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import math
from scipy.stats import norm

def z_test_critical(mean_h0, sample_avg, pop_std, size_n, sig_level=0.05, test_type=1):
    # Compute standard error
    std_error = pop_std / math.sqrt(size_n)

    # TWO-TAILED TEST
    if test_type == 1:
        z_crit = norm.ppf(1 - sig_level / 2)
        lower_cv = mean_h0 - z_crit * std_error
        upper_cv = mean_h0 + z_crit * std_error

        verdict = (
            "Fail to Reject H0"
            if lower_cv <= sample_avg <= upper_cv
            else "Reject H0"
        )

        return {
            "Test Type": "Two-tailed",
            "Critical z": z_crit,
            "Lower CV": lower_cv,
            "Upper CV": upper_cv,
            "Sample Mean": sample_avg,
            "\nDecision": verdict
        }

    # RIGHT-TAILED TEST
    elif test_type == 2:
        z_crit = norm.ppf(1 - sig_level)
        upper_cv = mean_h0 + z_crit * std_error

        verdict = (
            "Fail to Reject H0"
            if sample_avg <= upper_cv
            else "Reject H0"
        )

        return {
            "Test Type": "Right-tailed",
            "Critical z": z_crit,
            "Upper CV": upper_cv,
            "Sample Mean": sample_avg,
            "\nDecision": verdict
        }

    # LEFT-TAILED TEST
    elif test_type == 3:
        z_crit = norm.ppf(1 - sig_level)
        lower_cv = mean_h0 - z_crit * std_error

        verdict = (
            "Fail to Reject H0"
            if sample_avg >= lower_cv
            else "Reject H0"
        )

        return {
            "Test Type": "Left-tailed",
            "Critical z": z_crit,
            "Lower CV": lower_cv,
            "Sample Mean": sample_avg,
            "\nDecision": verdict
        }

    else:
        raise ValueError("test_type must be 1 (two), 2 (right), or 3 (left)")

if __name__ == "__main__":
    print("Z-Test Hypothesis Testing Using Critical Value Method\n")

    pop_std = float(input("Enter population standard deviation: "))
    mean_h0 = float(input("Enter null hypothesis mean ( $\mu_0$ ): "))

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sample_avg = float(input("Enter observed sample mean: "))
size_n = int(input("Enter number of observations: "))
sig_level = float(input("Enter significance level: "))

print("\nChoose hypothesis test:")
print("1. Two-tailed test ( $H_1: \mu \neq \mu_0$ )")
print("2. Right-tailed test ( $H_1: \mu > \mu_0$ )")
print("3. Left-tailed test ( $H_1: \mu < \mu_0$ )")

test_type = int(input("Enter option (1/2/3): "))

print("\nTest Results:\n")

output = z_test_critical(
    mean_h0, sample_avg, pop_std, size_n, sig_level, test_type
)

for key, value in output.items():
    print(f"{key}: {value}")

print("\n")
```

#### Z-Test Hypothesis Testing Using Critical Value Method

Enter population standard deviation: 10  
Enter null hypothesis mean ( $\mu_0$ ): 50  
Enter observed sample mean: 52  
Enter number of observations: 36  
Enter significance level: 0.05

Choose hypothesis test:  
1. Two-tailed test ( $H_1: \mu \neq \mu_0$ )  
2. Right-tailed test ( $H_1: \mu > \mu_0$ )  
3. Left-tailed test ( $H_1: \mu < \mu_0$ )  
Enter option (1/2/3): 2

#### Test Results:

Test Type: Right-tailed  
Critical z: 1.6448536269514722  
Upper CV: 52.741422711585784  
Sample Mean: 52.0

Decision: Fail to Reject  $H_0$