## **Predicting Public Housing Prices Using Delayed Neural Networks**

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Abstract—This study uses delayed neural network models to predict public housing prices in Singapore. The delayed neural networks are used to estimate the trend of the resale price index (RPI) of Singapore housing from the Singapore Housing Development Board (HDB), with nine independent economic and demographic variables. The results show that the delayed neural network model is able to produce a good fit and predictions.

Index Terms—Artificial neural network (ANN), public housing prices, estimate, Singapore

### I. INTRODUCTION

Public housing in Singapore is important to the residents, as more than 80% of the nation's population live in the Housing and Development Board (HDB) flats nowadays. According to the Department of Statistics of Singapore, the population density of Singapore is one of the highest in the world.

Against this background, it could be beneficial to have a reliable prediction of the public housing prices. Based on the pricing predictions, the authority can better develop sustainable public housing plans and forestall any housing bubbles. With such predictions, investors could maximize profits gained from the performed transactions, whereas potential buyers will acquire the basic understanding of the latest pricing trends, enabling them to make informed decisions and reducing the risk of loss.

Traditionally, various approaches have been introduced to forecast the housing prices. Some of the most widely used methods include the sales comparison grid and, more recently, the hedonic pricing models derived from multiple regression analysis. Nonetheless, both of these methods have their respective shortcomings. According to Worzala et al. [1], the sales comparison grid is criticized as inaccurate due to the difficulty in obtaining reliable data. Hedonic pricing, on the other hand, not only is unable to effectively capture the multi co-linearity and non-linearity among the variables, but also involves statistical assumptions in the samples. Therefore, the results generated might be unfavorable.

Artificial neural networks (ANN) are recognized for their learning and generalization abilities [2]. ANNs are able to approximate the mapping of arbitrary nonlinear variables [3-13]. Today, ANNs are used not only for housing prices estimation (e.g., [14-33]), but also in other fields, such as stock price index estimation (e.g., [34-42]) and many types of time series prediction (e.g., [43-48]).

Numerous studies have been conducted to assess the effectiveness of ANNs in housing price predictions. In this

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context, ANN has been applied for more than 20 years (e.g., [14-33]).

The main objective of this study is to examine the accuracy of ANNs in predicting Singapore's public housing prices. In order to fulfill this objective, we will attempt to identify the possible factors influencing the public housing prices.

In Section 2, a dynamic ANN is used for forecasting, as the time factor is now taken into consideration. It is undeniable that the public housing price varies over time. Therefore, timeseries data is used as the input and output variables. Besides that, it is assumed that economic variables will play an important role in determining the price trend of public housing. As a result, several economic and demographic factors are chosen as the inputs.

# II. PREDICTING PUBLIC HOUSING PRICES USING DELAYED NEURAL NETWORKS

The housing prices could be affected by the characteristics of a particular housing unit, as well as other economic and demographic factors [49-54].

There are a number factors to be taken in consideration when evaluating the potential selling price of a HDB unit, of which the following six are intrinsic to each unit:

- Number of rooms
- Floor / Level
- Area of floor space
- Duration of elapsed lease ("Age" of the HDB unit)
- Distance to the nearest school
- Distance to the nearest subway (MRT) station

In this study, ten Singapore economic variables are initially considered as exogenous variables, which may exhibit a strong correlation with the housing prices. Before training the ANN, these variables are to undergo a correlation test to determine the most suitable variables for the input vectors. All the ten variables are listed as follows:

- Singapore Real Gross Domestic Product (GDP)
- Population
- Unemployment Rate
- Average Monthly Wages
- · Labour Cost
- Straits Times Index (STI) for Singapore stock market
- Prime Lending Rate
- Interbank Rate
- Singapore Consumer Spending
- Singapore Consumer Price Index (CPI)

There are several general steps when developing and implementing the ANN model, as listed below:

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- 1. Data Collection and Preprocessing
- 2. Network Creation and Configuration
- 3. Network Training, Validation and Testing
- 4. Result Analysis

This study consists of two parts, i.e., (1) MATLAB Neural Network Fitting Tool and (2) the MATLAB Neural Network Time Series Tool will be deployed.

The data used for part 1 is retrieved from the HDB and the PropertyGuru websites [49-54]. The statistics of the HDB resale prices are collected for the 26 HDB estates in Singapore, from December 2012 to February 2014.

There are six input (independent) variables to be examined, as indicated earlier. The targeted output variable is the resale price of the HDB unit (in ten thousands of Singapore Dollar, i.e., \$\$ '0,000).

Meanwhile, the data used in part 2 is different from that of part 1. In part 2, the independent variables used are listed earlier, while the HDB Resale Price Index (RPI) is chosen as the dependent variable. RPI acts as the single indicator that reflects the movements of public housing prices.

For all the variables, quarterly time-series data from 1990 Quarter 1 to 2013 Quarter 4 are used for the ANN model training, validation and testing. There are a total of 96 time steps for each of the time-series data. These data are collected from HDB and Trading Economy website (online resources) [49-54].

In this analysis, the feed-forward ANN models constructed are of different architecture (in terms of the number of hidden layer and neurons), and different distribution ratio of data samples are used for training, validation and testing purposes. The default training algorithm to be used is the Levenberg-Marquardt algorithm. The two main performance indicators are the Mean Squared Error (MSE) and Regression Value (R-value). Each ANN model is to be trained for several times, and the best-performed ANN is chosen based on the lowest MSE value generated.

Table 1. Exprimental Results

Gro up	ANN Archite cture	Data Sample Distribution Ratio	Average MSE	Overall R- value
1	6-8-1	60:20:20	3.882	0.9554
2	6-8-1	60:20:20	39.90	0.9062
3	6-10-1	60:20:20	21.46	0.9209
4	6-15-1	70:15:15	13.03	0.9579

From Table 1, it can be observed that the results produced by the ANN model are acceptable. For the cases of best-performed ANNs, the R-value lies between 0.9062 and 0.9579. This shows that there are strong correlations between the generated outputs and the targeted outputs. The ANN is able to formulate a good fit between those independent variables with the corresponding dependent variable.

In Figure 1, it can be seen that the ANN is able to produce accurate forecasts for most of the time steps. However, significant errors occurred around the 10th, 20th and 30th time steps. Generally, the predictions are reliable, since most of the

error correlations are within the 95% confidence limit (except for the one at zero lag). The R-values for training, validation and testing are 0.997 and above. The low MSE values imply that the ANN model is able to produce predictions close to the actual output targets.

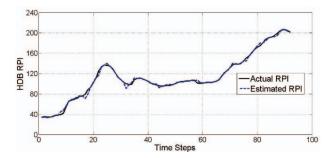


Fig. 1. Plot of RPI against Time Steps

### III. CONCLUSION

The study aims to evaluate the effectiveness of artificial neural network in predicting the Singapore public housing prices. The analysis has shown that the neural network is able to provide estimations that correlate well with the real housing market situation.

For static ANNs, the neural network model is able to map the non-linear relationship between resale price and those housing characteristics that influence the housing price. The R-value for all the best-performed ANN models is higher than 0.9. Therefore, the fitting between independent variables and dependent variables is reasonably good. The performance of the static ANN can be improved after making changes to the training procedure.

For dynamic ANNs, the accuracy of the predictions is high, because the values of predicted RPI are close to the actual target. It has the ability to deduce and generalize the relationship between independent input vectors and the housing price index. The price index movement can therefore be estimated, with a relatively small error.

However, ANN has its limitations. One main problem is the inconsistency in the results. During the training process, the ANN model is capable of self-learning and adjusting the weights accordingly to minimize the error. The initial conditions of the network are totally different for each training, and there are neither formulae nor rules to be followed. As a result, no conclusion can be made on whether the obtained ANN architecture and the results produced are optimal. One may conduct n-fold cross validation or run multiple times with different initial weights.

To summarize, ANN is a useful tool in housing prices prediction and other financial applications. Nonetheless, users must also be aware of its underlying weaknesses, and caution is important when using ANN models for financial forecasting. In future studies, we shall use more rigorous techniques to select input features (e.g., [23-25]) and test other predictive models (e.g., [26-28])

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