# Assignment\_3

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knitr::opts chunk\$set(echo = TRUE)

#Summary 1. Using the information in this dataset, if an accident has just been reported and no further information is available, what should the prediction be? (INJURY = Yes or No?) Why? Ans: According to the data in this dataset, there is a 50.88% chance that an injury occurred if an accident has just been reported and no other information is available. This is because data indicates that earlier out of 42,183 cases, 21,462 cases had reported "injury=yes."

2. Select the first 24 records in the dataset and look only at the response (INJURY) and the two predictors WEATHER\_R and TRAF\_CON\_R. Create a pivot table that examines INJURY as a function of the two predictors for these 12 records. Use all three variables in the pivot table as rows/columns? 2.1:- Compute the exact Bayes conditional probabilities of an injury (INJURY = Yes) given the six possible combinations of the predictors? Ans: For each of the six potential combinations of the predictors, the precise Bayes conditional probabilities of an injury (INJURY = Yes) are:

Predictor combination Probability WEATHER\_R = 1 and TRAF\_CON\_R = 1 0.6666667 WEATHER\_R = 2 and TRAF\_CON\_R = 0 0.1818182 WEATHER\_R = 1 and TRAF\_CON\_R = 1 0.0000000 WEATHER\_R = 2 and TRAF\_CON\_R = 1 0.0000000 WEATHER\_R = 1 and TRAF\_CON\_R = 2 0.0000000 WEATHER\_R = 2 and TRAF\_CON\_R = 2 0.0000000

2.2:-Classify the 24 accidents using these probabilities and a cutoff of 0.5? Ans: The 24 accidents are quantitatively classified using their probability and a cutoff of 0.5:

 $\begin{bmatrix} 0.6666667 \ 0.1818182 \ 0.00000000 \ 0.00000000 \ 0.66666667 \ 0.1818182 \ 0.1818182 \ 0.6666667 \\ 0.1818182 \ 0.1818182$ 

qualitatively are:

["yes" "no" "no" "no" "yes" "no" "no" "no" "no" "no" "no" "yes" "yes" "yes" "yes" "yes" "no" "no" "no" "ves" "ves" "ves" "ves" "no"]

2.3:-Compute manually the naive Bayes conditional probability of an injury given WEATHER\_R = 1 and TRAF\_CON\_R = 1? Ans: The probability or output was "0" when the naive Bayes conditional probability of an injury was manually calculated using WEATHER\_R = 1 and TRAF\_CON\_R = 1.

- 2.4:-Run a naive Bayes classifier on the 24 records and two predictors. Check the model output to obtain probabilities and classifications for all 24 records. Compare this to the exact Bayes classification. Are the resulting classifications equivalent? Is the ranking (= ordering) of observations equivalent? Ans: Now that the naive Bayes classifier has been applied to the 24 records and two predictors, it has been discovered that the resultant classifications and rankings do not match those of the exact Bayes computation. This was discovered after checking the model output to acquire probabilities and classifications for all 24 records.
  - 3. Let us now return to the entire dataset. Partition the data into training (60%) and validation (40%)? 3.1:- Run a naive Bayes classifier on the complete training set with the relevant predictors (and INJURY as the response). Note that all predictors are categorical. Show the confusion matrix? Ans: Using the naive Bayes classifier on the complete training set with the relevant predictors (and INJURY as the response) The Following Confusion Matrix and Statistics are obtained. The accuracy comes out to be 53.7%.

**Confusion Matrix and Statistics** 

Reference

Prediction no yes no 3444 4866 yes 2947 5617

Accuracy: 0.537

3.2:- What is the overall error of the validation set? Ans: The overall error of the validation set is "46.3".

#### **Problem Statement**

The file accidentsFull.csv contains information on 42,183 actual automobile accidents in 2001 in the United States that involved one of three levels of injury: NO INJURY, INJURY, or FATALITY. For each accident, additional information is recorded, such as day of week, weather conditions, and road type. A firm might be interested in developing a system for quickly classifying the severity of an accident based on initial reports and associated data in the system (some of which rely on GPS-assisted reporting).

Our goal here is to predict whether an accident just reported will involve an injury  $(MAX\_SEV\_IR = 1 \text{ or } 2)$  or will not  $(MAX\_SEV\_IR = 0)$ . For this purpose, create a dummy variable called INJURY that takes the value "yes" if  $MAX\_SEV\_IR = 1$  or 2, and otherwise "no."

- 1. Using the information in this dataset, if an accident has just been reported and no further information is available, what should the prediction be? (INJURY = Yes or No?) Why?
- 2. Select the first 24 records in the dataset and look only at the response (INJURY) and the two predictors WEATHER\_R and TRAF\_CON\_R. Create a pivot table that examines INJURY as a function of the two predictors for these 12 records. Use all

three variables in the pivot table as rows/columns. 2.1:- Compute the exact Bayes conditional probabilities of an injury (INJURY = Yes) given the six possible combinations of the predictors. 2.2:-Classify the 24 accidents using these probabilities and a cutoff of 0.5. 2.3:-Compute manually the naive Bayes conditional probability of an injury given WEATHER\_R = 1 and TRAF\_CON\_R = 1. 2.4:-Run a naive Bayes classifier on the 24 records and two predictors. Check the model output to obtain probabilities and classifications for all 24 records. Compare this to the exact Bayes classification. Are the resulting classifications equivalent? Is the ranking (= ordering) of observations equivalent?

3. Let us now return to the entire dataset. Partition the data into training (60%) and validation (40%). 3.1:- Run a naive Bayes classifier on the complete training set with the relevant predictors (and INJURY as the response). Note that all predictors are categorical. Show the confusion matrix. 3.2:- What is the overall error of the validation set?

## **Data Importing and Cleaning**

Install and load the required package

```
library(e1071)
library(caret)

## Loading required package: ggplot2

## Loading required package: lattice
library(ggplot2)
```

Q1. Using the information in this dataset, if an accident has just been reported and no further information is available, what should the prediction be? (INJURY = Yes or No?) Why?

```
accidents <- read.csv("C:\\Users\\yashw\\FML\\accidentsFull.csv")</pre>
accidents$INJURY = ifelse(accidents$MAX_SEV_IR>0,"yes","no")
injury table <- table(accidents$INJURY)</pre>
injury_table
##
##
      no
            yes
## 20721 21462
head(accidents)
##
     HOUR I R ALCHL I ALIGN I STRATUM R WRK ZONE WKDY I R INT HWY LGTCON I R
## 1
             0
                      2
                               2
                                          1
                                                    0
                                                               1
                                                                        0
                                                                                    3
             1
                      2
                               1
                                          0
                                                    0
                                                               1
                                                                                    3
## 2
                                                                        1
             1
                      2
                               1
                                          0
                                                    0
                                                               1
                                                                        0
                                                                                    3
## 3
             1
                      2
                               1
                                                    0
                                                                                    3
## 4
                                          1
                                                               0
                                                                        0
                                                                                    3
## 5
             1
                      1
                               1
                                          0
                                                    0
                                                               1
                                                                        0
## 6
             1
                      2
                               1
                                          1
                                                    0
                                                               1
```

```
MANCOL I R PED ACC R RELJCT I R REL RWY R PROFIL I R SPD LIM SUR COND
## 1
                                                                        40
                                        1
                                                                1
## 2
                2
                           0
                                        1
                                                   1
                                                                1
                                                                        70
                                                                                    4
## 3
                2
                           0
                                        1
                                                                1
                                                                        35
                                                                                    4
                                                   1
## 4
                2
                           0
                                        1
                                                   1
                                                                1
                                                                        35
                                                                                    4
## 5
                2
                           0
                                        0
                                                   1
                                                                1
                                                                        25
                                                                                    4
                                        1
                                                                                    4
## 6
                           0
                                                   0
                                                                1
                                                                        70
     TRAF_CON_R TRAF_WAY VEH_INVL WEATHER_R INJURY_CRASH NO_INJ_I
PRPTYDMG CRASH
## 1
                          3
                                    1
                                                1
                                                               1
                                                                         1
0
                          3
                                    2
                                                2
## 2
                0
                                                               0
                                                                         0
1
                          2
                                                2
## 3
                1
                                    2
                                                               0
                                                                         0
1
                          2
                                    2
## 4
                1
                                                1
                                                               0
                                                                         0
1
                          2
## 5
                0
                                    3
                                                1
                                                               0
                                                                         0
1
                          2
                                                2
## 6
                0
                                    1
                                                               1
                                                                         1
0
##
     FATALITIES MAX_SEV_IR INJURY
## 1
                0
                            1
                                  yes
## 2
                0
                            0
                                   no
## 3
                            0
                0
                                   no
## 4
                0
                            0
                                   no
                            0
## 5
                0
                                   no
## 6
                            1
                0
                                  yes
probability_injury <- (injury_table["yes"] / sum(injury_table))*100</pre>
probability_injury
##
         ves
## 50.87832
#converting factors from variables
for (i in c(1:dim(accidents)[2])){
  accidents[,i] <- as.factor(accidents[,i])</pre>
}
head(accidents, n=24)
       HOUR I R ALCHL I ALIGN I STRATUM R WRK ZONE WKDY I R INT HWY LGTCON I R
##
## 1
                        2
               0
                                 2
                                             1
                                                       0
                                                                 1
                                                                          0
                                                                                       3
## 2
               1
                        2
                                 1
                                            0
                                                       0
                                                                 1
                                                                          1
                                                                                       3
               1
                        2
                                                                                       3
## 3
                                 1
                                            0
                                                       0
                                                                 1
                                                                          0
               1
                        2
                                                                                       3
## 4
                                 1
                                            1
                                                       0
                                                                 0
                                                                          0
               1
                        1
                                 1
                                            0
                                                       0
                                                                 1
                                                                          0
                                                                                       3
## 5
                        2
                                                                                       3
## 6
               1
                                 1
                                             1
                                                       0
                                                                 1
                                                                          0
               1
                        2
                                 1
                                            0
                                                       0
                                                                 1
                                                                          1
                                                                                       3
## 7
## 8
               1
                        2
                                 1
                                            1
                                                       0
                                                                 1
                                                                          0
                                                                                       3
               1
                        2
                                 1
                                                       0
                                                                 1
                                                                          0
                                                                                       3
## 9
                                             1
```

##	10	0	2	1	0		0	0	0		3
	11	1	2	1	0		0	1	0		3
	12	1	2	1	1		0	1	0		3
##	13	1	2	1	1		0	1	0		3
##	14	1	2	2	0		0	1	0		3
##		1	2	2	1		0	1	0		3
##		1	2	2	1		0	1	0		3
##		1	2	1	1		0	1	0		3
	18	1	2	1	1		0	0	0		3
##		1	2	1	1		0	1	0		3
##		1	2	1	0		0	1	0		3
	21	1	2	1	1		0	1	0		3
	22	1	2	2	0		0	1	0		3
	23 24	1	2	1	0		0	1	9 9		3
##	24	MANICOL T P	2 PED_ACC_R	1 PEL 10T T	D DEI	DI/IV D	DPOETL T	1 p cr		CLID COND	2
##	1	MANCOL_I_N		KELJCI_I_	N NEL_	-TW1_N	PROFIL_I	_^ 3F	40	30K_COND 4	
##		2			1	1		1	70	4	
##		2			1	1		1	35	4	
##		2			1	1		1	35	4	
##		2			0	1		1	25	4	
##		ē			1	0		1	70	4	
	7	6			0	0		1	70	4	
##	8	0			0	0		1	35	4	
##	9	0	0		1	0		1	30	4	
##	10	6	0		1	0		1	25	4	
##	11	0	0		0	0		1	55	4	
	12	2	. 0		0	1		1	40	4	
##		1	. 0		0	1		1	40	4	
##		6			0	0		1	25	4	
##		0	) 0		0	0		1	35	4	
##		0	_		0	0		1	45	4	
	17	0			0	0		1	20	4	
##		0			0	0		1	50	4	
	19	0			0	0		1	55	4	
	20	0			1	1		1	55 45	4	
##	22	0			1 1	0 0		0 0	45 65	4 4	
##		9			0	0		0	65 65	4	
	24	2			1	1		0	55	4	
##	4		TRAF_WAY				IIIRV CRAS				
	ТҮГ	DMG_CRASH		VE.I	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		, o.r.1_c.r.		_==		
##		0	3	1		1		1	1		
0				_					_		
##	2	e	3	2		2		0	0		
1											
##	3	1	. 2	2		2		0	0		
1											
##	4	1	. 2	2		1		0	0		
1											

##	5	0	2	3	1	0	0	
1 ##	6	0	2	1	2	1	1	
0 ##	7	0	2	1	2	0	0	
1 ##	8	0	1	1	1	1	1	
0 ##	9	0	1	1	2	0	0	
	10	0	1	1	2	0	0	
1 ##	11	0	1	1	2	0	0	
1 ##	12	2	1	2	1	0	0	
1 ##	13	0	1	4	1	1	2	
	14	0	1	1	1	0	0	
1 ##	15	0	1	1	1	1	1	
	16	0	1	1	1	1	1	
	17	0	1	1	2	0	0	
1 ##	18	0	1	1	2	0	0	
1 ##	19	0	1	1	2	0	0	
	20	0	1	1	2	0	0	
1 ##	21	0	3	1	1	1	1	
	22	0	3	1	1	0	0	
1 ##	23	2	2	1	2	1	2	
0 ##	24	0	2	2	2	1	1	
0 ##		EATAL TTTES	MAX_SEV_IR	TNJLIBV				
##		0	1	yes				
##	2	0	0	no				
##		0	0	no				
##		0	0	no				
## ##		0 0	0	no				
##		0	1 0	yes no				
##		0	1	yes				
##		0	0	no				

```
## 10
                               0
                                      no
                  0
## 11
                               0
                                      no
                  0
## 12
                               0
                                      no
## 13
                  0
                               1
                                     yes
                  0
                               0
## 14
                                      no
## 15
                  0
                               1
                                     yes
                  0
## 16
                               1
                                     yes
                  0
                               0
## 17
                                      no
                  0
## 18
                               0
                                      no
## 19
                  0
                               0
                                      no
                  0
                               0
## 20
                                      no
                  0
                               1
## 21
                                     yes
                  0
## 22
                               0
                                      no
## 23
                  0
                               1
                                     yes
## 24
                  0
                               1
                                     yes
```

Q2. Select the first 24 records in the dataset and look only at the response (INJURY) and the two predictors WEATHER\_R and TRAF\_CON\_R. Create a pivot table that examines INJURY as a function of the two predictors for these 12 records. Use all three variables in the pivot table as rows/columns. 2.1:- Compute the exact Bayes conditional probabilities of an injury (INJURY = Yes) given the six possible combinations of the predictors. 2.2:-Classify the 24 accidents using these probabilities and a cutoff of 0.5. 2.3:=Compute manually the naive Bayes conditional probability of an injury given WEATHER\_R = 1 and TRAF\_CON\_R = 1. 2.4:-Run a naive Bayes classifier on the 24 records and two predictors. Check the model output to obtain probabilities and classifications for all 24 records. Compare this to the exact Bayes classification. Are the resulting classifications equivalent? Is the ranking (= ordering) of observations equivalent?

```
accidents24 <- accidents[1:24,c("INJURY","WEATHER_R","TRAF_CON_R")]</pre>
head(accidents24)
     INJURY WEATHER R TRAF CON R
##
## 1
        yes
                     1
                     2
## 2
                                 0
         no
                     2
                                 1
## 3
         no
## 4
                     1
                                 1
         no
                     1
                                 0
## 5
         no
                     2
                                 0
## 6
        yes
Pt1 <- ftable(accidents24)
Pt2 <- ftable(accidents24[,-1]) # print table only for conditions
Pt1
                     TRAF CON R Ø 1 2
##
## INJURY WEATHER_R
## no
          1
                                 3 1 1
##
           2
                                 9 1 0
          1
## yes
                                 6 0 0
          2
##
                                 2 0 1
```

```
Pt2

## TRAF_CON_R 0 1 2

## WEATHER_R

## 1 9 1 1

## 2 11 1 1
```

2.1:- Compute the exact Bayes conditional probabilities of an injury (INJURY = Yes) given the six possible combinations of the predictors.

```
#Injury = yes
p1 = Pt1[3,1] / Pt2[1,1] # Injury, Weather=1 and Traf=0
p2 = Pt1[4,1] / Pt2[2,1] # Injury, Weather=2, Traf=0
p3 = Pt1[3,2] / Pt2[1,2] # Injury, W=1, T=1
p4 = Pt1[4,2] / Pt2[2,2] # I, W=2,T=1
p5 = Pt1[3,3] / Pt2[1,3] # I, W=1,T=2
p6 = Pt1[4,3]/ Pt2[2,3] \#I,W=2,T=2
# Injury = no
n1 = Pt1[1,1] / Pt2[1,1] # Weather=1 and Traf=0
n2 = Pt1[2,1] / Pt2[2,1] # Weather=2, Traf=0
n3 = Pt1[1,2] / Pt2[1,2] # W=1, T=1
n4 = Pt1[2,2] / Pt2[2,2] # W=2,T=1
n5 = Pt1[1,3] / Pt2[1,3] # W=1,T=2
n6 = Pt1[2,3] / Pt2[2,3] # W=2,T=2
print(c(p1,p2,p3,p4,p5,p6))
## [1] 0.6666667 0.1818182 0.0000000 0.0000000 0.0000000 1.0000000
print(c(n1,n2,n3,n4,n5,n6))
```

2.2:-Classify the 24 accidents using these probabilities and a cutoff of 0.5.

```
prob.inj <- rep(0,24)

for (i in 1:24) {
    print(c(accidents24$WEATHER_R[i],accidents24$TRAF_CON_R[i]))
    if (accidents24$WEATHER_R[i] == "1") {
        if (accidents24$TRAF_CON_R[i]=="0"){
            prob.inj[i] = p1
        }
        else if (accidents24$TRAF_CON_R[i]=="1") {
            prob.inj[i] = p3
        }
        else if (accidents24$TRAF_CON_R[i]=="2") {
            prob.inj[i] = p5
        }
    }
    else {</pre>
```

```
if (accidents24$TRAF_CON_R[i]=="0"){
        prob.inj[i] = p2
      else if (accidents24$TRAF_CON_R[i]=="1") {
        prob.inj[i] = p4
      else if (accidents24$TRAF_CON_R[i]=="2") {
        prob.inj[i] = p6
      }
    }
  }
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 1
## Levels: 1 2 0
## [1] 1 1
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 1 2
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
```

```
## [1] 2 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 2
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
accidents24$prob.inj <- prob.inj
accidents24$prob.inj
## [1] 0.6666667 0.1818182 0.0000000 0.0000000 0.6666667 0.1818182 0.1818182
## [8] 0.6666667 0.1818182 0.1818182 0.1818182 0.0000000 0.6666667 0.6666667
## [15] 0.6666667 0.6666667 0.1818182 0.1818182 0.1818182 0.1818182 0.6666667
## [22] 0.6666667 1.0000000 0.1818182
accidents24$pred.prob <- ifelse(accidents24$prob.inj>0.5, "yes", "no")
accidents24$pred.prob
## [1] "yes" "no" "no" "no" "yes" "no" "no"
                                                 "yes" "no" "no" "no"
"no"
## [13] "yes" "yes" "yes" "no" "no" "no"
                                                 "no" "ves" "ves" "ves"
"no"
```

- 2.3Compute manually the naive Bayes conditional probability of an injury given WEATHER\_R = 1 and TRAF\_CON\_R = 1. Answer:Probability(Injury=Yes/WEATHER\_R=1,TRAF\_CON\_R=1)
- = [ Probability(W=1/Injury=Yes) \* Probability(TRAF\_CON\_R=1/Injury=Yes) \* Probability(Injury=Yes) ] / [ Probability(W=1/Injury=Yes) \* Probability(TRAF\_CON\_R=1/Injury=Yes) \* Probability(Injury=Yes) + Probability(WEATHER\_R=1/Injury=No) \* Probability(TRAF\_CON\_R=1/Injury=No) \* Probability(Injury=No) ]
- = [6/9\*0/9\*9/24]/[6/9\*0/9\*9/24+5/15\*2/15\*15/24] = The result will be "0" since the numerator is equal to zero.
- 2.4:- Run a naive Bayes classifier on the 24 records and two predictors. Check the model output to obtain probabilities and classifications for all 24 records. Compare this to the exact Bayes classification. Are the resulting classifications equivalent? Is the ranking (= ordering) of observations equivalent?

```
## [1] 0.571428571 0.250000000 0.002244949 0.008919722 0.571428571 0.250000000 ## [7] 0.250000000 0.571428571 0.250000000 0.250000000 0.250000000 0.666666667 ## [13] 0.571428571 0.571428571 0.571428571 0.571428571 0.250000000 0.250000000 ## [19] 0.250000000 0.250000000 0.571428571 0.571428571 0.333333333 0.250000000
```

Let us use Caret

```
library(klaR)
## Loading required package: MASS
#Loading the klaR package for Naive Bayes
# Creating a variable named formula that includes all variables of interest
formula <- INJURY ~ TRAF_CON_R + WEATHER_R
# Training the Naive Bayes model with Laplace
accidents24$INJURY <- as.factor(accidents24$INJURY)</pre>
nb2 <- NaiveBayes(formula,data = accidents24, laplace = 1)</pre>
# Making predictions with the model
predict(nb2, newdata = accidents24[, c("INJURY", "WEATHER R",
"TRAF_CON_R")])
## $class
##
   1
        2
            3
                    5
                        6
                            7
                                8
                                    9
                                       10
                                           11 12 13 14 15 16 17
                                                                       18
19 20
## yes no no no yes no no yes no no no yes yes yes yes no no
no no
## 21 22 23 24
## yes yes no
## Levels: no yes
##
## $posterior
##
            no
                       yes
## 1 0.4285714 0.571428571
## 2 0.7500000 0.250000000
## 3 0.9977551 0.002244949
## 4 0.9910803 0.008919722
## 5 0.4285714 0.571428571
## 6 0.7500000 0.250000000
## 7 0.7500000 0.250000000
## 8 0.4285714 0.571428571
## 9 0.7500000 0.250000000
## 10 0.7500000 0.250000000
## 11 0.7500000 0.250000000
## 12 0.3333333 0.666666667
```

```
## 13 0.4285714 0.571428571
## 14 0.4285714 0.571428571
## 15 0.4285714 0.571428571
## 16 0.4285714 0.571428571
## 17 0.7500000 0.250000000
## 18 0.7500000 0.250000000
## 19 0.7500000 0.250000000
## 20 0.7500000 0.250000000
## 21 0.4285714 0.571428571
## 22 0.4285714 0.571428571
## 23 0.6666667 0.333333333
## 24 0.7500000 0.250000000
predict(nb2, newdata = accidents24[, c("INJURY", "WEATHER_R", "TRAF_CON_R")],
type = "raw")
## $class
##
   1
         2
             3
                 4
                     5
                         6
                            7
                                 8
                                     9
                                       10 11 12 13 14 15 16
                                                                   17
                                                                        18
19
   20
## yes
       no
           no
              no yes no no yes no no no yes yes yes yes no
                                                                       no
no no
##
   21
       22
                24
           23
## yes yes no
## Levels: no yes
##
## $posterior
##
             no
                        yes
## 1 0.4285714 0.571428571
## 2 0.7500000 0.250000000
## 3 0.9977551 0.002244949
## 4 0.9910803 0.008919722
## 5 0.4285714 0.571428571
## 6 0.7500000 0.250000000
## 7 0.7500000 0.250000000
## 8 0.4285714 0.571428571
## 9 0.7500000 0.250000000
## 10 0.7500000 0.250000000
## 11 0.7500000 0.250000000
## 12 0.3333333 0.666666667
## 13 0.4285714 0.571428571
## 14 0.4285714 0.571428571
## 15 0.4285714 0.571428571
## 16 0.4285714 0.571428571
## 17 0.7500000 0.250000000
## 18 0.7500000 0.250000000
## 19 0.7500000 0.250000000
## 20 0.7500000 0.250000000
## 21 0.4285714 0.571428571
## 22 0.4285714 0.571428571
```

```
## 23 0.6666667 0.3333333333
## 24 0.7500000 0.250000000

#predictions
#raw_probabilities

# Comparing the naive Bayes model and exact Bayes classification
classification_match <- all(accidents24$nbpred.prob == accidents24$prob.inj)
probability_match <- all.equal(accidents24$nbpred.prob, accidents24$prob.inj)

# Checking if classifications and rankings are equivalent
if (classification_match && is.na(probability_match)) {
    cat("The resulting classifications and rankings are equivalent.\n")
} else {
    cat("The resulting classifications and rankings are not equivalent.\n")
}

## The resulting classifications and rankings are not equivalent.\n")</pre>
```

Q3, Let us now return to the entire dataset. Partition the data into training (60%) and validation (40%). 3.1, Run a naive Bayes classifier on the complete training set with the relevant predictors(and INJURY as the response). Note that all predictors are categorical. Show the confusion matrix.

```
set.seed(123)
train.index <- sample(c(1:dim(accidents)[1]), dim(accidents)[1]*0.6)
train.df <- accidents[train.index,]</pre>
valid.df <- accidents[-train.index,]</pre>
#defining a variable to be used here
"TRAF CON R",
                      "TRAF WAY",
                                    "WEATHER R")
nbTotal <- naiveBayes(INJURY~.,data = train.df[,vars])</pre>
nbTotal
## Naive Bayes Classifier for Discrete Predictors
## Call:
## naiveBayes.default(x = X, y = Y, laplace = laplace)
##
## A-priori probabilities:
## Y
##
                 yes
         no
## 0.4903789 0.5096211
##
## Conditional probabilities:
##
       HOUR I R
## Y
                         1
  no 0.5690919 0.4309081
##
```

```
##
     ves 0.5690029 0.4309971
##
##
        ALIGN_I
## Y
                 1
     no 0.8726936 0.1273064
##
##
     yes 0.8696697 0.1303303
##
##
        WRK_ZONE
## Y
                              1
                  0
     no 0.97502216 0.02497784
##
##
     yes 0.97883393 0.02116607
##
##
        WKDY I R
## Y
##
     no 0.2190798 0.7809202
##
     yes 0.2384091 0.7615909
##
##
        INT HWY
## Y
##
     no 0.8491660624 0.1501087745 0.0007251632
##
     yes 0.8617615134 0.1374631726 0.0007753140
##
##
        LGTCON_I_R
## Y
##
     no 0.6871324 0.1285150 0.1843526
##
     yes 0.6957668 0.1131958 0.1910374
##
##
        PROFIL I R
## Y
##
     no 0.7555394 0.2444606
##
     yes 0.7617460 0.2382540
##
##
        SPD LIM
## Y
                    5
                                 10
                                              15
                                                            20
     no 8.057368e-05 7.251632e-04 4.673274e-03 8.299090e-03 1.099831e-01
##
     ves 7.753140e-05 3.876570e-04 4.419290e-03 4.729415e-03 9.094433e-02
##
##
        SPD_LIM
## Y
                   30
                                 35
                                              40
                                                            45
                                                                         50
     no 8.726130e-02 1.892676e-01 9.411006e-02 1.560712e-01 4.101201e-02
##
     ves 8.885098e-02 2.163901e-01 1.076911e-01 1.554505e-01 3.806792e-02
##
##
        SPD LIM
## Y
                                 60
                                              65
                                                            70
     no 1.604222e-01 3.545242e-02 6.711788e-02 3.948111e-02 6.043026e-03
##
     yes 1.532020e-01 4.209955e-02 6.179253e-02 2.876415e-02 7.132889e-03
##
##
##
        SUR_COND
## Y
                                2
                                            3
     no 0.778341794 0.173797438 0.015550721 0.028120216 0.004189832
##
##
     yes 0.815475267 0.153434641 0.011397116 0.015118623 0.004574353
##
```

```
TRAF_CON_R
##
## Y
                                      2
                 0
                           1
     no 0.6581259 0.1907985 0.1510757
##
##
     yes 0.6217243 0.2203442 0.1579315
##
##
        TRAF_WAY
## Y
                  1
                             2
     no 0.57360406 0.37426477 0.05213117
##
##
    yes 0.56419600 0.39471236 0.04109164
##
        WEATHER_R
##
## Y
                 1
##
     no 0.8411893 0.1588107
##
    yes 0.8717631 0.1282369
#generating the confusion matrix using the train.df, the prediction and the
confusionMatrix(train.df$INJURY, predict(nbTotal, train.df[, vars]), positive
= "yes")
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                no yes
##
          no 5214 7197
##
          yes 4475 8423
##
##
                  Accuracy : 0.5388
##
                    95% CI: (0.5327, 0.545)
##
       No Information Rate: 0.6172
##
       P-Value [Acc > NIR] : 1
##
##
                     Kappa: 0.0735
##
   Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 0.5392
##
##
               Specificity: 0.5381
##
            Pos Pred Value: 0.6530
##
            Neg Pred Value : 0.4201
##
                Prevalence: 0.6172
##
            Detection Rate: 0.3328
      Detection Prevalence: 0.5096
##
##
         Balanced Accuracy: 0.5387
##
##
          'Positive' Class : yes
##
```

3.2, What is the overall error of the validation set?

```
confusionMatrix(valid.df$INJURY, predict(nbTotal, valid.df[, vars]), positive
= "yes")
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                no yes
##
         no 3444 4866
##
          yes 2947 5617
##
                  Accuracy: 0.537
##
##
                    95% CI: (0.5294, 0.5445)
##
       No Information Rate: 0.6213
##
       P-Value [Acc > NIR] : 1
##
##
                     Kappa: 0.0706
##
##
   Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 0.5358
##
               Specificity: 0.5389
            Pos Pred Value: 0.6559
##
##
            Neg Pred Value : 0.4144
##
                Prevalence: 0.6213
            Detection Rate: 0.3329
##
##
      Detection Prevalence: 0.5075
##
         Balanced Accuracy: 0.5374
##
##
          'Positive' Class : yes
##
#Calculated overall error
ver=1-0.537
verp=ver*100
paste("Overall Error: ",verp)
## [1] "Overall Error: 46.3"
```

### #CONCLUSION

The Naive Bayes classifier was used firstly to predict injury outcomes in a data set with 24 records then to the entire data set with using two predictors both times.

Using the exact Bayes classifier for the first 24 records, we discover that the most risky combination for drivers is WEATHER\_CON=2,TRAF\_CON=0 because the likelihood for injury is maximal at "1" in this case.

The model's accuracy on the training set was 53.7%, and its validation error was 46.3%, showing a modest level of predictive ability. However, it makes the assumption that the predictor variables are independent, which may not always be the case in real-world

situations and might result in errors.But for classification and ranking, we can utilize the Naive Bayes classifier. Although Naive Bayes is a straightforward and useful