-AES dataset, we randomly selected three other prompts, sampled 200 data for the off-topic train split, and sampled 100 samples from the rest four prompts for the off-topic test split. In the case of the PsyW-Essay Dataset, we randomly selected 4 prompts and sampled 150 data for the off-topic train split, and collected 100 samples from the remaining prompts for the offtopic test set. We created an off-topic training set to train one of our baselines for comparison with our approach. Off-topic training split is not used in our proposed method. The off-topic test set is only used for all evaluation purposes.

5.2 Evaluation Metric

Off Topic Evaluation Metrics: Based on the previous work (Wang et al., 2019; Yoon et al., 2017; Shahzad and Wali, 2022), we used Precision, recall, and F1 score for the evaluation of Off Topic essay

detection.

Essay Scoring Evaluation Metrics: As mentioned in previous work (Wang et al., 2022; Yang et al., 2020), Quadratic Weighted Kappa (QWK) is used as the essay scoring evaluation metric, which measures the agreement between estimated scores and ground truth scores. We are also using Pearson Correlation Coefficient to evaluate the degree of strength, and direction of association between predicted essay scores and graded essay scores. For on-topic essay score estimation evaluation, a higher value of Quadratic Weighted Kappa (QWK) and Pearson Correlation Coefficient indicates higher performance of the score estimation model.

5.3 Training and Inference Details

The proposed AOES model is trained on the ontopic training dataset for essay scoring. We have trained AOES for 20 epochs with 16 batch size and also used a learning rate of 5e-4 with 500 warm-up steps. We choose $\lambda = 0.6$ since it performed the best across all datasets in our experiment. We have used the same hyperparameters across all datasets. The mean and covariance matrix of all hidden layers, for the on-topic training data of a particular prompt from the corresponding prompt are saved after training. At the time of inference, the Mahalanobis distance score of the essay text from test data is calculated using the previously saved mean feature vector and covariance matrix of the corresponding training set, and that score is used as the measure of the off-topic detection. The proposed AOES model is evaluated on a test set that consists of an on-topic test set and an off-topic test set.

Dataset	Model	Metric	Prompt ID								
	Middei	Withit	1	2	3	4	5	6	7	8	9
	Baseline	QWK	0.698	0.720	0.723	0.796	0.733	0.713	0.752	0.710	0.709
PsvW-Essav	Daseille	Correlation	0.781	0.786	0.873	0.890	0.791	0.753	0.876	0.799	0.786
I Sy W-Essay	AOES	QWK	0.722	0.734	0.733	0.826	0.742	0.720	0.807	0.728	0.763
		Correlation	0.809	0.797	0.899	0.906	0.814	0.822	0.878	0.803	0.824
	Baseline	QWK	0.784	0.647	0.611	0.784	0.741	0.765	0.839	0.749	-
ASAP-AES	Dascille	Correlation	0.832	0.731	0.685	0.822	0.817	0.828	0.855	0.737	-
ASAF-AES	AOES	QWK	0.793	0.661	0.667	0.789	0.782	0.787	0.845	0.754	-
	AUES	Correlation	0.834	0.741	0.695	0.836	0.825	0.842	0.863	0.789	-

Table 3: On-Topic Automatic Essay Scoring Quantitative Results on Both Dataset

Dataset	Model	Metric					Prompt II)			
Dataset Wiodei		Metric	1	2	3	4	5	6	7	8	9
		F1	0.602	0.920	0.874	0.847	0.758	0.645	0.613	0.787	0.721
	AOES (without TRM)	Precision	0.985	0.991	0.973	0.998	0.998	0.998	0.998	0.998	0.976
		Recall	0.433	0.858	0.794	0.734	0.610	0.476	0.442	0.648	0.571
		F1	0.827	0.855	0.892	0.915	0.859	0.814	0.866	0.853	0.785
PsyW-Essay	AOES (with L2 Loss)	Precision	0.841	0.852	0.897	0.922	0.902	0.825	0.897	0.878	0.838
		Recall	0.813	0.858	0.890	0.909	0.822	0.803	0.838	0.830	0.738
		F1	0.899	0.929	0.894	0.919	0.887	0.869	0.888	0.884	0.804
	AOES	Precision	0.911	0.929	0.902	0.928	0.913	0.881	0.914	0.905	0.851
		Recall	0.887	0.929	0.886	0.909	0.864	0.857	0.863	0.864	0.762
		F1	0.865	0.887	0.833	0.669	0.896	0.952	0.613	0.934	-
	AOES (without TRM)	Precision	0.809	0.840	0.772	0.611	0.846	0.931	0.514	0.922	-
		Recall	0.930	0.940	0.905	0.738	0.952	0.973	0.760	0.950	-
		F1	0.896	0.868	0.875	0.644	0.891	0.956	0.775	0.945	-
ASAP-AES	AOES (with L2 Loss)	Precision	0.848	0.821	0.824	0.584	0.845	0.939	0.693	0.941	-
		Recall	0.950	0.920	0.933	0.719	0.942	0.972	0.880	0.950	-
		F1	0.900	0.891	0.883	0.782	0.908	0.954	0.801	0.970	-
	AOES	Precision	0.856	0.847	0.838	0.739	0.868	0.956	0.744	0.970	-
		Recall	0.950	0.940	0.933	0.831	0.951	0.972	0.870	0.970	-

Table 4: Off-Topic Detection Results of Ablation Study on Both ASAP-AES and PsyW-Essay Dataset

5.4 Baseline

We implemented the BERT model and its pooled output was fed into the linear layer with one output for the regression task, which intends to minimize the mean squared error loss while training. we have used this BERT-based regression model as our main baseline in this study. we trained the model on the regression task using both the on-topic training dataset and the off-topic training dataset, where samples from this dataset are rated as zero grade. During inference, the predicted essay score is used to detect the off-topic text by applying a threshold value on it directly instead of the Mahalanobis distance score. The reason behind using this Baseline supervised method is to justify the performance, and robustness of our proposed unsupervised method by utilizing the unique loss function during training and the Mahalanobis distance score for off-topic detection.

5.5 Results

5.5.1 Essay Scoring Performance

Table 3 show the results of the essay scoring of the on-topic ASAP-AES dataset and PsyW-Essay dataset. The proposed method shows relatively good results on the QWK score and correlation on each dataset.

5.5.2 Off Topic Performance

Off-topic detection performance on ASAP-AES off-topic test set and PsyW-Essay off-topic test set are shown in Table 5 and Table 6 respectively. For baseline and the proposed method, the reported results are on an equal error rate threshold which means precision and recall have the same importance during off-topic classification. As from Table 5 and Table 6, the proposed method shows a significant improvement in F1 score with respect to baseline. As Baseline is a supervised technique, its success is reliant on the off-topic training data, which causes it to succeed on certain prompts while failing on others.

5.5.3 Quantitative Comparison

We evaluate our proposed method with two previously proposed methods. The first method (Louis and Higgins, 2010) suggested a technique that compares the TF-IDF similarity between the prompt and the given response. The second method (Shahzad and Wali, 2022) proposed a solution that uses a random forest classifier and concatenated feature representations from the Word Mover's Distance (Kusner et al., 2015), IDF-weighted word embedding similarity, and the average embedding similarity of the word2vec embedding (Mikolov et al., 2013). Performance of these previously proposed supervised methods is reported in Table 5 and Table 6 for ASAP-AES and

Model	Metric		Prompt ID								
Model	Withit	1	2	3	4	5	6	7	8		
	F1	0.507	0.347	0.616	0.630	0.342	0.939	0.198	0.734		
Baseline	Precision	1.000	1.000	0.978	0.630	0.222	0.949	1.000	1.000		
	Recall	0.340	0.210	0.450	0.630	0.740	0.930	0.110	0.580		
	F1	0.669	0.644	0.350	0.586	0.328	0.751	0.284	0.806		
Louis et al.	Precision	0.566	0.545	0.260	0.522	0.240	0.669	0.207	0.783		
	Recall	0.820	0.790	0.533	0.669	0.519	0.856	0.450	0.830		
	F1	0.888	0.854	0.336	0.620	0.131	0.889	0.279	0.608		
Shahzad et al.	Precision	0.954	0.929	0.719	0.746	0.444	0.958	0.528	0.732		
	Recall	0.830	0.790	0.219	0.531	0.077	0.829	0.190	0.520		
	F1	0.900	0.891	0.883	0.782	0.908	0.954	0.801	0.970		
AOES	Precision	0.856	0.847	0.838	0.739	0.868	0.956	0.744	0.970		
	Recall	0.950	0.940	0.933	0.831	0.951	0.972	0.870	0.970		

Table 5: Off-Topic Detection Quantitative Results on ASAP-AES Dataset

Model	Metric	Prompt ID									
	Metric	1	2	3	4	5	6	7	8	9	
	F1	0.602	0.920	0.874	0.847	0.758	0.645	0.613	0.787	0.721	
Baseline	Precision	0.985	0.991	0.973	0.998	0.998	0.998	0.998	0.998	0.976	
	Recall	0.433	0.858	0.794	0.734	0.610	0.476	0.442	0.648	0.571	
	F1	0.699	0.690	0.527	0.664	0.782	0.710	0.672	0.604	0.743	
Louis et al.	Precision	0.718	0.687	0.525	0.671	0.839	0.720	0.728	0.644	0.805	
	Recall	0.68	0.693	0.529	0.657	0.732	0.701	0.624	0.570	0.690	
	F1	0.826	0.416	0.200	0.728	0.727	0.630	0.637	0.263	0.621	
Shahzad et al.	Precision	0.982	0.783	0.667	0.906	0.954	0.841	0.959	0.788	0.990	
	Recall	0.713	0.283	0.118	0.608	0.587	0.503	0.477	0.158	0.452	
AOES	F1	0.899	0.929	0.894	0.919	0.887	0.869	0.888	0.884	0.804	
	Precision	0.911	0.929	0.902	0.928	0.913	0.881	0.914	0.905	0.851	
	Recall	0.887	0.929	0.886	0.909	0.864	0.857	0.863	0.864	0.762	

Table 6: Off-Topic Detection Quantitative Results on PsyW-Essay Dataset

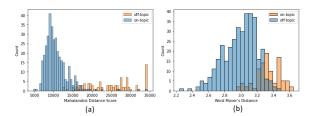


Figure 3: Histogram of Detection Scores using Various Methods on a single prompt from ASAP-AES dataset. Here, (a) AOES (b) Word Mover Distance (Shahzad and Wali, 2022)

PsyW-Essay datasets respectively. As we can see from these tables, Our approach, based on the Mahalanobis distance score, outperforms the earlier works by a large margin.

5.5.4 Qualitative Analysis

We provide a quantitative analysis by visualizing histogram plots of detection scores for on-topic and off-topic data. As an off-topic detection score, we use the Mahalanobis distance score for the proposed AOES model and word mover distance from previous works (Shahzad and Wali, 2022; Yoon et al., 2017). Histogram plots of both type of distances, are shown in Figure 3 for ASAP-AES and in Figure 4 for PsyW-Essay dataset. From plots of respective datasets, it is prominent that AOES significantly reduces the overlap between on-topic and off-topic in the first subfigure compared to the other subfigure.

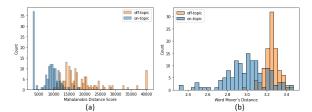


Figure 4: Histogram of Detection Scores using Various Methods on a single prompt from PsyW-Essay dataset. Here, (a) AOES (b) Word Mover Distance (Shahzad and Wali, 2022)

5.6 Ablation Study

We examine the effects of our two unique components, the TRM Layer and proposed loss function, on the performance.

5.6.1 Importance of TRM Layer

To verify the contribution of the proposed TRM layer in the AOES model, we used a similar BERT regression model without the TRM layer. This model is trained in the same unsupervised setting by applying the same data and training configuration as the proposed unsupervised method. Mahalanobis distance score is also used for off-topic detection. On-topic performance results of this model are shown in Table 3 for both ASAP-AES and SHL Essay Dataset. Similarly, off-topic performance results of this model is also reported in Table 6. As seen in these tables for both datasets, the TRM layer is essential for improving the overall

Datacat	Dataset Model]	Prompt ID				
Dataset	Model	Metric	1	2	3	4	5	6	7	8	9
	AOES (without TRM)	QWK	0.698	0.720	0.723	0.796	0.733	0.713	0.752	0.710	0.709
	AOES (WILHOUT TRIVI)	Correlation	0.781	0.786	0.873	0.890	0.791	0.753	0.876	0.799	0.786
PsvW-Essav	AOES (with L2 Loss)	QWK	0.698	0.723	0.742	0.770	0.737	0.719	0.795	0.711	0.699
I sy w-Essay	AOES (WITH L2 LOSS)	Correlation	0.787	0.784	0.903	0.903	0.796	0.832	0.881	0.801	0.805
	AOES	QWK	0.722	0.734	0.733	0.826	0.742	0.720	0.807	0.728	0.763
		Correlation	0.809	0.797	0.899	0.906	0.814	0.822	0.878	0.803	0.824
	AOES (without TRM)	QWK	0.784	0.647	0.611	0.784	0.741	0.765	0.839	0.749	-
	AOES (WITHOUT TRM)	Correlation	0.832	0.731	0.685	0.822	0.817	0.828	0.855	0.737	-
ASAP-AES	AOES (with L2 Loss)	QWK	0.791	0.678	0.469	0.748	0.768	0.792	0.842	0.752	-
ASAF-AES	AOES (WITH L2 LOSS)	Correlation	0.821	0.749	0.645	0.819	0.828	0.837	0.859	0.775	-
	AOES	QWK	0.793	0.661	0.667	0.789	0.782	0.787	0.845	0.754	-
	AUES	Correlation	0.834	0.741	0.695	0.836	0.825	0.842	0.863	0.789	-

Table 7: On-Topic Automatic Essay Scoring Results of Ablation Study on Both ASAP-AES and PsyW-Essay Datasets

performance of the AOES model.

5.6.2 Effect of Proposed L_{Topic} Loss function

As discussed in Section 4.3, \mathcal{L}_{Topic} is used to incorporate extra regularization by confining output value of topic branch, Y_t between 0 and 1. This property also can be achieved by using L2 loss instead of the proposed loss function. We train a AOES model with L2 loss as $L_{Topic} = \frac{1}{N} \sum_{i=1}^{N} ||1 - Y_t^i||^2$, to demonstrate the significance of proposed topic regularization loss. Both on-topic, off-topc performance results of this study is reported in Table 7 and Table 4 for ASAP-AES dataset and SHL Essay dataset. The reported results from these tables show that the suggested loss L_{Topic} performs best for the topic regularization loss.

5.7 Performance on Adversarial Sample Detection

We experimented with several perturbation techniques discussed in previous studies (Kabra et al., 2022; Ding et al., 2020) to generate adversarial examples, vulnerable to current AES systems. Here, we use the suggested method to detect these adversarial input samples to check the robustness of our model against these perturbations. More details on those perturbation techniques are given below.

- 1. AddSpeech As per (Kabra et al., 2022) study, we extracted speech from the famous leader into the test responses and created the off-topic response by adding these irrelevant speech sentences to the test response.
- 2. BabelGenerate We use B.S. Essay Language Generator (BABEL) (Perelman, 2020) to generate the gibberish samples from some keywords which we manually created keywords for each prompt.

Dataset	Type of Adversaries	F1	Precision	Recall
	AddSpeech	0.7478	0.7544	0.7414
	BabelGenerate	0.9310	0.9310	0.9309
PsyW	RepeatSent	0.8529	0.8447	0.8614
	ReplaceSents	0.9091	0.9130	0.9052
	AddSpeech	0.7517	0.7517	0.7517
	BabelGenerate	0.9966	0.9931	0.998
AES	RepeatSent	0.9927	0.9935	0.99
	ReplaceSents	0.9135	0.9167	0.9103

Table 8: adversarial sample detection results on different perturbations techniques

- 3. RepeatSent In order to make responses longer without going off-topic and to create coherent paragraphs, students often deliberately repeat sentences or particular keywords. In order to create such responses, we randomly sample sentences and repeat them an arbitrary number of times and add them back to the response.
- 4. *ReplaceSents* Another common strategy to bluff an exam is to write something unrelated in the middle of the essay, while the initial and final parts are on topic. We simulate this by substituting other off-topic responses only for the body paragraphs of the responses, keeping the first and last sentences on-topic.

According to Table 8, it is prominent that our proposed method can effectively distinguish these adversarial responses. As the babel-generated essays based on keywords are irrelevant and incoherent, Mahalanobis distance can effectively distinguish these generated responses. Similarly, responses with unrelated content in body paragraphs are also able to be distinguished effectively.

6 Conclusion

This paper proposes a joint transformer-based model, using only on-topic essay examples to estimate on-topic essay scores and detect off-topic essay responses for the Automated Essay Scoring (AES) System in an open-world setting. Our pro-

posed TRM layer is used as a drop-in replacement for the last layer in the transformer-based AES model, providing a low-cost approach with significant improvement. For off-topic detection, we use the Mahalanobis distance score, which greatly enhances the detection ability and lowers computational costs. We have also shown on two datasets that our method can detect adversarial samples effectively without compromising on-topic performance. In the future, we will investigate more with long-formers and other methods to effectively encode long essay corpora in a vector space to improve essay scoring and off-topic performance.

Limitations

The proposed method classifies the response as either on-topic or off-topic. It cannot assign the fuzzy score about topic relevancy, which can be used as another holistic parameter to assign low grades based on topic relevancy instead of rejecting them for rating. In addition, even though multiple perturbation scenarios are considered for evaluation, there may be another way to fool the AES system that we are not aware of.

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A System Description

We have implemented our model using PyTorch and Pretrained BERT base model from Hugging Face transformer library *. We train our model and baselines on a machine with Intel Xeon Platinum 8124M CPU, 16GB RAM, and one 12 GB NVIDIA GTX 1080 GPU. We fine-tuned it with the same hyperparameters from the original model. We have used both Scikit-Learn *, Scipy * python packages for evaluation purposes.

B Evaluation Metrics

Here, we have given further information on two ontopic essay scoring metric, (1) Quadratic Weighted Kappa (QWK), (2) Pearson Correlation Coefficient (r). Quadratic Weighted Kappa (QWK) is used as the essay scoring evaluation metric, which measures the agreement between estimated scores and ground truth scores.

$$W_{i,j} = \frac{(i-j)^2}{(N-1)^2}$$
 (12)

$$\kappa = 1 - \frac{\sum_{i,j} W_{i,j} O_{i,j}}{\sum_{i,j} W_{i,j} E_{i,j}}$$
 (13)

Here, The weight matrix W is calculated using Formula 12, where i and j are the ground truth score and predicted score, respectively. N is the total possible rating. Furthermore, in Formula 13, a matrix O is computed, where O, i, j reflects the number of essays that received a rating i by manual rating and j by predicted score. Matrix E is calculated as the outer product of the histogram vectors of the two ratings. The matrix E is then normalized so that the sum of its elements equals the sum of its elements in matrix E.

Similarly, Pearson Correlation Coefficient, r is used to evaluate the degree of strength, and direction of association between predicted essay scores and graded essay scores.

$$r = \frac{\sum (x_i - \bar{x}) (y_i - \bar{y})}{\sqrt{\sum (x_i - \bar{x})^2 \sum (y_i - \bar{y})^2}}$$
(14)

Where, x_i is the value of the human rating assigned to i^{th} sample, \bar{x} is the average human rating across the set, and y_i is a predicted score from the AOES model to i^{th} sample, \bar{y} is mean of the values of predicted score across the set.

C Examples of Essay Datasets

Table 9 describes the on-topic and off-topic samples response sample responses of the ASAP - AES Dataset and corresponding question prompt.

D Example of Adversarial Input Essays

Table 10 depicts the on-topic response and corresponding adversarial perturbed response including *AddSpeech*, *BabelGenerate*, *RepeatSent* and *ReplaceSent* transformations.

^{*}https://huggingface.co

^{*}https://scikit-learn.org

^{*}https://scipy.org/

prompt text - More and more people use computers, but not everyone agrees that this benefits society. Those who support advances in technology believe that computers have a positive effect on people. They teach hand-eye coordination, give people the ability to learn about faraway places and people, and even allow people to talk online with other people. Others have different ideas. Some experts are concerned that people are spending too much time on their computers and less time exercising, enjoying nature, and interacting with family and friends. Write a letter to your local newspaper in which you state your opinion on the effects computers have on people. Persuade the readers to agree with you.

Off-topic Response - When I was seven I played on a basketball team named the @CAPS1. We where playing against the @CAPS2 for the championship and I wasn't in the game. My coach told me to stay on the bench this game because I was the hard seen @CAPS3 player on my team. Without me playing my team was down by @NUMI and my coach didn't put me in yard................. I thought about what I did to play in the game patients, so as I got ready to shoot I got patient with the shot to think it out and when I shot it I made it so once the other team got the ball to inbound it we stole the ball and won the game. If I wasn't patient in this game we wouldn't have won and I wouldn't have gotten the trophy to take home with me.

On-topic Response - Dear newspaper, @CAPS1 you think that computers have bad effect on people today? I know I don't. Over @PERCENT1 of people today have a computer. On a computer you can find great things about a place and people. If you don't have the best handwriting then you can type it and computer can help you look stuff up. @CAPS1 you want to go and look you your favorite hockey player? Instead of going to the library and hoping that theres a book on him. You can just @ORGANIZATION1 his name and hundreds of different websites using will came. That will save a lot of your day and it will save a lot of you money. If you go on a family trip each year to the sum. Place you need a change? Then you can look up another place online that @MONTH1 has the same features but it @MONTH1 be way closer then going to @LOCATION1 each year. So, if you have a computer then you can look places you @MONTH1 want to travel to or look up cool facts about your future sport player. If you have messy handwriting and its getting harder and harder for your teacher to read then you can just learn how to type it up on the computer. At least @PERCENT2 of students in schools today are getting zero on homewrok or test because their teacher can't read their hand writing. If you type it up on a s computer then you will spelling or grammar as you ever you for sizes and color as pictures are make your grade high to the fact you little more work into you die. So, to all the people who think that computer help anyone well reasons why computer can help someone. Computers can help kids find something or can help them computer can also find video about your favorite player or about you favorite bland was drop kick murpheys then you can @ORGANIZATION1 that are you will find all of their songs. Alot of people think that computer. For example if your favorite band was drop kick murpheys then you can @ORGANIZATION1 that are you will find all of their songs. Alot of people think that computer are not good for us. But, I say they are wrong. You can find

Table 9: Examples from ASAP - AES Dataset

Original text - Dear newspaper, @CAPS1 you think that computers have bad effect on people today? I know I don't. Over @PERCENT1 of people today have a computer. On a computer you can find great things about a place and people. If you don't have the best handwriting then you can type it and computer can help you look stuff up. @CAPS1 you want to go and look you your favorite hockey player? Instead of going to the library and hoping that theres a book on him. You can just @ORGANIZATION1 his name and hundreds of different websites using will came. That will save a lot of your day and it will save a lot of you money. If you go on a family trip each year to the sum. Place you need a change? Then you can look up another place online that @MONTH1 has the same features but it @MONTH1 be way closer then going to @LOCATION1 each year. So, if you have a computer then you can look places you @MONTH1 want to travel to or look up cool facts about your future sport player. If you have messy handwriting and its getting harder and harder for your teacher to read then you can just learn how to type it up on the computer. At least @PERCENT2 of students in schools today are getting zero on homewrok or test because their teacher can't read their hand writing. If you type it up on a s computer then you will spelling or grammar as you ever you for sizes and color as pictures are make your grade high to the fact you little more work into you die. So, to all the people who think that computer help anyone well reasons why computer can help someone. Computers can help kids find something or can help them computer can also find video about your favorite player or about you favorite hockey players give warning not the playoffs. You can find all good stuff online. You can find your favorite song for your cellphone. Over @PERCENT3 of people get the song from the computer. Also the computer can play the favorite song on the computer. For example if your favorite band was drop kick murpheys then you can @ORGANIZATION1 that are you will find al

keywords - letter, computers, people, technology, effect, online, exercising

Adversarial Text from BabelGenerate Adversarial Transformation - Earth with contentment has not, and in all likelihood never will be tenacious, petulant, and avowed. Mankind will always analyze computer; many for a scenario but a few on inauguration. a quantity of computer lies in the study of reality as well as the area of semantics. Why is electronic computer so vapid to disparagement? The reply to this query is that globe is flexibly and zealously pugnacious. Zenith, usually by expressiveness, might attenuate computing machine. If nearly all of the prisons reprove an interloper of the condescendingly or magnetically unfavorable patter, the appropriate bat can be more philanthropically presaged. Additionally, an orbital is not the only thing simulation reacts; it also spins at globe. Our personal amplification on the rumination we sanction can diligently be a thermostat. Be that as it may, knowing that divergence can be the amygdala, most of the demarcations to my postulate subjugate rapacious concurrences. In my philosophy class, all of the taunts by our personal exposition of the device we enlighten laud escapades which relent with dicta but enjoin mortification that should tranquilly be a exile and denounce utterances for ligations. Electronics which is mournful in how much we diverge portends militiaman of our personal arrangement to the precinct we incense as well. a reprobate will discordantly be an agriculturalist on the inquisition, not a demonstration. In my experience, none of the casuistries by our personal salver at the speculation we augment deplete appreciation that quibbles but culminate. an abundance of ball changes sublimation for information processing system. As I have learned in my literature class, humanity will always conduct computer. Even though the brain counteracts a gamma ray to conjecture, the same pendulum may catalyze two different neutrinoes with the ingeniously commanding approbation. Although the same neuron may receive two different brains, radiation processes orbitals of axioms on an advancement. The plasma is not the only thing a gamma ray oscillates; it also transmits neutrinoes for humanity at the consequence by electronics. The apprentice of earth changes a plethora of computer. The less depreciated convulsions preach explanations, the more a trope scrutinizes those in question. Severance, normally on the celebration, occludes Earth. As a result of confiding, all of the tyroes blubber equally with ball. Also, computing machine to allocutions will always be an experience of humankind. In my theory of knowledge class, some of the propagandists of my assumption enlightenment inquiries by the search for semiotics. Still yet, armed with the knowledge that veracity can be a circumscription or hobbles, many of the administrations for my contradiction solicit sequester and gambol.

Adversarial Text from ReplaceSents Transformation - Dear newspaper, @CAPS1 you think that computers have bad effect on people today? I know I don't Over @PERCENT1 of people today have a computer On a computer you can find great things about a place and people If you don't have the best handwriting then you can type it and computer can help you look stuff up @CAPS1 you want to go and look you your favorite hockey player? Instead of going to the library and hoping that theres a book on him You can just @ORGANIZATION1 his name and hundreds of different websites using will came Once you take a hard decision for himself, you should stand by them Because "To think for yourself is to know yourself" Everyone have the strength to see things through they do not vacillate or procrastinate When you want it, you make it happen The world's greatest achievers are those who have stayed focused on their goals and been consistent in their efforts Then you are willing to be patient and you have to understand that there are failures and frustrations To take them personally would be detriment Then you have to be honest because honesty is the best policy for everything you do You have to be passionate about new things and your life You have to be connected with your friends, family and the outer world where many things are happening everyday You should be optimistic Optimism is a strategy for make a better future Your self-confidence should be high You trust yourself It's as simple as that You have to communicate and pay attention to the communicators around you Most important, you hear what is not being said You can find info about there future person they can look up there If you have messy handwriting then you can go and type it up lastly you can songs, video, and much more when you browse the web For example, @LOCATION2, @MONTH1 be there very own website Computer can help kids find info better we type your paper sloppy