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LAB REPORT on

Analysis and Design of Algorithms

Submitted by

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in partial fulfillment for the award of the degree of BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING



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CERTIFICATE

This is to certify that the Lab work entitled "Analysis and Design of Algorithms" carried out by YASHASVINI M R (1BM21CS252), who is bonafide student of B.M.S. College of Engineering. It is in partial fulfillment for the award of Bachelor of Engineering in Computer Science and Engineering of the Visvesvaraya Technological University, Belgaum during the academic semester May-2023 to July-2023. The Lab report has been approved as it satisfies the academic requirements in respect of a Analysis and Design of Algorithms (22CS4PCADA) work prescribed for the said degree.

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Course Outcome

CO1	Analyze time complexity of Recursive and Non-recursive algorithms using asymptotic notations.	
CO2	Apply various design techniques for the given problem.	
CO3	Apply the knowledge of complexity classes P, NP, and NP-Complete and prove certain problems are NP-Complete	
CO4	Design efficient algorithms and conduct practical experiments to solve problems.	

1. Write program to do the following:

a. Print all the nodes reachable from a given starting node in a digraph using BFS method.

```
#include<stdio.h>
void bfs(int);
int a[10][10],vis[10],n;
void main()
 int i,j,src;
 printf("Enter the number of vertices\n");
 scanf("%d",&n);
 printf("Enter the adjacency matrix\n");
  for(i=1;i<=n;i++)
   for(j=1;j \le n;j++)
     scanf("%d",&a[i][j]);
   vis[i]=0;
 printf("Enter the source vertex\n");
 scanf("%d",&src);
 printf("Nodes reachable from source vertex\n");
 bfs(src);
}
void bfs(int v)
  int q[10],f=1,r=1,u,i;
  q[r]=v;
  vis[v]=1;
  while(f<=r)
    u=q[f];
```

```
printf("%d",u);
for(i=1;i<=n;i++)
{
    if(a[u][i]==1 && vis[i]==0)
    {
       vis[i]=1;
       r=r+1;
       q[r]=i;
    }
}
GUTPUT

Enter the number of vertices
Enter the adjacency matrix
0 1 1 0 0 0 0 0
1 0 0 1 1 0 0 0
1 0 0 0 1 1 0</pre>
```

b. Check whether a given graph is connected or not using DFS method.

```
scanf("%d",&a[i][j]);
     for(i=1;i \le n;i++)
     vis[i]=0;
     printf("DFS traversal\n");
     for(i=1;i \le n;i++)
           if(vis[i]==0)
           dfs(i);
     return 0;
int dfs(int v)
     int i; vis[v]=1;
     printf("%d",v);
     for(i=1;i<=n;i++)
           if(a[v][i]==1&& vis[i]==0)
           dfs(i);
     return 0;
OUTPUT
 Enter number of vertices
Enter adjacency matrix
 1100000
  0011000
  0000110
  1000001
  1000001
  0100001
  0100001
```

2. Write a program to obtain the Topological ordering of vertices in a given digraph.

```
#include<stdio.h>
#include<conio.h>
void dfs(int);
int a[10][10],vis[10],exp[10],n,j,m;
void main()
 int i,x,y;
 printf("Enter the number of vertices\n");
 scanf("%d",&n);
 for(i=1;i \le n;i++)
  {
   for(j=1;j \le n;j++)
        a[i][j]=0;
   vis[i]=0;
  printf("Enter the number of edges\n");
  scanf("%d",&m);
  for(i=1;i \le m;i++)
    printf("Enter a directed edge\n");
    scanf("%d %d",&x,&y);
    a[x][y]=1;
  }
  j=0;
  for(i=1;i \le n;i++)
  {
    if(vis[i]==0)
        dfs(i);
  printf("Topological sort\n");
  for(i=n-1;i>=0;i--)
    printf("%d",exp[i]);
```

```
getch();
void dfs(int v)
 int i;
 vis[v]=1;
 for(i=1;i<=n;i++)
  if(a[v][i]==1 && vis[i]==0)
   dfs(i);
 \exp[j++]=v;
OUTPUT
Enter the number of vertices
Enter the number of edges
Enter a directed edge
Enter a directed edge
1 3
Enter a directed edge
Enter a directed edge
Enter a directed edge
4 5
```

Topological sort

13245

3. Implement Johnson Trotter algorithm to generate permutations.

```
#include <stdio.h>
#include <stdbool.h>
#define RIGHT TO LEFT false
#define LEFT TO RIGHT true
int searchArr(int a[], int n, int mobile)
{
  for (int i = 0; i < n; i++)
    if (a[i] == mobile)
       return i + 1;
  return -1;
}
int getMobile(int a[], bool dir[], int n)
{
  int mobile prev = 0, mobile = 0;
  for (int i = 0; i < n; i++)
  {
    if (dir[a[i] - 1] == RIGHT_TO_LEFT && i != 0)
       if (a[i] > a[i - 1] & & a[i] > mobile prev)
       {
         mobile = a[i];
```

```
mobile_prev = mobile;
    if (dir[a[i] - 1] == LEFT\_TO\_RIGHT && i != n - 1)
       if (a[i] > a[i+1] && a[i] > mobile\_prev)
       {
         mobile = a[i];
         mobile_prev = mobile;
       }
  if (mobile == 0 && mobile_prev == 0)
    return 0;
  else
  return mobile;
void swap(int *x, int *y)
  int temp = *x;
  x = y;
  *y = temp;
```

}

```
}
void printOnePerm(int a[], bool dir[], int n)
{
  int mobile = getMobile(a, dir, n);
  int pos = searchArr(a, n, mobile);
  if (dir[a[pos - 1] - 1] == RIGHT TO LEFT)
    swap(&a[pos - 1], &a[pos - 2]);
  else if (dir[a[pos - 1] - 1] == LEFT_TO_RIGHT)
    swap(&a[pos], &a[pos - 1]);
  for (int i = 0; i < n; i++)
    if (a[i] > mobile)
     {
       if (dir[a[i] - 1] == LEFT_TO_RIGHT)
         dir[a[i] - 1] = RIGHT TO LEFT;
       else if (dir[a[i] - 1] == RIGHT TO LEFT)
         dir[a[i] - 1] = LEFT_TO_RIGHT;
     }
  }
  for (int i = 0; i < n; i++)
    printf("%d", a[i]);
```

```
printf(" ");
}
int fact(int n)
  int res = 1;
  for (int i = 1; i \le n; i++)
     res = res * i;
  return res;
}
void printPermutation(int n)
  int a[n];
  bool dir[n];
  for (int i = 0; i < n; i++)
     a[i] = i + 1;
     printf("%d", a[i]);
  }
  printf(" ");
  for (int i = 0; i < n; i++)
     dir[i] = RIGHT_TO_LEFT;
```

```
for (int i = 1; i < fact(n); i++)
    printOnePerm(a, dir, n);
}
int main()
{
    int n;
    printf("Enter the value of n: ");
    scanf("%d", &n);
    printPermutation(n);
    return 0;
}</pre>
```

OUTPUT

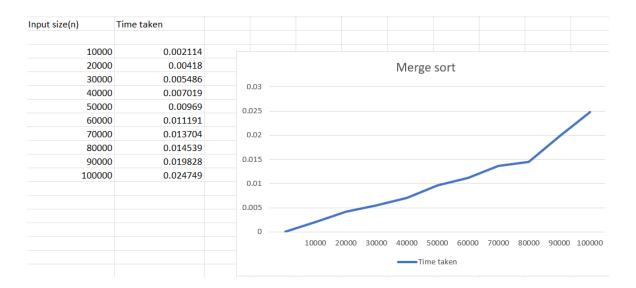
 4. Sort a given set of N integer elements using Merge Sort technique and compute its time taken. Run the program for different values of N and record the time taken to sort.

```
#include<stdio.h>
void mergesort(int a[],int i,int j);
void merge(int a[],int i1,int j1,int i2,int j2);
int main()
  int a[30],n,i;
  printf("Enter no of elements:");
  scanf("%d",&n);
  printf("Enter array elements:");
  for(i=0;i< n;i++)
  scanf("%d",&a[i]);
  mergesort(a,0,n-1);
  printf("\nSorted array is :");
  for(i=0;i< n;i++)
  printf("%d ",a[i]);
  return 0;
}
void mergesort(int a[],int i,int j)
  int mid;
  if(i \le j)
  {
     mid=(i+j)/2;
     mergesort(a,i,mid);
     mergesort(a,mid+1,j);
     merge(a,i,mid,mid+1,j);
  }
}
void merge(int a[],int i1,int i1,int i2,int i2)
  int temp[50];
  int i,j,k;
  i=i1;
```

```
j=i2;
  k=0;
  while(i \le j1 \&\& j \le j2)
   if(a[i] \le a[j])
   temp[k++]=a[i++];
    else
    temp[k++]=a[j++];
  while(i \le j1)
  temp[k++]=a[i++];
  while(j \le j2)
  temp[k++]=a[j++];
  for(i=i1,j=0;i<=j2;i++,j++)
  a[i]=temp[j];
}
OUTPUT
Enter no of elements:7
Enter array elements:23 45 21 23 98 67 56
Sorted array is :21 23 23 45 56 67 98
Process returned 0 (0x0) execution time : 11.775 s
Press any key to continue.
```

```
Enter no of elements:15
Enter array elements:23 87 34 56 12 34 65 78 54 67 15 23 63 20
29
Sorted array is :12 15 20 23 23 29 34 34 54 56 63 65 67 78 87
Process returned 0 (0x0) execution time : 43.156 s
```

GRAPH

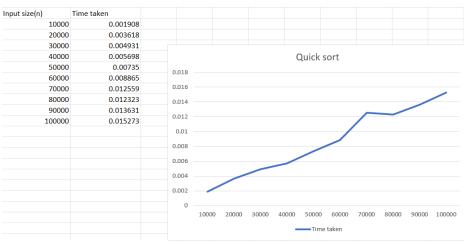


5. Sort a given set of N integer elements using Quick Sort technique and compute its time taken.

```
#include<stdio.h>
void qsort(int a[], int low, int high)
  int mid;
  if(low<high)
     mid=partition(a,low,high);
     qsort(a,low,mid-1);
     qsort(a,mid+1, high);
  }
}
int partition(int a[],int low, int high)
  int i,j,temp, pivot;
  pivot=a[low];
  i=low+1;
  j=high;
  while(i<=j)
     while(a[i]<=pivot)
       i++;
     while(a[j]>pivot)
       j--;
     if(i<j)
       temp=a[i];
       a[i]=a[j];
       a[j]=temp;
     }
  temp=a[low];
  a[low]=a[j];
  a[j]=temp;
  return j;
```

```
int main()
 int a[30], n, i;
 printf("Enter no of elements:");
 scanf("%d",&n);
 printf("Enter array elements:");
 for(i=0;i< n;i++)
 scanf("%d",&a[i]);
 qsort(a,0,n-1);
 printf("\nSorted array is :");
 for(i=0;i< n;i++)
 printf("%d ",a[i]);
 return 0;
OUTPUT
Enter no of elements:5
Enter array elements:1 8 3 2 10
Sorted array is :1 2 3 8 10
Process returned 0 (0x0) execution time : 13.919 s
Enter no of elements:10
Enter array elements:12 54 17 23 97 90 17 27 45 22
Sorted array is :12 17 17 22 23 27 45 54 90 97
Process returned 0 (0x0) execution time : 18.328 s
```

GRAPH

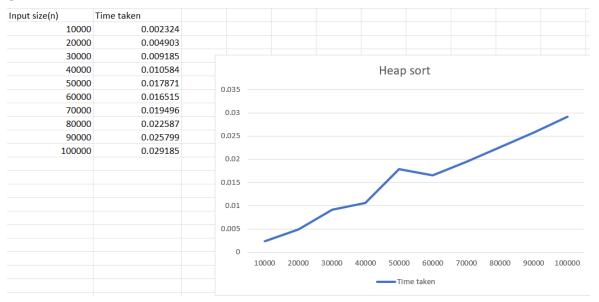


6.Sort a given set of N integer elements using Heap Sort technique and compute its time taken.

```
#include <stdio.h>
void swap(int* a, int* b)
  int temp = *a;
  a = b;
  *b = temp;
}
void heapify(int arr[], int N, int i)
  int largest = i;
  int left = 2 * i + 1;
  int right = 2 * i + 2;
  if (left < N && arr[left] > arr[largest])
     largest = left;
  if (right < N && arr[right] > arr[largest])
     largest = right;
  if (largest != i) {
     swap(&arr[i], &arr[largest]);
     heapify(arr, N, largest);
  }
}
void heapSort(int arr[], int N)
  for (int i = N / 2 - 1; i \ge 0; i--)
     heapify(arr, N, i);
  for (int i = N - 1; i \ge 0; i - 1) {
     swap(&arr[0], &arr[i]);
     heapify(arr, i, 0);
}
```

```
void printArray(int arr[], int N)
{
  for (int i = 0; i < N; i++)
    printf("%d ", arr[i]);
 printf("\n");
}
int main()
 int i, N;
  printf("Enter the number of elements in the array:\n");
  scanf("%d", &N);
  int arr[N];
  printf("Enter the elements of the array:\n");
  for(i = 0; i < N; i++)
    scanf("%d", &arr[i]);
  heapSort(arr, N);
  printf("Sorted array is\n");
  printArray(arr, N);
OUTPUT
Enter the number of elements in the array:
 5
Enter the elements of the array:
23 54 12 8965 56
Sorted array is
12 23 54 56 8965
```

GRAPH



7.Implement 0/1 Knapsack problem using dynamic programming.

```
#include<stdio.h>
#include<conio.h>
int n,m,w[10],p[10],v[10][10],x[10];
void knapsack()
  int i,j;
  for(i=0;i<=n;i++)
     for(j=0;j<=m;j++)
     {
       if(i==0||j==0)
          v[i][j]=0;
       if(w[i]>j)
          v[i][j]=v[i-1][j];
       else
          v[i][j]=(v[i-1][j]>v[i-1][j-w[i]]+p[i])?v[i-1][j]:v[i-1][j-w[i]]+p[i];
  object selected();
void object selected()
  int i,j;
  printf("Optimal solution:%d\n",v[n][m]);
  for(i=1;i \le n;i++)
     x[i]=0;
     i=n;
     j=m;
  while(i!=0 && j!=0)
     if(v[i][j]!=v[i-1][j])
       x[i]=1;
       j=j-w[i];
     i--;
  for(i=1;i \le n;i++)
```

```
if(x[i]==1)
      printf("Object %d is selected\n",i);
}
void main()
  int i;
  printf("Enter number of objects:");
  scanf("%d",&n);
  printf("\nMaximum capacity:");
  scanf("%d",&m);
  printf("\nEnter weights of the objects:");
  for(i=1;i \le n;i++)
    scanf("%d",&w[i]);
  printf("\nEnter profits of the objects:");
  for(i=1;i \le n;i++)
    scanf("%d",&p[i]);
  knapsack();
OUTPUT
Enter number of objects:4
Maximum capacity:5
Enter weights of the objects:2 1 3 2
 Enter profits of the objects:12 10 20 15
 Optimal solution:37
 Object 1 is selected
 Object 2 is selected
 Object 4 is selected
```

8. Implement All Pair Shortest paths problem using Floyd's algorithm.

```
#include<stdio.h>
#include<conio.h>
int c[10][10],d[10][10],n;
void floyd()
  int i,j,k;
  for(i=1;i \le n;i++)
     for(j=1;j \le n;j++)
       d[i][j]=c[i][j];
  for(k=1;k \le n;k++)
     for(i=1;i \le n;i++)
        for(j=1;j \le n;j++)
          d[i][j] = (d[i][j] < d[i][k] + d[k][j])?d[i][j] : (d[i][k] + d[k][j]);
void main()
  int i,j;
  printf("Enter the number of vertices:");
  scanf("%d",&n);
  printf("Enter the weight adjacency matrix(999 if infinity):\n");
  for(i=1;i<=n;i++)
   {
     for(j=1;j \le n;j++)
        scanf("%d",&c[i][j]);
```

```
floyd();
  printf("\nThe transitive closure is:\n");
  for(i=1;i \le n;i++)
     for(j=1;j \le n;j++)
        printf("%d\t",d[i][j]);
     printf("\n");
  printf("\n The shortest paths are:\n");
        for (i=1;i \le n;i++)
         for (j=1;j \le n;j++) {
               if(i!=j&&d[i][j]!=999)
                  printf("\n <%d,%d>=%d",i,j,d[i][j]);
OUTPUT
Enter the number of vertices:4
Enter the weight adjacency matrix(999 if infinity):
0 999 3 999
2 0 999 999
999 7 0 1
6 999 999 0
The transitive closure is:
         10
                            4
         0
                            6
                   0
                            0
         16
                   9
 The shortest paths are:
 <1,2>=10
 <1,3>=3
 <1,4>=4
 (2,1)=2
 \langle 2, 3 \rangle = 5
 (2,4)=6
 <3,1>=7
 \langle 3,2 \rangle = 7
 (4,1)=6
 <4,2>=16
 <4,3>=9
```

9. Find Minimum Cost Spanning Tree of a given undirected graph using Prim's and Kruskal's algorithm.

```
PRIM'S
#include<stdio.h>
int main()
{
  int cost[10][10], visited[10]=\{0\}, i,j,n,no e=1,min,a,b,min cost=0;
  printf("Enter the number of nodes:\n");
  scanf("%d",&n);
  printf("Enter the cost in form of adjacency matrix:\n");
  for(i=1;i \le n;i++)
     for(j=1;j \le n;j++)
       scanf("%d",&cost[i][j]);
       if(cost[i][j]==0)
         cost[i][j]=1000;
     }
  }
  visited[1]=1;
  while(no e<n)
  {
     min=1000;
     for(i=1;i \le n;i++)
        for(j=1;j \le n;j++)
          if(cost[i][j]<min)</pre>
            if(visited[i]!=0)
               min=cost[i][j];
               a=i;
               b=j;
```

```
if(visited[b]==0)
       printf("\n%d to %d cost=%d",a,b,min);
       min_cost=min_cost+min;
       no e++;
    visited[b]=1;
    cost[a][b]=cost[b][a]=1000;
  printf("\nminimum weight is %d",min_cost);
  return 0;
}
OUTPUT
Enter the number of nodes:
Enter the cost in form of adjacency matrix:
1 0 999 999 999
 5 999 0 3 999
2 999 3 0 1
999 999 999 1 0
 1 to 2 cost=1
  to 3 cost=3
 minimum weight is 7
```

KRUSKAL'S

```
#include<stdio.h>
int parent[10]={0};
int find_parent(int);
int is_cyclic(int,int);
int main()
{
   int cost[10][10],min_cost=0,min,i,j,n,no_e=1,a,b,u,v,x;
   printf("Enter number of vertices:\n");
```

```
scanf("%d",&n);
printf("Enter the weight in the form of an adjacency matrix:\n");
for(i=1;i \le n;i++)
  for(j=1;j \le n;j++)
     scanf("%d",&cost[i][j]);
     if(cost[i][j]==0)
      cost[i][j]=999;
  }
}
while(no_e<n)
  min=999;
  for(i=1;i \le n;i++)
     for(j=1;j<=n;j++)
       if(cost[i][j]<min)</pre>
         min=cost[i][j];
         a=u=i;
          b=v=j;
  u=find_parent(u);
  v=find_parent(v);
  x=is_cyclic(u,v);
  if(x==1)
     printf("\n%d to %d cost=%d",a,b,min);
    no e++;
     min cost+=min;
```

```
cost[a][b]=cost[b][a]=999;
  printf("\nMinimum cost of the spanning tree is %d",min cost);
  return 0;
int find_parent(int a)
  while(parent[a]!=0)
   a=parent[a];
  return a;
int is_cyclic(int a ,int b)
  if(a!=b)
  {
    parent[b]=a;
    return 1;
  return 0;
OUTPUT
```

```
Enter number of vertices:

5
Enter the weight in the form of an adjacency matrix:

0 1 5 2 999
1 0 999 999 999
5 999 0 3 999
2 999 3 0 1
999 999 99 1 0

1 to 2 cost=1
4 to 5 cost=1
1 to 4 cost=2
3 to 4 cost=3
Minimum cost of the spanning tree is 7
```

10. From a given vertex in a weighted connected graph, find shortest paths to other vertices using Dijkstra's algorithm.

```
#include<stdio.h>
#include<conio.h>
#define INFINITY 9999
#define MAX 10
void dijkstra(int G[MAX][MAX],int n,int startnode);
int main()
  int G[MAX][MAX],i,j,n,u;
  printf("Enter no. of vertices:");
  scanf("%d",&n);
  printf("\nEnter the adjacency matrix:\n");
  for(i=0;i< n;i++)
  for(j=0;j< n;j++)
  scanf("%d",&G[i][j]);
  printf("\nEnter the starting node:");
  scanf("%d",&u);
  dijkstra(G,n,u);
  return 0;
}
void dijkstra(int G[MAX][MAX],int n,int startnode)
  int cost[MAX][MAX],distance[MAX],pred[MAX];
  int visited[MAX],count,mindistance,nextnode,i,j;
  for(i=0;i< n;i++)
  for(j=0;j< n;j++)
  if(G[i][j] == 0)
  cost[i][j]=INFINITY;
  else
  cost[i][j]=G[i][j];
  for(i=0;i< n;i++)
    distance[i]=cost[startnode][i];
    pred[i]=startnode;
    visited[i]=0;
```

```
distance[startnode]=0;
  visited[startnode]=1;
  count=1;
  while(count<n-1)
    mindistance=INFINITY;
     for(i=0;i<n;i++)
    if(distance[i]<mindistance&&!visited[i])
       mindistance=distance[i];
       nextnode=i;
    visited[nextnode]=1;
    for(i=0;i<n;i++)
       if(!visited[i])
       if(mindistance+cost[nextnode][i]<distance[i])
         distance[i]=mindistance+cost[nextnode][i];
         pred[i]=nextnode;
       count++;
    for(i=0;i<n;i++)
    if(i!=startnode)
       printf("\nDistance of node%d=%d",i,distance[i]);
       printf("\nPath=%d",i);
       j=i;
       do
         j=pred[j];
         printf("<-%d",j);
    while(j!=startnode);
OUTPUT
```

```
Enter no. of vertices:5
Enter the adjacency matrix:
0 3 999 7 999
3 0 4 2 999
999 4 0 5 6
7 2 5 0 4
999 999 6 4 0
Enter the starting node:0
Distance of node1=3
Path=1 ← 0
Distance of node2=7
Path=2 ← 1 ← 0
Distance of node3=5
Path=3 ← 1 ← 0
Distance of node4=9
Path=4 ← 3 ← 1 ← 0
```

11.Implement "N-Queens Problem" using Backtracking.

```
#include <stdio.h>
#include <math.h>
int board[20], count;
int main()
 int n, i, j;
 void queen(int row, int n);
 printf(" - N Queens Problem Using Backtracking -");
 printf("\n\nEnter number of Queens:");
 scanf("%d", &n);
 queen(1, n);
 return 0;
// function for printing the solution
void print(int n)
 int i, j;
 printf("\n\nSolution %d:\n\n", ++count);
 for (i = 1; i \le n; ++i)
  printf("\t%d", i);
 for (i = 1; i \le n; ++i)
  printf("\n^{d}", i);
  for (j = 1; j \le n; ++j) // for nxn board
   if (board[i] == j)
     printf("\tQ"); // queen at i,j position
    else
     printf("\t-"); // empty slot
```

```
/*funtion to check conflicts
If no conflict for desired postion returns 1 otherwise returns 0*/
int place(int row, int column)
 int i;
 for (i = 1; i \le row - 1; ++i)
  // checking column and digonal conflicts
  if (board[i] == column)
   return 0;
  else if (abs(board[i] - column) == abs(i - row))
   return 0;
 }
 return 1; // no conflicts
// function to check for proper positioning of queen
void queen(int row, int n)
 int column;
 for (column = 1; column <= n; ++column)
  if (place(row, column))
   board[row] = column; // no conflicts so place queen
   if (row == n)
                     // dead end
                   // printing the board configuration
     print(n);
                  // try queen with next position
   else
     queen(row + 1, n);
OUTPUT
```

```
- N Queens Problem Using Backtracking -

Enter number of Queens:4

Solution 1:

1 2 3 4

1 - Q - - Q

3 Q - - - Q

4 - Q - - - Q

Solution 2:

1 2 3 4

1 - Q - Q - - - - Q

2 Q - - - Q - - - Q

3 A Q - - - Q - - - Q

4 A - Q - - - Q - - - - Q

4 A - Q - - - Q - - - - Q

4 A - Q - - - Q - - - - Q

4 A - Q - - - - Q - - - - Q

4 A - Q - - - - Q - - - - - Q
```