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ASSIGNMENT

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Question 12.13.6.11 In a game, a man wins a rupee for a six and loses a rupee for any other number when a fair die is thrown. The man decided to throw a die thrice but to quit as and when he gets a six. Find the expected value of the amount he wins / loses.

Solution: For $i \in \{1, 2, 3\}$. Random variables defined as

Random Variable	Values	Description
X_i	$\{-1, 1\}$	Money recieved on "i th " roll

$$P_{X_i}(k) = \begin{cases} \frac{1}{6} & \text{if } k = 1\\ \frac{5}{6} & \text{if } k = -1\\ 0 & \text{otherwise} \end{cases}$$
 (1)

$$E(X_i) = \sum_{i=1}^{n-1} k P_{X_i}(k)$$
 (2)

$$= (-1)\frac{5}{6} + 0 + (1)\frac{1}{6} \tag{3}$$

$$=-\frac{4}{6}\tag{4}$$

Calculating the expected value

$$E(X) = E(X_1) + P_{X_1}(-1) \cdot E(X_2)$$

+ $P_{X_1}(-1) \cdot P_{X_2}(-1) \cdot E(X_3)$ (5)

$$E(X) = E(X_1) + \frac{5}{6} \cdot E(X_2) + \frac{25}{36} \cdot E(X_3)$$
 (6)

$$= \left(-\frac{4}{6}\right) + \frac{5}{6}\left(-\frac{4}{6}\right) + \frac{25}{36}\left(-\frac{4}{6}\right) \tag{7}$$

$$= \left(-\frac{4}{6}\right) \left(\frac{36+30+25}{36}\right) \tag{8}$$

$$=\left(-\frac{364}{216}\right)\tag{9}$$

$$\approx -1.685\tag{10}$$