

Cartesian Product  $\Rightarrow$   
(multiplication of sets)

$|A| = 3$  cardinality  
 $A = \{k, l, m\}$   
 $B = \{q, r\}$   
 $|B| = 2$

$A \times B = \{(k, q), (k, r), (l, q), (l, r), (m, q), (m, r)\}$

ordered pair

$B \times A = \{(q, k), (q, l), (q, m), (r, k), (r, l), (r, m)\}$

$A \times B \neq B \times A$

$|A \times B| = ? \quad |A| \times |B| = 3 \times 2 = 6$

$|A \times B| = |B \times A|$

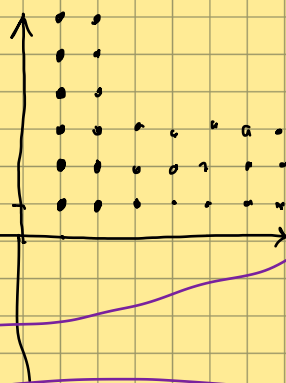
$\mathbb{N}, \mathbb{Z}, \mathbb{R}$

$\mathbb{N} \times \mathbb{N} = ? \quad \{(x, y) : x \in \mathbb{N}, y \in \mathbb{N}\}$

$\mathbb{N} = \{1, 2, 3, 4, \dots\}$

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$\mathbb{N} \times \mathbb{N}$



$\mathbb{N} \times \mathbb{N}$   
infinite

$\mathbb{N} \times \mathbb{N} = \{(1,1), (1,2), (1,3), (1,4), \dots, (2,1), (2,2), (2,3), (2,4), \dots, (3,1), (3,2), \dots, (4,1), \dots, (5,1), \dots\}$

I	✓
II	
III	
IV	

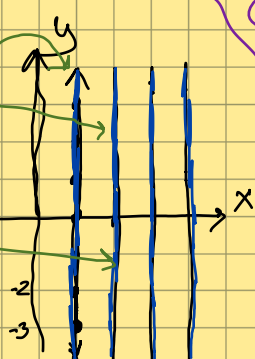
$\mathbb{N} \times \mathbb{R} = \{(x, y) : x \in \mathbb{N}, y \in \mathbb{R}\}$

$\{(1, -3), (1, -2), (1, -1), (1, 0), (1, 1), (1, 2), \dots\}$

$(2, -3) \dots$

$(3, -3) \dots$

$\vdots$



$\mathbb{R} \times \mathbb{N}$

