ASSIGNMENT

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Question 12.13.6.11 In a game, a man wins a rupee for a six and loses a rupee for any other number when a fair die is thrown. The man decided to throw a die thrice but to quit as and when he gets a six. Find the expected value of the amount he wins / loses.

Solution: Random variables defined as

Random Variable	Values	Description
X	$\{0,1,2,3\}$	6 appeared roll

k be roll on which 6 appeared.Let m_k be money recieved till 6 appeared.

$$p_X(k) = \begin{cases} \left(\frac{5}{6}\right)^{k-1}\frac{1}{6} & \text{if } k \in \{1,2,3\} \\ \left(\frac{5}{6}\right)^3 & \text{if } k = 0 \\ 0 & \text{otherwise} \end{cases} \tag{1}$$

$$m_k = \begin{cases} (-1)(k-1)+1 & \text{if } k \in \{1,2,3\} \\ -3 & \text{if } k = 0 \end{cases} \tag{2}$$

Calculating the expected value

$$\text{Expected value} = \sum_{k=0}^{3} m_k p_X(k) \tag{3}$$

$$= (1 \times \frac{1}{6}) + (0 \times \frac{5}{36}) + (-1 \times \frac{25}{216})$$

$$+ (-3 \times \frac{125}{216}) \tag{4}$$

$$= \frac{1}{6} - 0 + \left(-\frac{25}{216}\right) - \frac{375}{216} \tag{5}$$

$$= \frac{36}{216} - 0 + \left(-\frac{25}{216}\right) - \frac{375}{216} \tag{6}$$

$$= \frac{36 - 0 - 25 - 375}{216} \tag{7}$$

$$= -\frac{364}{216} \tag{8}$$

$$\approx -1.685 \tag{9}$$