

Cartesian Product: $\rightarrow |A| = 3$ cardinality
 (multiplication)
 of sets
 $A = \{k, l, m\}$
 $B = \{q, r\}$
 $|B| = 2$

$$A \times B = \{(k, q), (k, r), (l, q), (l, r), (m, q), (m, r)\}$$

ordered pair

$$B \times A = \{(q, k), (q, l), (q, m), (r, k), (r, l), (r, m)\}$$

$$\rightarrow A \times B \neq B \times A$$

$$\rightarrow |A \times B| = ? \quad |A| \times |B| = 3 \cdot 2 = 6$$

$$\rightarrow \mathbb{N}, \mathbb{Z}, \mathbb{R}$$

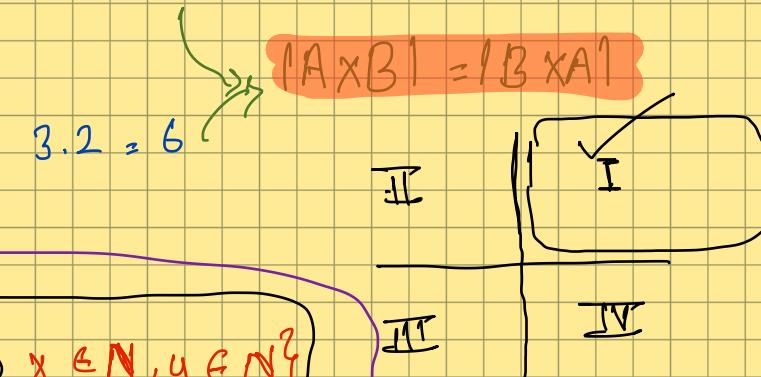
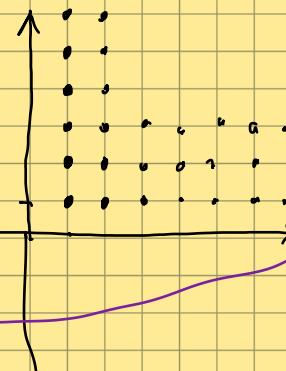
$$N \times N = ?$$

$$\{(x, y) : x \in \mathbb{N}, y \in \mathbb{N}\}$$

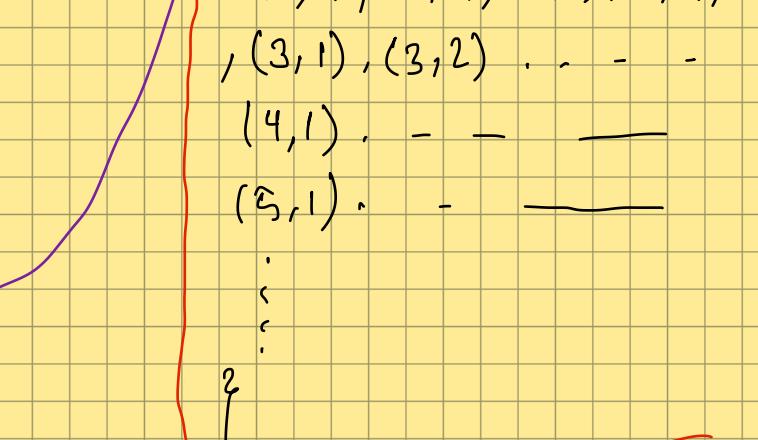
$$\rightarrow N = \{1, 2, 3, 4, \dots\}$$

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$$N \times N$$



$$N \times N = \{(1, 1), (1, 2), (1, 3), (1, 4), \dots, (2, 1), (2, 2), (2, 3), (2, 4), \dots, (3, 1), (3, 2), \dots, (4, 1), \dots, (5, 1), \dots\}$$



$$\rightarrow N \times \mathbb{R} = \{(x, y) : x \in \mathbb{N}, y \in \mathbb{R}\}$$

$$\{(1, -3), (1, -2), (1, -1), (1, 0), (1, 1), (1, 2), \dots, (2, -3), (2, -2), (2, -1), (2, 0), (2, 1), (2, 2), \dots, (3, -3), (3, -2), (3, -1), (3, 0), (3, 1), (3, 2), \dots\}$$

$$(2, -3), (2, -2), (2, -1), (2, 0), (2, 1), (2, 2)$$

$$(3, -3), (3, -2), (3, -1), (3, 0), (3, 1), (3, 2)$$

$$\rightarrow \mathbb{R} \times \mathbb{N}$$

